

ACN'2011

Conference/School of Young Scientists

"Diagnostics of Carbon Nanostructures"

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**Investigation of Atomic and Electron Structure
of Nanocarbon Materials
by Use of EXAFS and NEXAFS
Spectroscopy Techniques**



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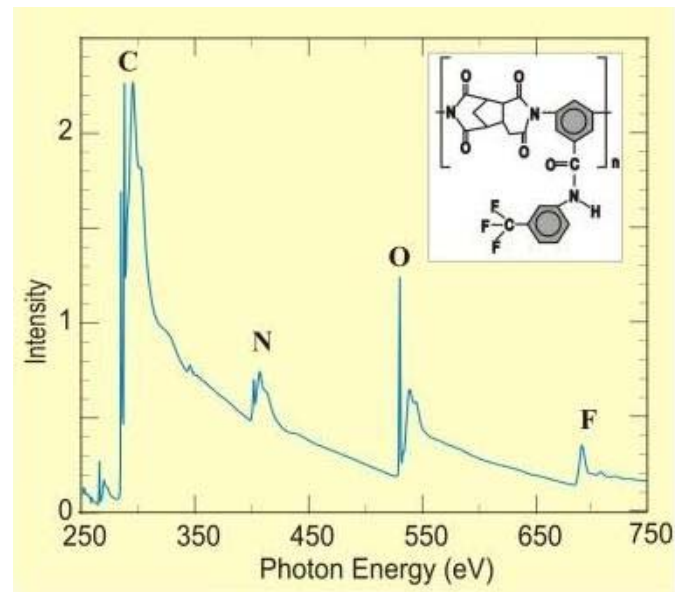
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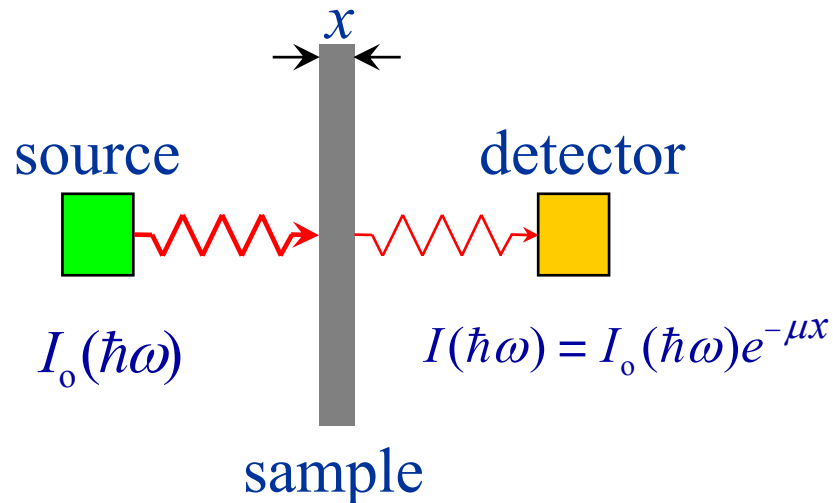
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2. Theoretical Background and a Little of History .
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I. Basic Concepts and Definitions



X-ray Absorption Spectroscopy (XAS): Basic Concepts ...



$$\mu(\hbar\omega) \propto \ln(I_0/I)$$



x-ray absorption coefficient

XAS of a polyimide polymer

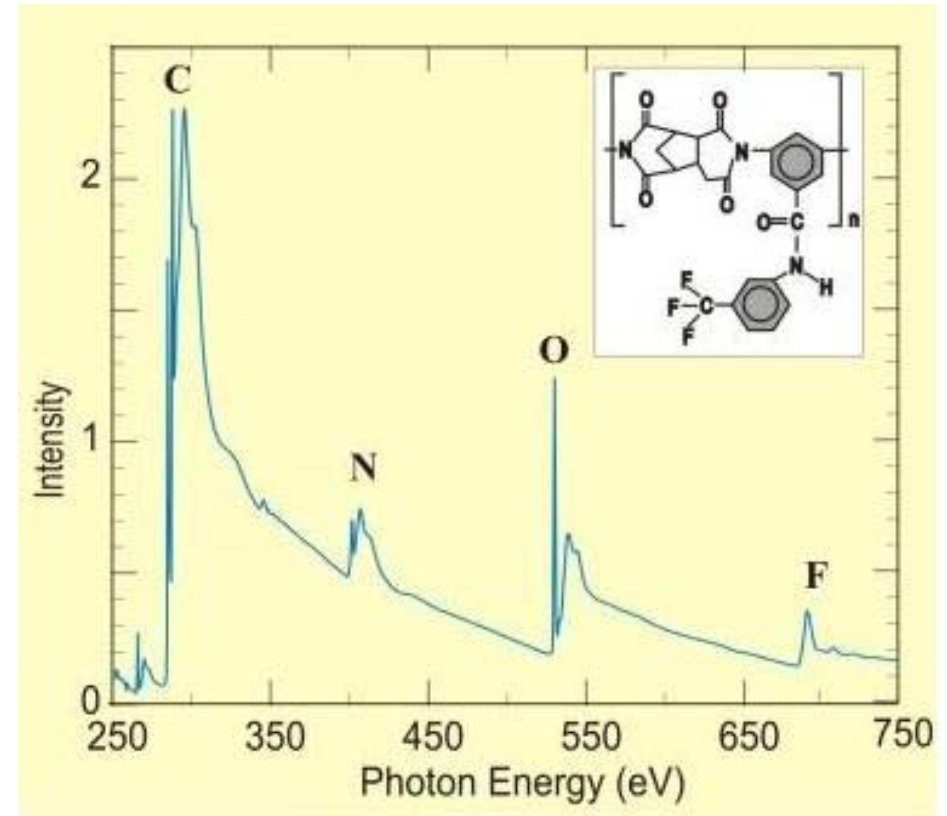


Figure reproduced from the site
<http://ssrl.slac.stanford.edu/stohr/nexafs.htm>
presenting the book
“J. Stöhr. NEXAFS spectroscopy. Springer, 1996”

...and Basic Definitions

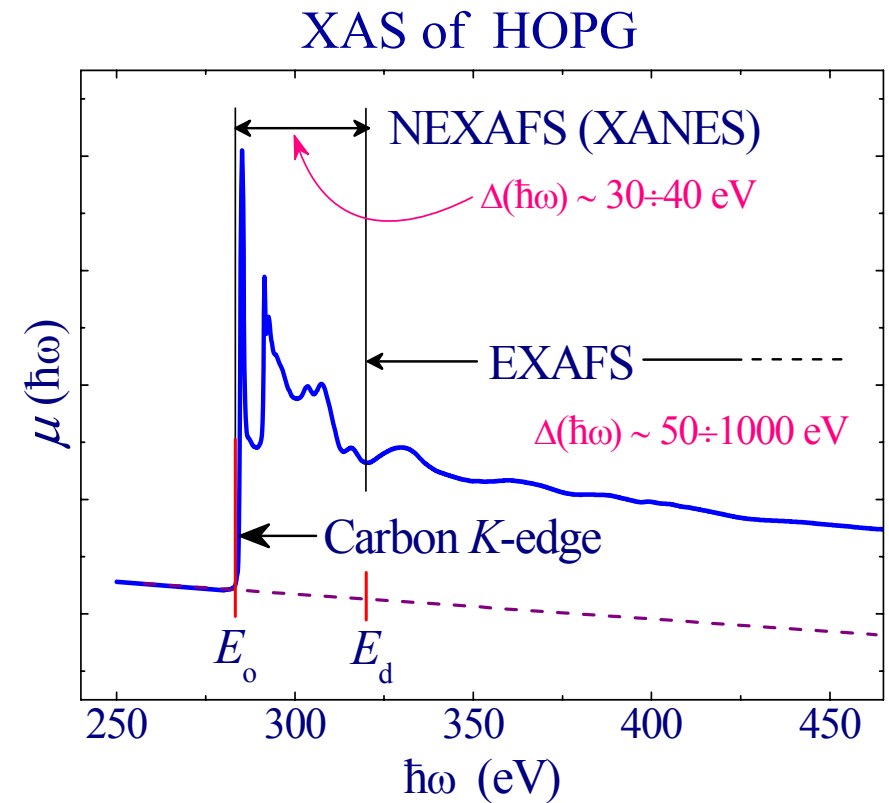
Near Edge X-ray Absorption Fine Structure
– NEXAFS

X-ray Absorption Near Edge Structure
– XANES

Extended X-ray Absorption Fine Structure
– EXAFS

Surface Extended X-ray Absorption Fine
Structure – SEXAFS

X-ray Absorption Fine Structure
– XAFS



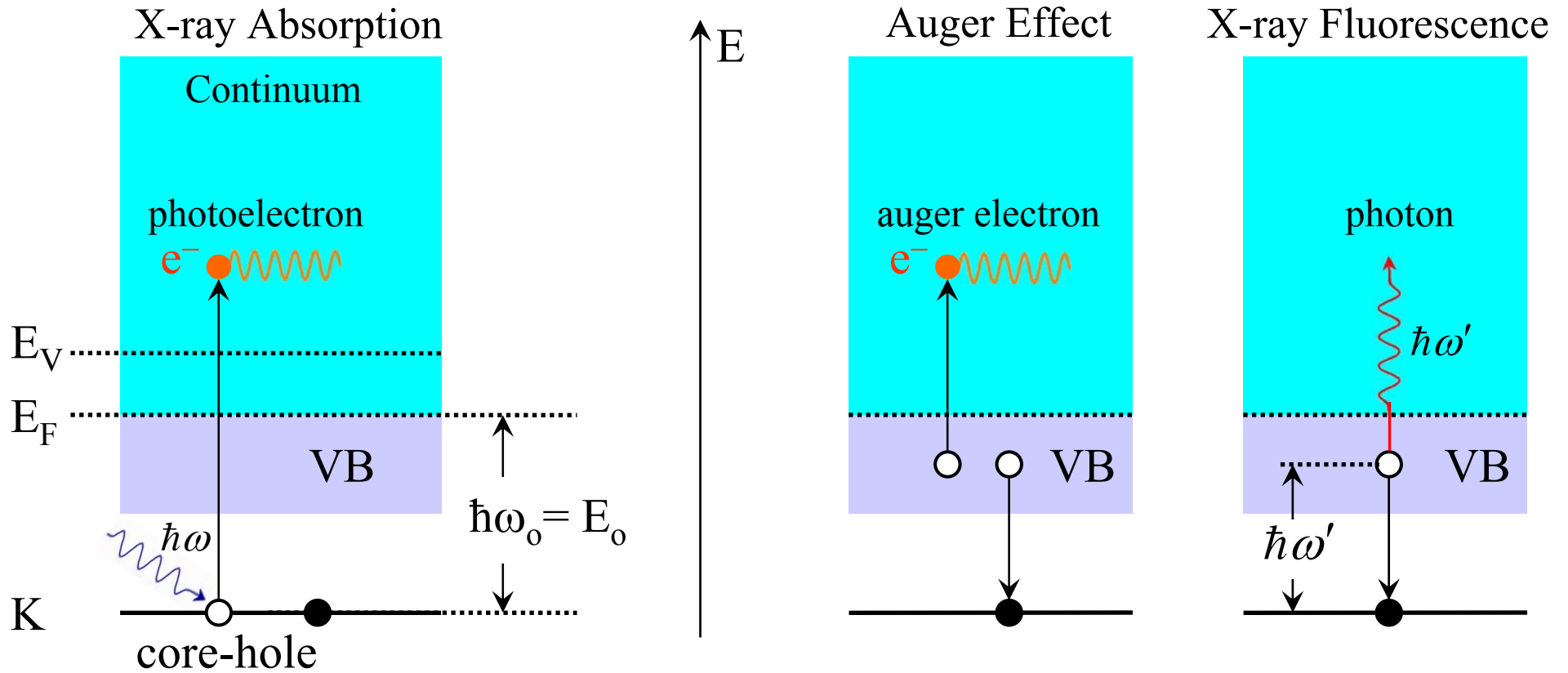
E_0 – Carbon K - edge (CK - edge)

$E_0 \approx 285$ eV

E_d – Divide between NEXAFS and EXAFS

$E_d \sim 320$ eV

Important Details of X-ray Absorption Process



E_0 - energy of absorption K -edge

τ_h, τ_a, τ_f - total and partials core-hole lifetimes

if $Z \leq 8$ then $\tau_a \sim 10^{-15} \text{ s} \gg \tau_f \sim 10^{-13} \text{ s} \Rightarrow \frac{1}{\tau_h} = \frac{1}{\tau_a} + \frac{1}{\tau_f} \cong \frac{1}{\tau_a} \sim 10^{-15} \text{ s}$

II. Theoretical Background and a Little of History

$$\chi(k) = S_o^2 \cdot \sum_j \frac{N_j \cdot f_j(k) \cdot e^{-2\sigma_j^2 k^2} \cdot e^{-2R_j/\lambda(k)}}{kR_j^2} \sin(2kR_j + \delta_j(k))$$

X-ray Absorption Cross-Section

$$\mu(\hbar\omega) = \sigma_x(\hbar\omega) \cdot n_a$$

σ_x – x-ray absorption cross-section [cm^2], n_a – atomic density [$\text{atoms} \cdot \text{cm}^{-3}$]

$$\sigma_x [\text{nm}^2] = \frac{\text{number of absorbed photons } [\text{s}^{-1}]}{\text{photon flux } [\text{nm}^{-2} \cdot \text{s}^{-1}]}$$

Fermi's Golden Rule $\Rightarrow \sigma_x(\hbar\omega) \propto \sum_f \left| \langle \Psi_f | (\mathbf{r} \cdot \mathbf{E}) | \Psi_i \rangle \right|^2 \cdot \delta(E_f - E_i - \hbar\omega)$

Ψ_i – initial wave function

localized state with
radius $\sim a_B/Z$

Ψ_f – final wave function

delocalized state with
wave number k
and wave length λ

$$\lambda = \frac{2\pi}{k} = \frac{2\pi}{\sqrt{\hbar\omega - E_o}}$$

$(\mathbf{r} \cdot \mathbf{E})$ – dipole transition operator

\mathbf{E} – electric field vector

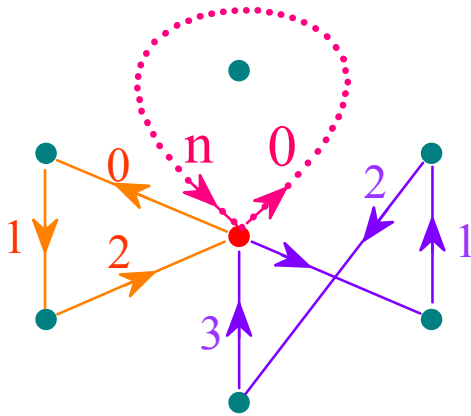
for K -edges of C, O, N, F
the only possible transition $1s \rightarrow 2p$

The Roots of Difference between NEXAFS and EXAFS

NEXAFS

(multiple strong scattering regime)

$$\Psi_f \cong \Psi_f^{(0)} + \Psi_f^{(1)} + \Psi_f^{(2)} + \dots + \Psi_f^{(n)}, n \gg 1$$



small $k \rightarrow$ large $f(k)$

$$\mu(E) \propto \rho(l, E)$$

NEXAFS - reflection of l - projected density of unoccupied states $\rho(l, E)$

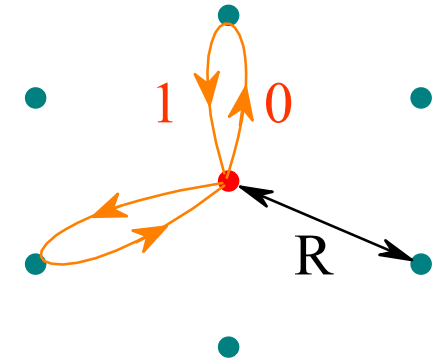
$$\mu(k) \propto \left| \langle \Psi_f | (\mathbf{r} \cdot \mathbf{E}) | \Psi_i \rangle \right|^2$$

$f(k, \theta)$ -
elastic
scattering
amplitude

EXAFS

(single weak scattering regime)

$$\Psi_f \cong \Psi_f^{(0)} + \Psi_f^{(1)}$$

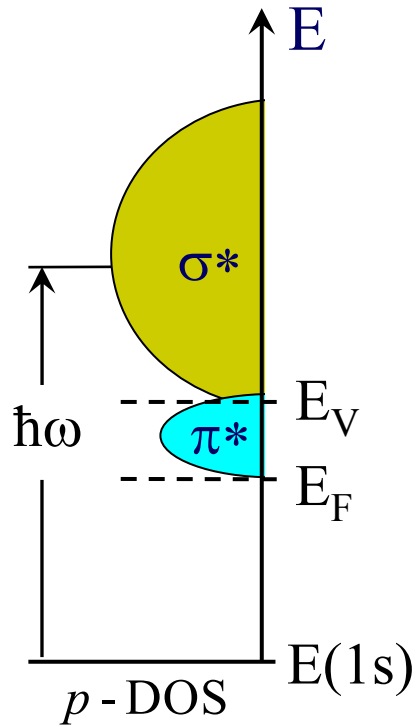


large $k \rightarrow$ small $f(k)$

$$\mu(k) \sim f(k) \cdot \sin(2kR)$$

EXAFS - reflection of interference pattern traced along photoelectron wave number scale

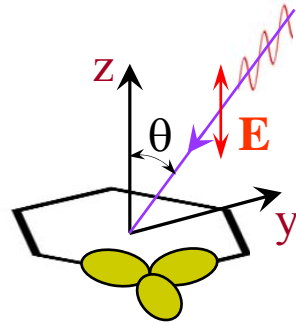
NEXAFS Dependence on X-Ray Polarization



$$(\mathbf{r} \cdot \mathbf{E})$$

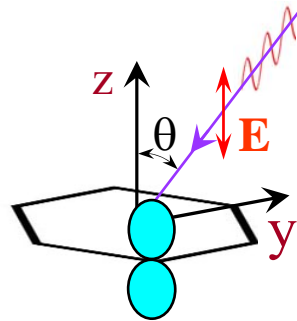


$$\mu(E) \rightarrow \mu(\theta, E)$$



in-plane σ^* - orbitals

$$|\langle \sigma^* | \mathbf{r} \cdot \mathbf{E} | s \rangle|^2 \sim \cos^2 \theta$$

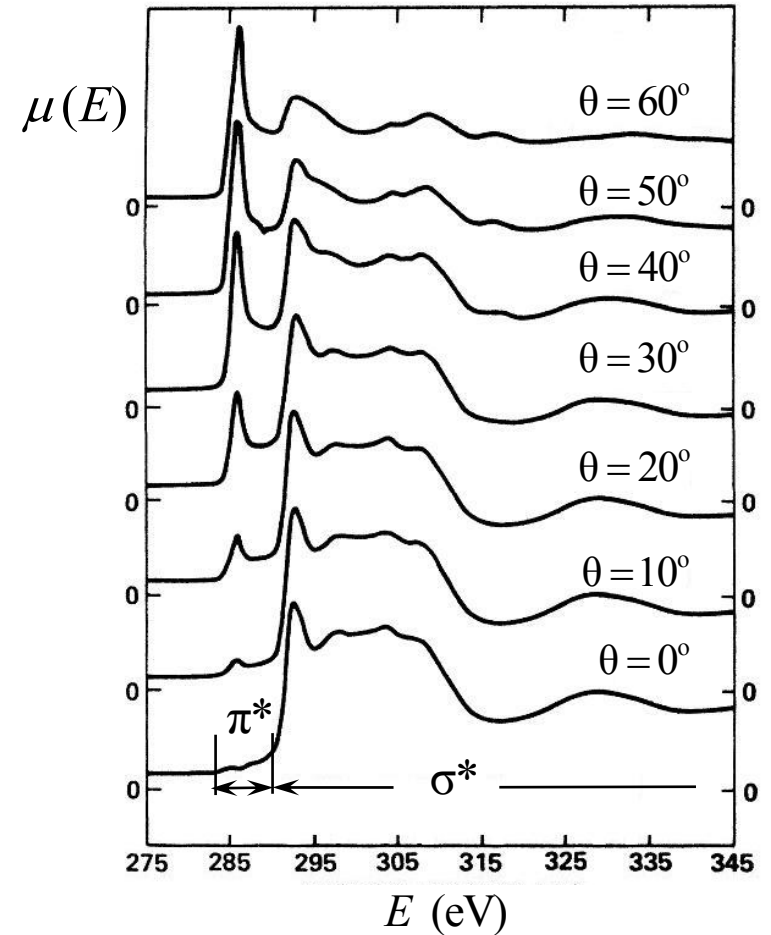


out-of-plane π^* - orbitals

$$|\langle \pi^* | \mathbf{r} \cdot \mathbf{E} | s \rangle|^2 \sim \sin^2 \theta$$

$$\mu(\theta, E) \sim \rho_{\pi}(E) \cdot \sin^2 \theta + \rho_{\sigma}(E) \cdot \cos^2 \theta$$

CK-edge XAS of HOPG



the figure reproduced from
R.A. Rosenberg et al..
Phys. Rev. B **33**, 4034 (1986).

Main features of CK-edge NEXAFS

1. π^* - resonances (exciton-like) : $E_F < E_{\pi^*} < E_V$

$$E_V = E_F + e\phi$$

for HOPG: $E_V = E_F + 4.7 \text{ eV}$

2. σ_{ex}^* - core hole (Frenkel) excitons:

$$E_V + 1 \text{ eV} < E_{ex} < E_V + 3 \text{ eV}$$

for HOPG: $E_{ex} = 291.65 \text{ eV}$

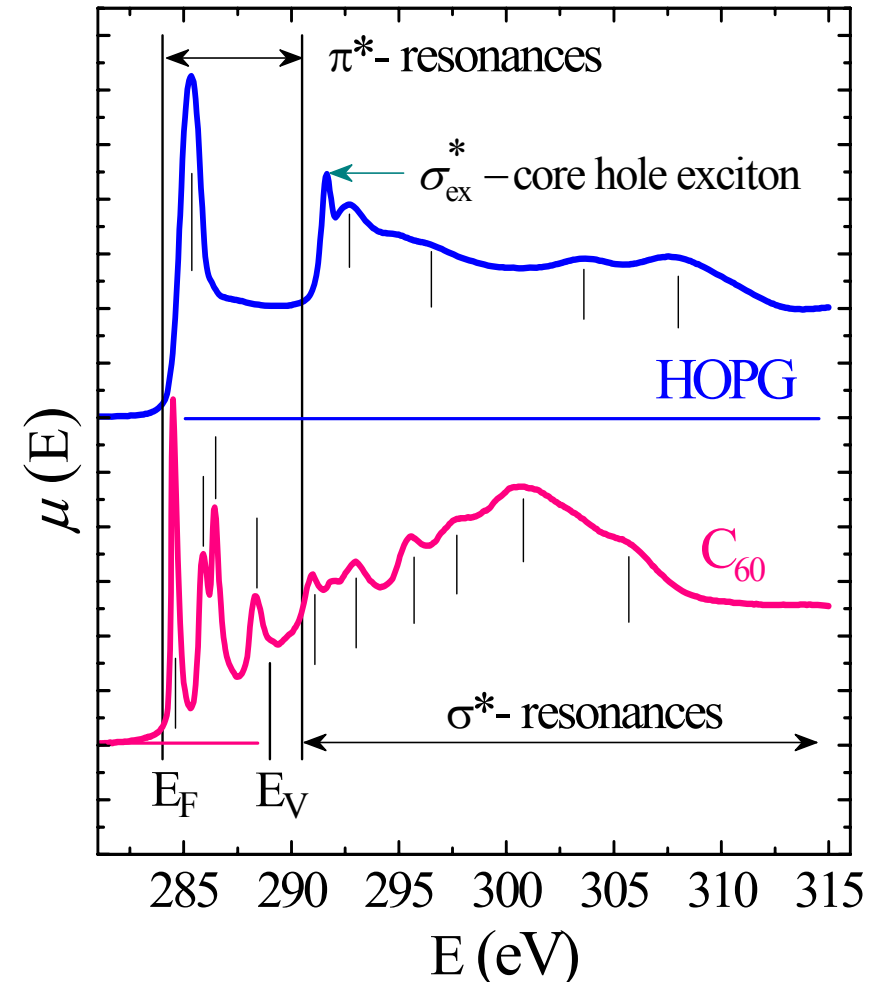
3. σ^* - resonances : $E_V + 3 \text{ eV} < E_{\sigma^*} < E_{EXAFS}$

E_{EXAFS} - lower boundary of EXAFS regime

for HOPG: $E_{EXAFS} \approx E_F + 30 \text{ eV}$

NEXAFS reflects: x-ray polarization dependent, core hole-perturbed partial density of unoccupied states (p-DOS) localized within a few atomic sites from the excited atom ($R \sim 5$ angstroms) [*].

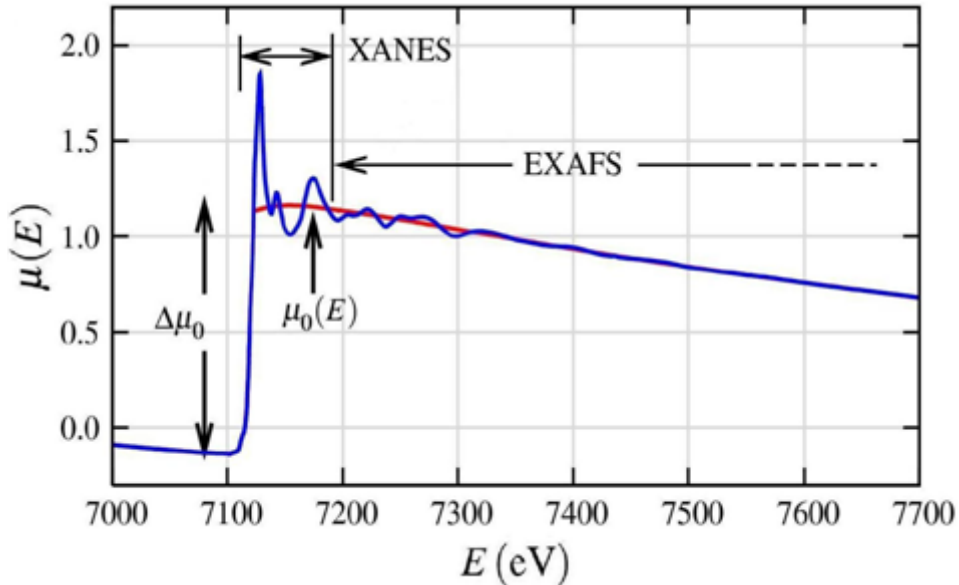
CK-edge XAS of HOPG



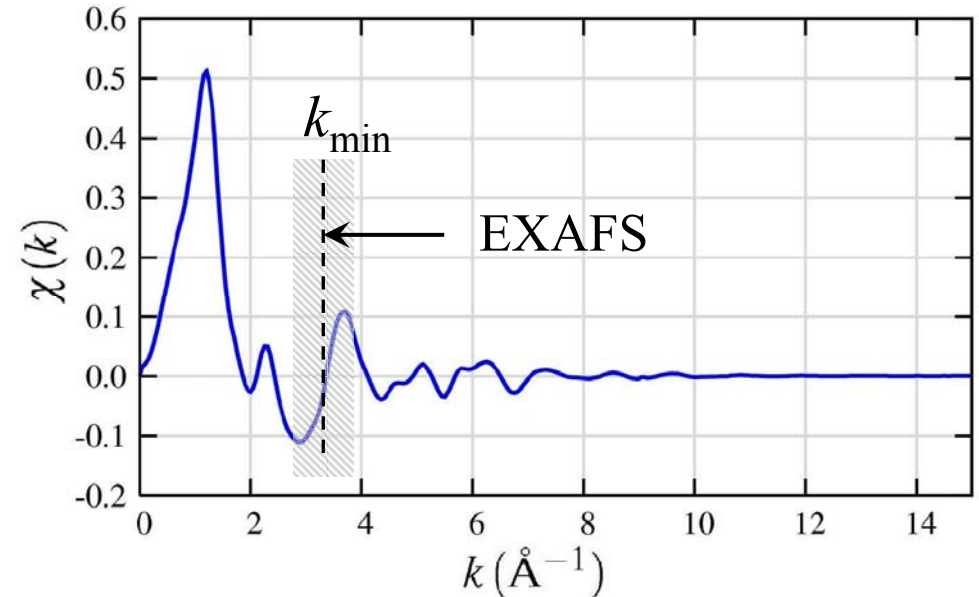
[*] J. Schiessling et al., J. Phys.: Condens. Matter **15**, 6563 (2003).

Isolation of the Fine-Structure Oscillations $\chi(k)$

XAFS $\mu_o(E)$ for FeO [*]



Isolated XAFS $\chi(k)$ for FeO [*]



$$\chi(E) = \frac{\mu(E) - \mu_o(E)}{\Delta\mu} \quad \longrightarrow \quad k = \sqrt{\frac{2m(E - E_o)}{\hbar^2}} \quad \longrightarrow \quad \chi(k) = \frac{\mu(k) - \mu_o(k)}{\Delta\mu}$$

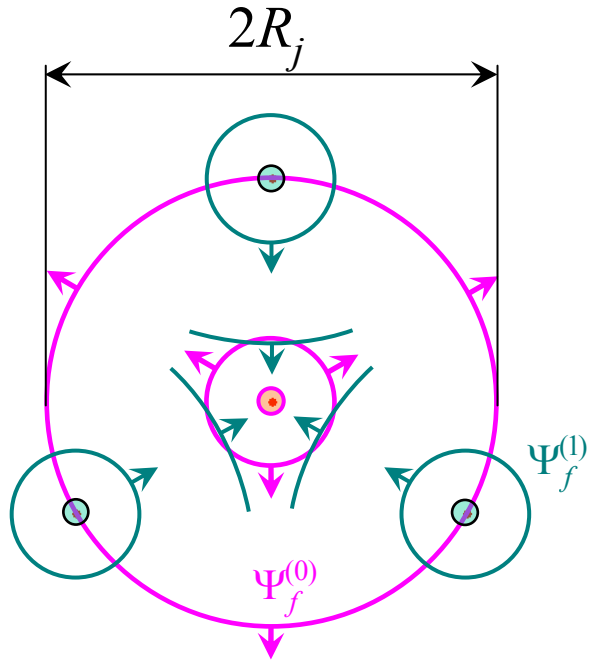
$\mu_o(E)$ - absorption in the absence of neighboring scatterers (atomic-like background)

k_m - lower EXAFS boundary

$$|\chi(k < k_{\min})| \gg |\chi(k > k_{\min})|$$

[*] M. Newville. Fundamentals of XAFS. University of Chicago, 2004.

EXAFS as a Quantum Interference Phenomenon



$$\Psi_f = \Psi_f^{(0)} + \Psi_f^{(1)}$$

$\Psi_f^{(0)}$ – outgoing wave, $\Psi_f^{(1)}$ – backscattered wave

$$\Psi_f^{(0)} \propto \frac{e^{ikr}}{r}, \quad \Psi_f^{(1)} \propto f(k, \pi) \frac{e^{i(kr+2\delta(k))}}{r}$$

$f(k, \pi)$ – backscattering amplitude

$\delta(k)$ – phase shift

$$\chi(k) \propto \left[\overbrace{\langle \Psi_f | (\mathbf{r} \cdot \mathbf{E}) | \Psi_i \rangle}^{\mu(k)} \right]^2 - \left[\overbrace{\langle \Psi_f^{(0)} | (\mathbf{r} \cdot \mathbf{E}) | \Psi_i \rangle}^{\mu_0(k)} \right]^2$$

Single Scattering Model



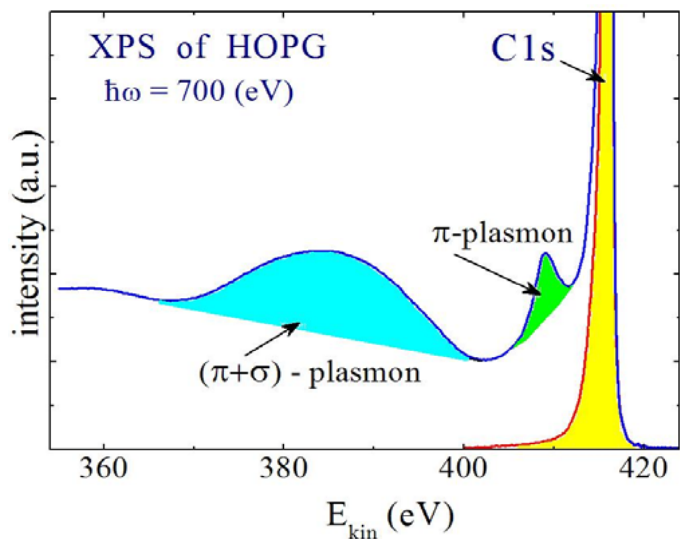
$$\chi(k) = \sum_j \frac{N_j \cdot f_j(k)}{kR_j^2} \cdot \sin(2kR_j + \delta_j(k))$$

where N_j, R_j are coordination number and average distance to atoms in shell j

$$k_{\min} = \frac{2\pi}{R} - \text{lower EXAFS boundary}$$

if $R = 1.42 \text{ \AA}$ then $k_d \cong 4.5 \text{ \AA}^{-1}$

Taking into Account Many-body Effects



Intrinsic Losses $\rightarrow S_o^2$

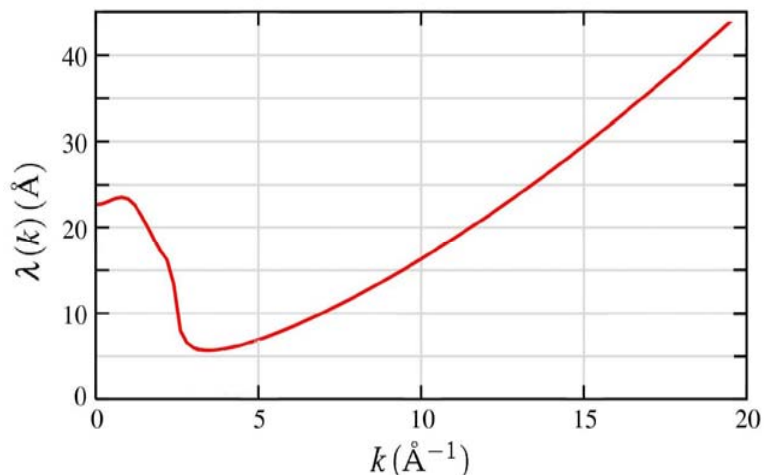
(shake-up and shake-off processes)

S_o^2 – amplitude reduction factor;

Structural and Temperature Disorder $\rightarrow e^{-2\sigma_j^2 k^2}$

$e^{-2\sigma_j^2 k^2}$ – Debye-Waller factor

σ_j^2 – mean square displacement of shell j atoms



Extrinsic Losses $\rightarrow e^{-2R_j/\lambda(k)}$

$\lambda(k)$ – photoelectron mean free path determined by inelastic scatterings and finite core-hole lifetime



$$\chi(k) = S_o^2 \cdot \sum_j \frac{N_j \cdot f_j(k) \cdot e^{-2\sigma_j^2 k^2} \cdot e^{-2R_j/\lambda(k)}}{kR_j^2} \sin(2kR_j + \delta_j(k))$$

The figure reproduced from M. Newville.
 Fundamentals of XAFS. University of Chicago, 2004.

Extraction of Structural Parameters from $\chi(k)$ - function

Radial structure function $F(R)$ can be obtained using Fourier transformation of $k\chi(k)$ [*]:

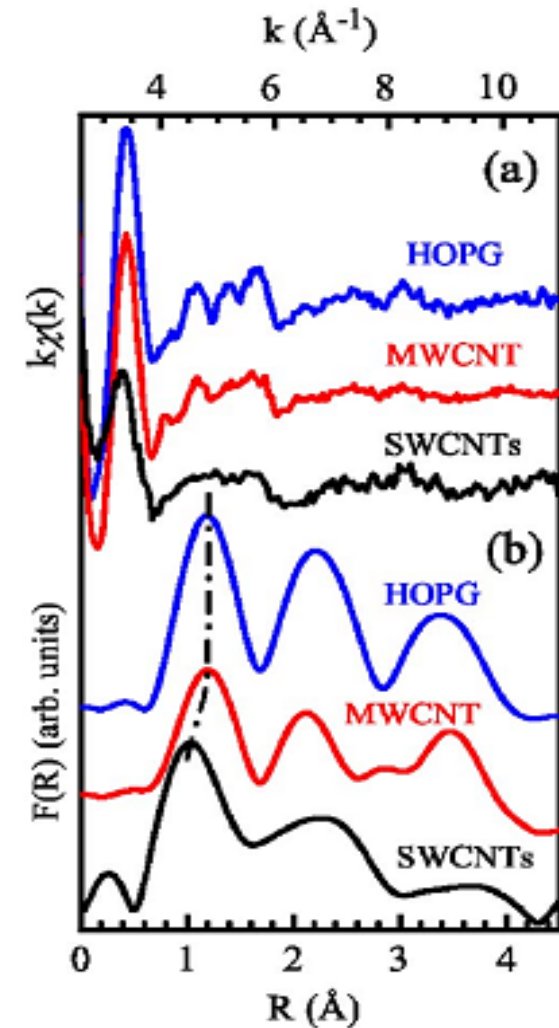
$$F(R) = \int_{k_{\min}}^{k_{\max}} dk (k\chi(k)) \cdot \sin(2kR)$$

k_{\min} and k_{\max} are determined, respectively, by lower EXAFS boundary and by acceptable value of signal/noise ratio

for carbon materials:

$$k_{\min} \approx 4 \text{ \AA}^{-1} \quad \text{and} \quad k_{\max} \approx 11 \div 12 \text{ \AA}^{-1}$$

FEFFx (FEFF6 \rightarrow FEFF8)



[*]- D. E. Sayers,, E. A. Stern, and F. W. Lytle,
Phys. Rev. Lett. **27**, 1204 (1971).

The figures reproduced from P. Castrucci et al.
Phys. Rev. B **75**, 035420 (2007).

The Key Points of NEXAFS/EXAFS History

Discovery of X-Rays - Röntgen (1895)

First measurements of absorption edge – Maurice de Broglie (1913)

The first observation of the fine structure – Fricke (K-edges) (1920), Hertz (L-edges) (1920)

The first theory of NEXAFS (“Kossel structure”) and EXAFS (“Kronig Structure”) –
Kossel (1920), R. Kronig (1931)

Improvement of theoretical models and experimental facilities (1930s – 1960s)

Creation of valid short-range-order theory of EXAFS – D. Sayers, E. Stern, F. Lytle (1968-1971)

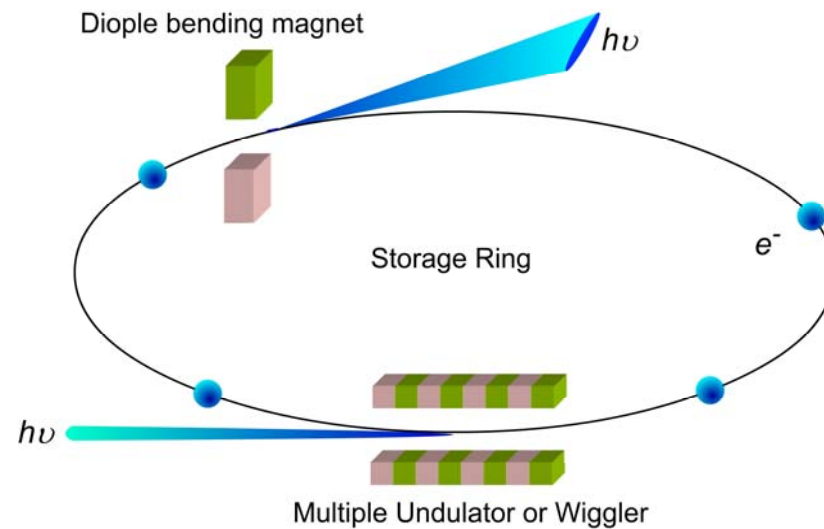
Appearance of the name EXAFS - F. Lytle, J. Prins (1968)

The dawn of “Synchrotron Era” – (1970s)

Appearance of the names XANES/NEXAFS - A. Bianconi (1980)/J. Stöhr(1982)

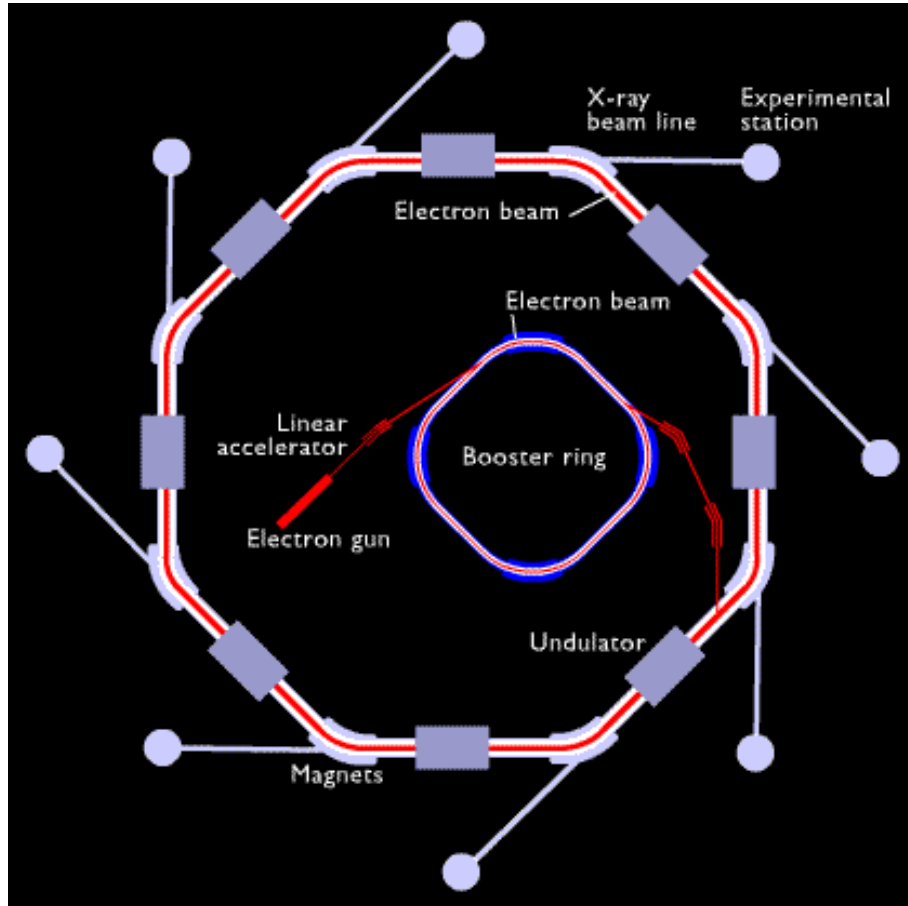
Development of highly quantitative multiple-scattering theories of XAFS – (1980s - present time)

III. Some Aspects of Modern XAFS Experiments and XAFS Data Processing Technique



Storage Ring as a X-ray Source

Storage Ring Scheme



The figure taken from site:
[http://www.odec.ca/projects/2005/shar5a0/public_html/images /model_animated.gif](http://www.odec.ca/projects/2005/shar5a0/public_html/images/model_animated.gif)

Synchrotron's Characteristics:

Electron beam energy : E_e [GeV]

Current: i_e [mA]

Circumference: L [m]

Pulse duration (FWHM): τ (ps)

Bending Magnet Field : B [T]

Critical Photon Energy : E_C [keV]

Total Photon Flux: F [photons/s]

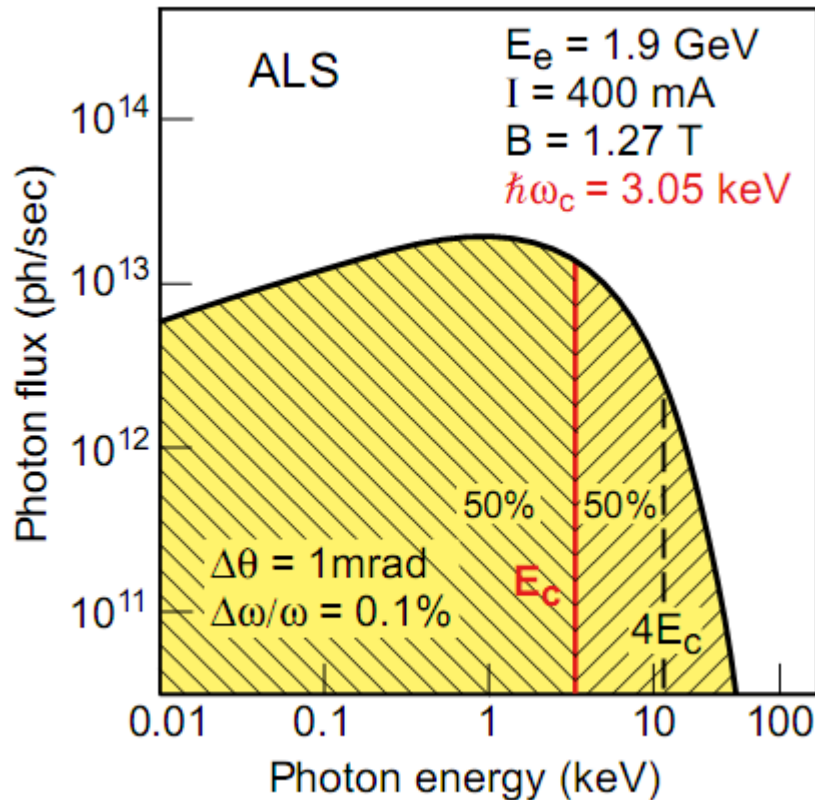
$$L = 2\pi R$$

$$E_C = \hbar\omega_C = 0.665 \cdot E_e^2 \cdot B$$

$$F \cong 1.3 \cdot 10^{17} \cdot i_e \cdot E_e$$

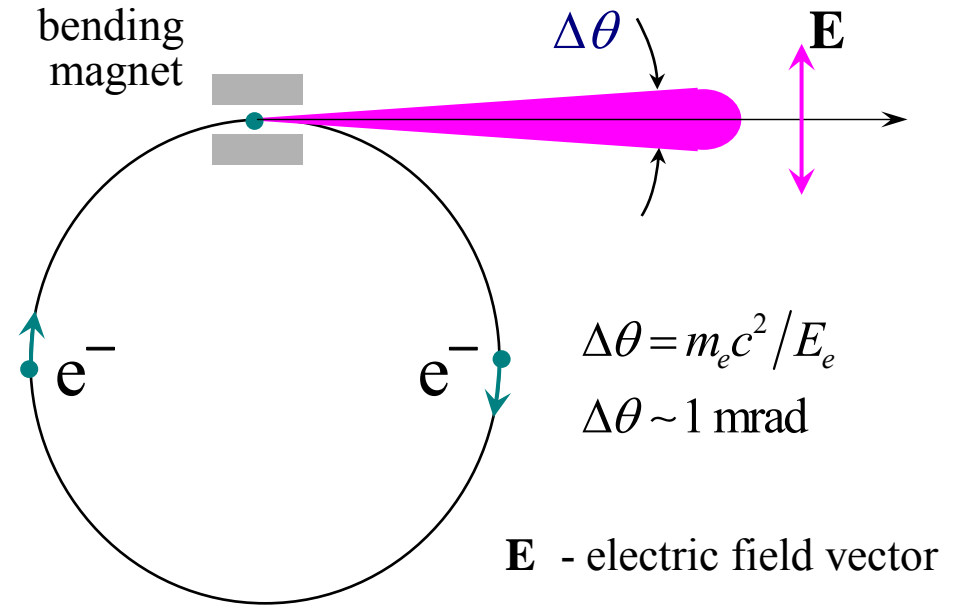
Main Characteristic of Synchrotron Radiation

Advanced Light Source (ALS).
Berkeley. USA



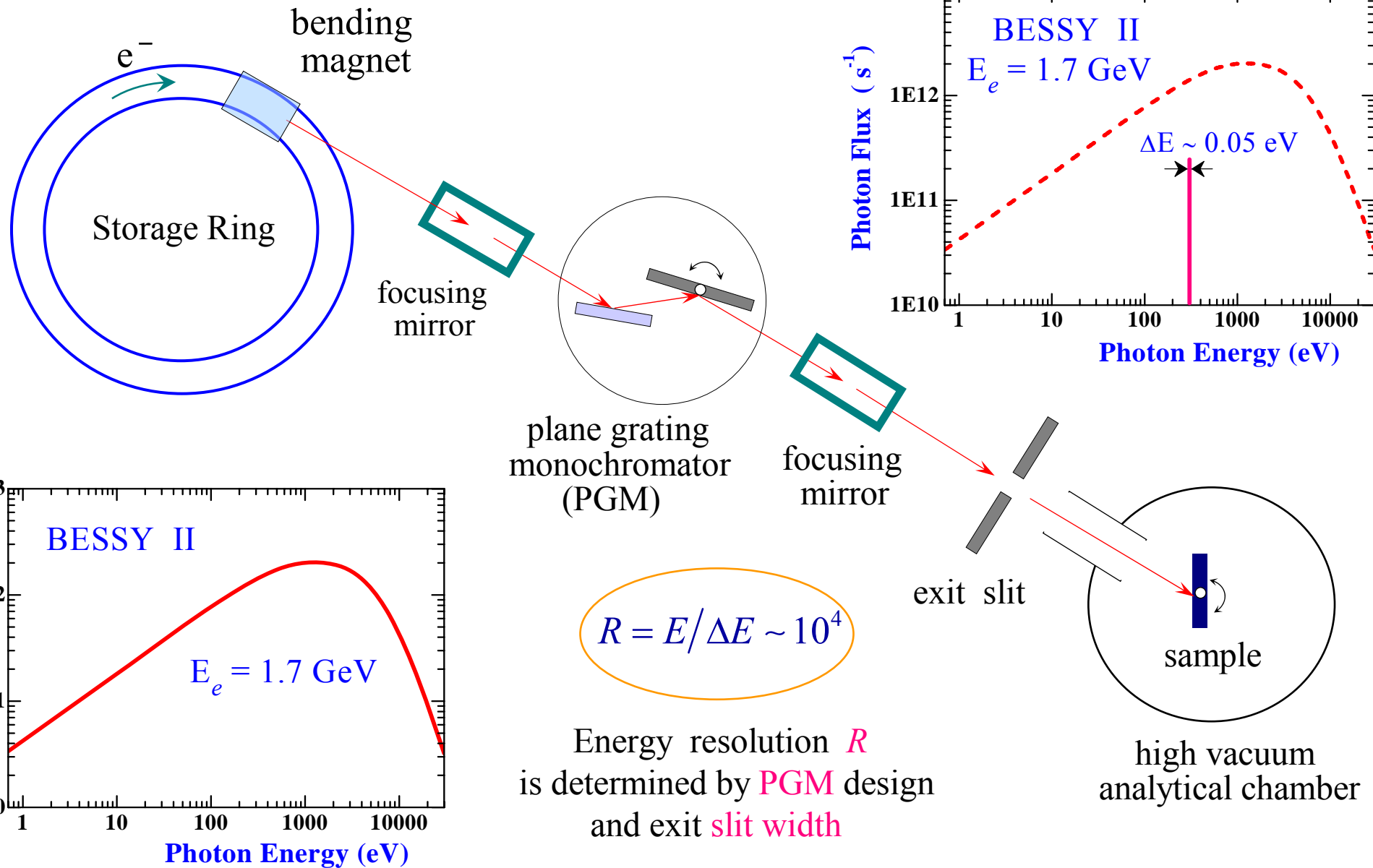
The figure taken from prof. D. Attwood lecture
 "Intro to Synchrotron Radiation" EE290F, 16 Jan 2007.
 Berkeley. USA.

Dipole Synchrotron Radiation (SR)



1. linear polarization of \mathbf{E} (in the plane of e^- orbit)
2. extremely high brightness ($\sim 10^{10}$ brighter than the most powerful laboratory source)

Monochromatization of Synchrotron Radiation

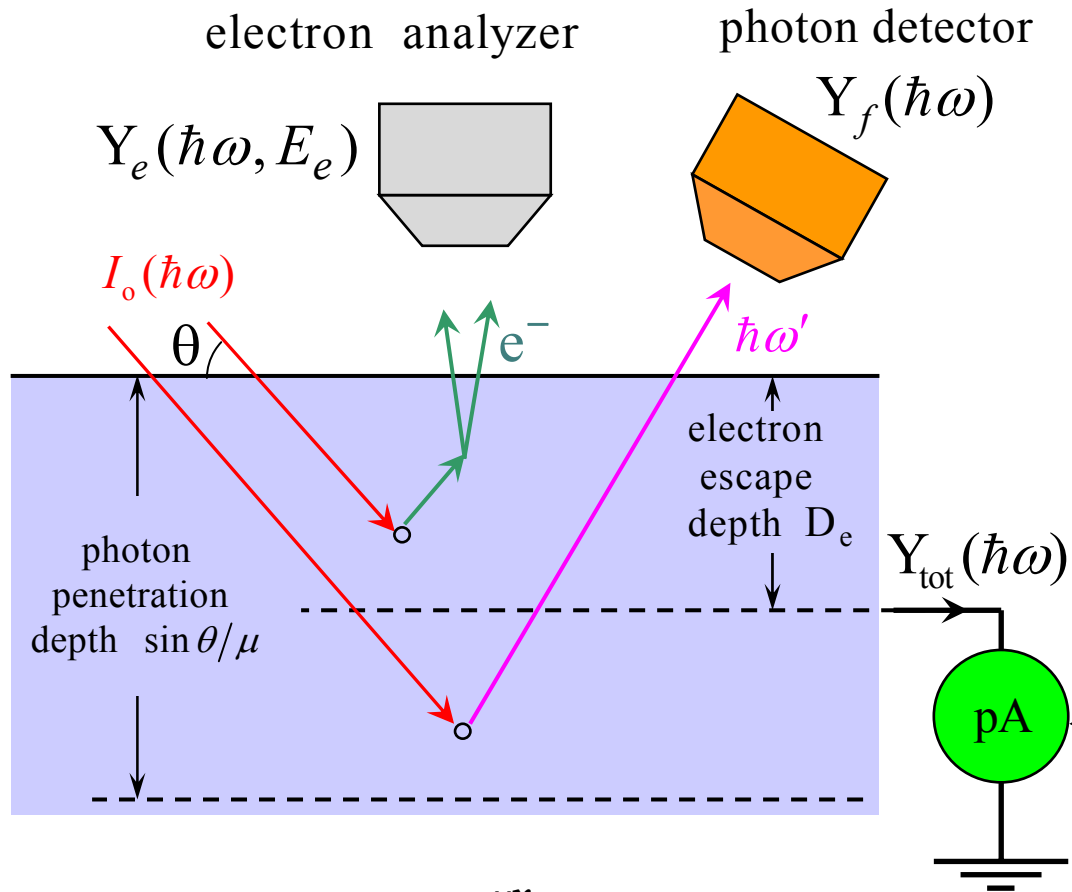


Typical Parameters of Third Generation Synchrotrons

Facility	ALS	BESSY II	ESRF	SPring-8
Country	USA	Germany	France	Japan
Electron energy	1.90 GeV	1.70 GeV	6.04 GeV	8.00 GeV
Current (mA)	400	200	300	100
Circumference (m)	197	240	884	1440
RF frequency (MHz)	500	500	352	509
Pulse duration (FWHM) (ps)	35-70	20-50	70	120
Bending magnet field (T)	1.27	1.30	0.806	0.679
Critical photon energy (keV)	3.05	2.50	19.6	28.9
Bending magnet sources	24	32	32	23

The Table taken from prof. D. Attwood lecture "Intro to Synchrotron Radiation" EE290F, 16 Jan 2007. Berkeley. USA.

Recording of the XAS in the Reflection Mode



$$I = I_0 e^{-\mu x}$$

$$\mu D_e / \sin\theta \ll 1 \Rightarrow I_{\text{abs}} = I - I_0 \propto \mu \cdot I_0$$

$$\underline{I_{\text{abs}}(\hbar\omega) \propto Y_e(\hbar\omega) \propto Y_f(\hbar\omega)}$$

$Y_f(\hbar\omega)$ – fluorescence yield (FY)

$Y_e(\hbar\omega)$ – electron yield (EY)

$$D_e \ll D_f \sim 1/\mu(\hbar\omega')$$

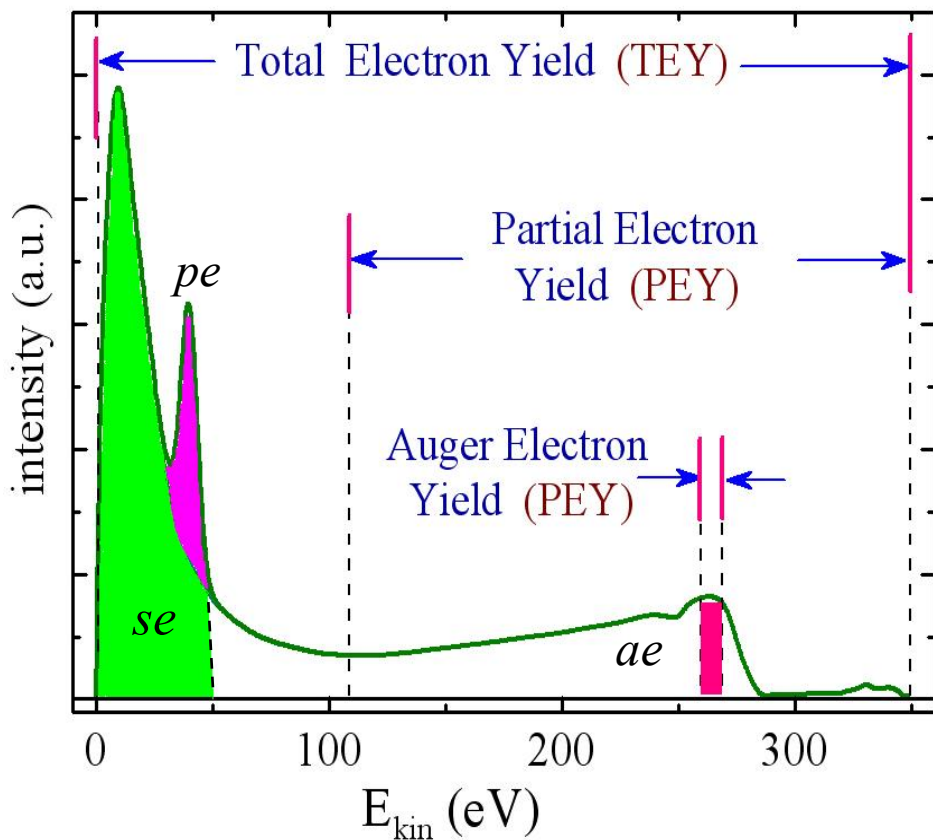
$$\text{if } Z \leq 16 \quad Y_f(\hbar\omega) \ll Y_e(\hbar\omega)$$

$$Y_{\text{tot}}(\hbar\omega) = Y_e(\hbar\omega, 0 \leq E_e \leq \hbar\omega - e\varphi)$$

TEY - Total **Electron** Yield

TFY - Total **Fluorescence** Yield

Peculiarities of Different Electron Yield Techniques



se, pe, ae – secondary, photo and auger electrons.

$$Y_{tot} = Y_{se} + Y_{ae} + Y_{pe} \gg Y_{ae} + Y_{pe}$$

e^- escape depth $D_e = \text{XAS information depth}$

1. TEY: $\mu(\hbar\omega) \propto Y_{tot}(\hbar\omega)/I_0 \rightarrow D_e \approx 50 \text{ \AA}$
2. PEY: $\mu(\hbar\omega) \propto Y_{part}(\hbar\omega)/I_0 \rightarrow 10 \text{ \AA} \leq D_e \leq 50 \text{ \AA}$
3. AEY: $\mu(\hbar\omega) \propto Y_{ae}(\hbar\omega)/I_0 \rightarrow D_e \sim 10 \text{ \AA}$



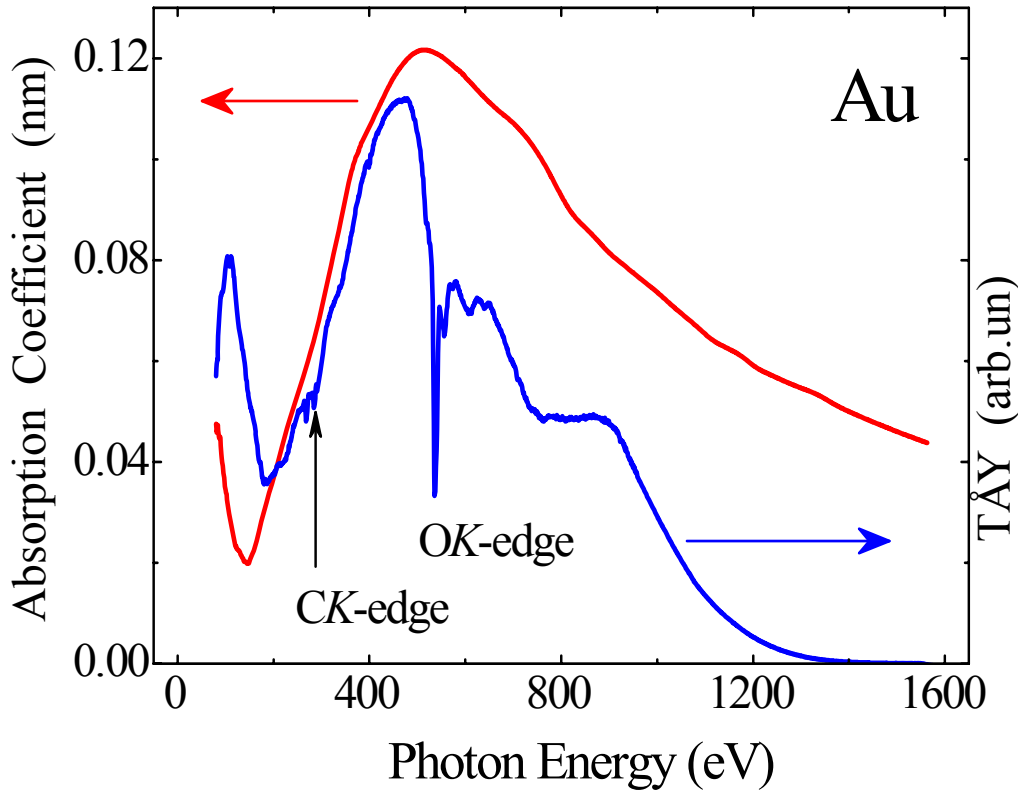
Choice of **XAS** recording mode determines **its information depth**

TEY - Surface + Bulk

TFY - Bulk

Normalization and Background Correction of the XAS

BESSY II, Russian-German Beam Line



$$I_o(\hbar\omega) \neq \text{const}$$

Measured electron yield $Y_e(\hbar\omega)$ must be corrected for beam line transmission function $T(\hbar\omega)$

$$\mu(\hbar\omega, \text{Au}) = T(\hbar\omega) \cdot Y_e(\hbar\omega, \text{Au})$$

$$T(\hbar\omega) = \frac{\mu(\hbar\omega, \text{Au})}{Y_e(\hbar\omega, \text{Au})}$$

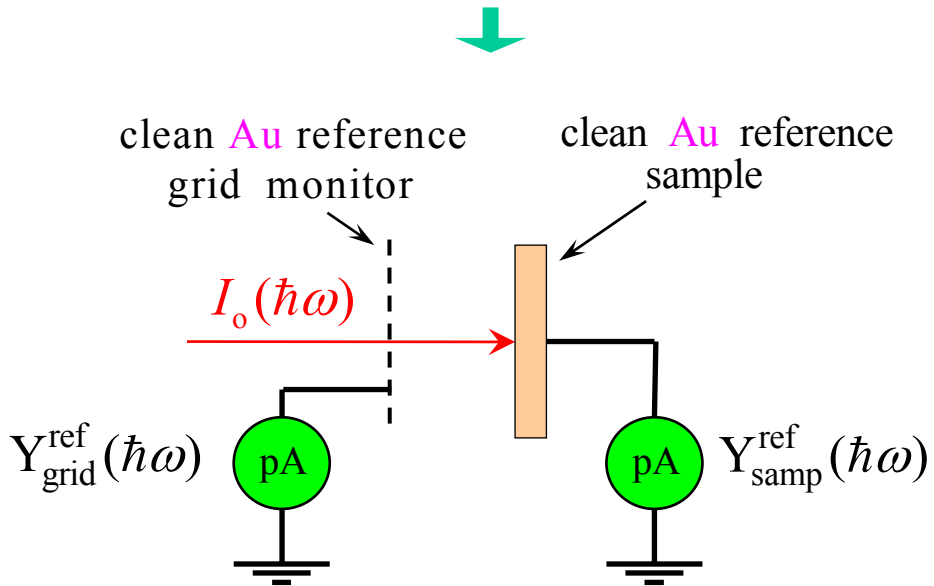
for CK-edge NEXAFS

$$\mu(\hbar\omega, \text{Au}) \approx \text{const}$$

$$\mu(\hbar\omega, X) = \frac{Y_e(\hbar\omega, X)}{Y_e(\hbar\omega, \text{Au})}$$

Normalization and Background Correction of the XAS

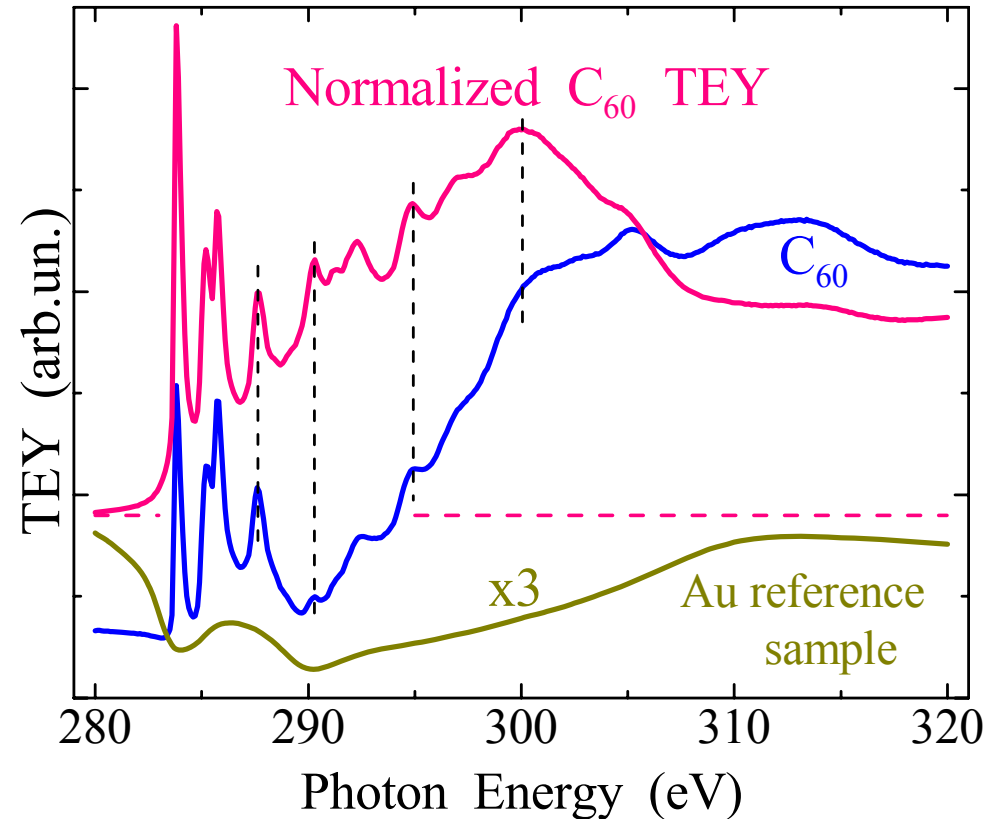
Normalization requires reference monitor



$Y_{\text{samp}}^{\text{ref}}(\hbar\omega)$ – more simple and controllable

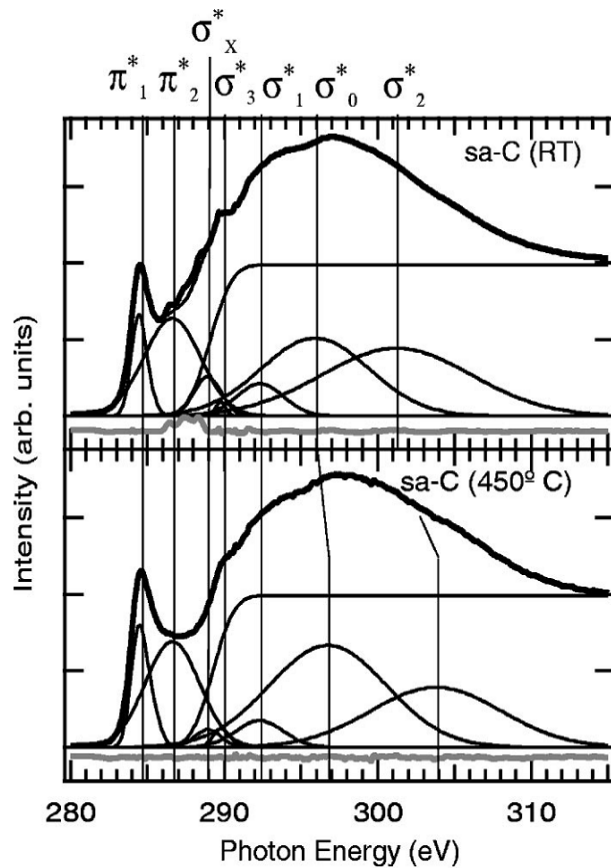
$Y_{\text{grid}}^{\text{ref}}(\hbar\omega)$ – accounts for photon flux instabilities

BESSY II, Russian-German Beam Line (RGBL)



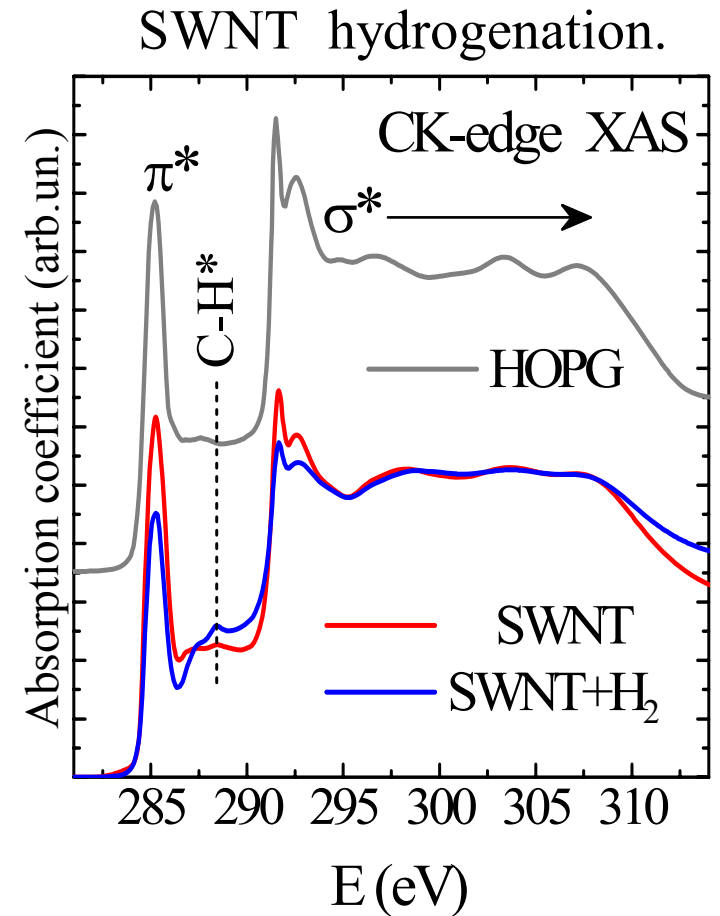
Normalization TEY of C_{60} film using clean Au reference sample

Analysis and Interpretation of NEXAFS Spectra



Complicated Way
decomposition into set of steps and peaks, theoretical modeling, etc... [*]

Simplified Way
direct comparison with properly normalized reference spectra

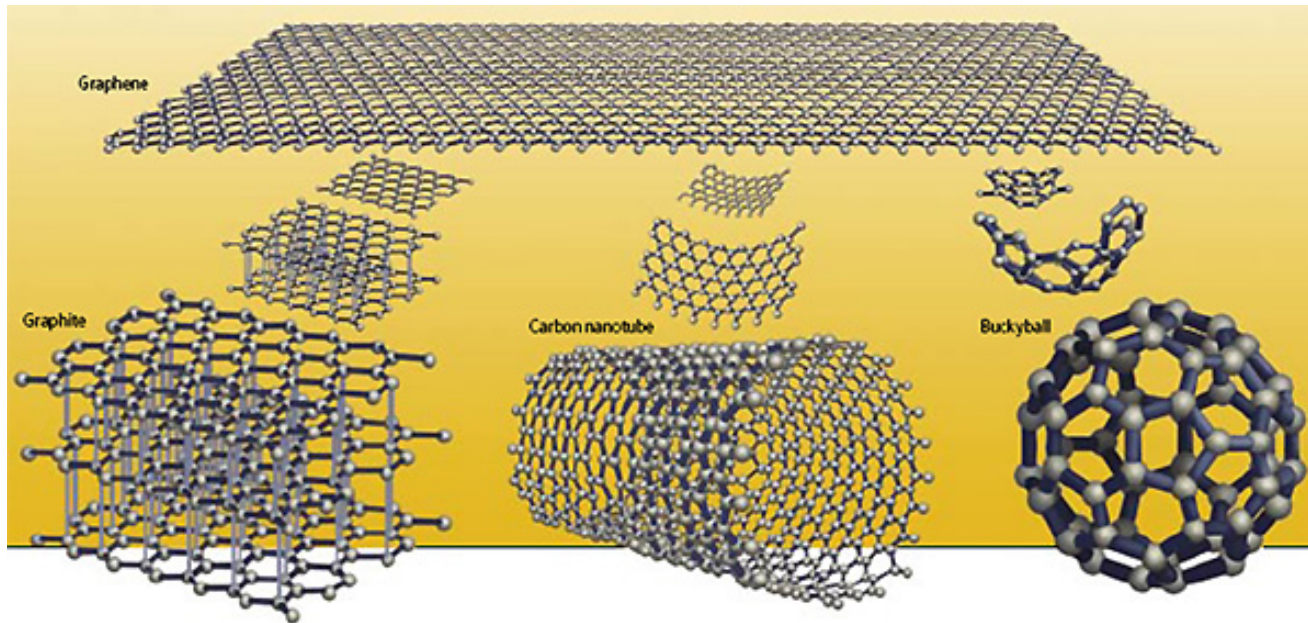


$$\frac{\pi^*(\text{SWNT} + \text{H}_2)}{\pi^*(\text{SWNT})} = 0.72 \pm 0.07$$

The figure reproduced from J. Diaz, S. Anders, X. Zhou et al. Phys. Rev. B **64**, 125204 (2001).

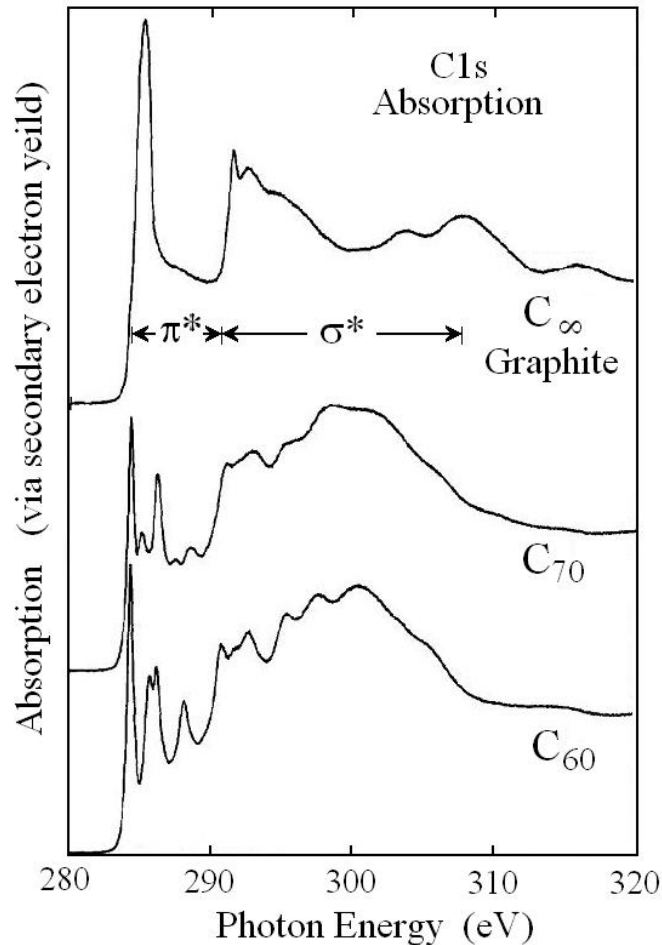
[*] For details see references [1-4] from Main Sources.

IV. The information that can be obtained by
NEXAS/EXAFS Spectroscopy.
Some Nanocarbons Related Examples



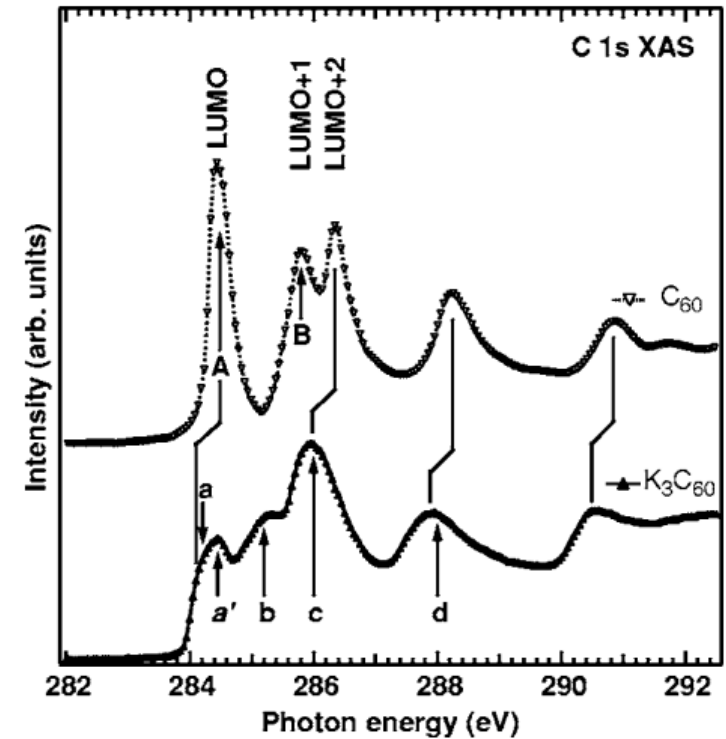
NEXAFS of Fullerites and Fullerides

XAS of C_{60} and C_{60} films [*]



narrow π^* and σ^* resonances show that solid C_{60} and C_{70} are the molecular crystals

XAS of crystalline K_3C_{60} [**]



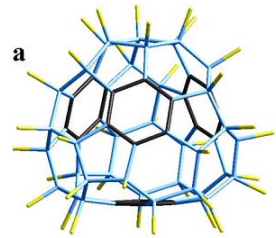
1. half-filled LUMO (a') in K_3C_{60} .
2. large general shift (~ 0.35 eV) of K_3C_{60} LUMOs

[*] L.J. Termenello et al. Chem. Phys. Letters, **182**, 491 (1991).

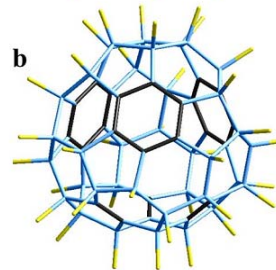
[**] T. Kaambre et al. Phys. Rev. B **75**, e195432 (2007).

Experimental and Theoretical study NEXAFS of $C_{60}F_{36}$ [*]

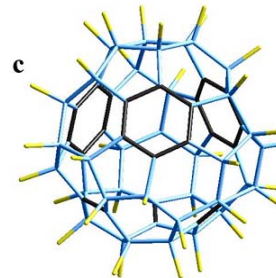
The structure of $C_{60}F_{36}$ isomers



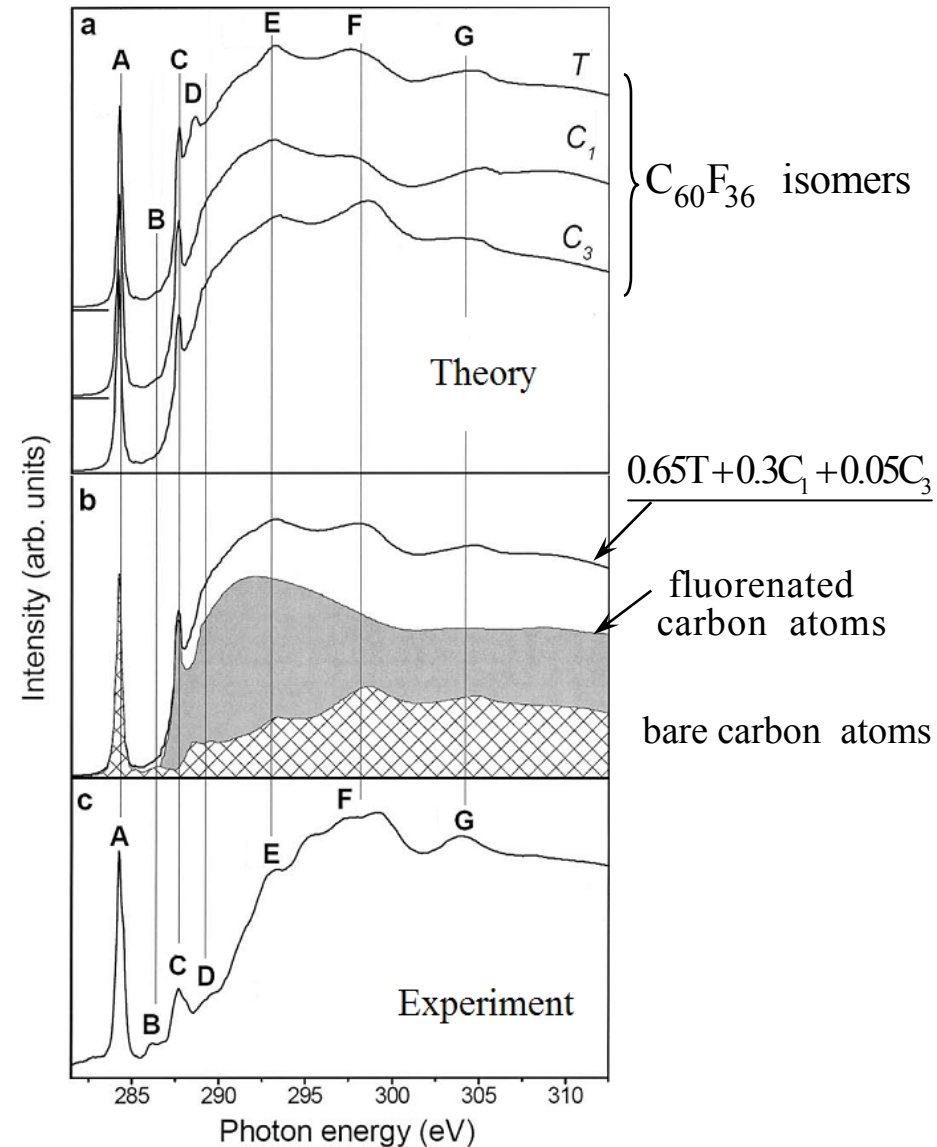
T-symmetry (65%)



C_1 -symmetry (30%)

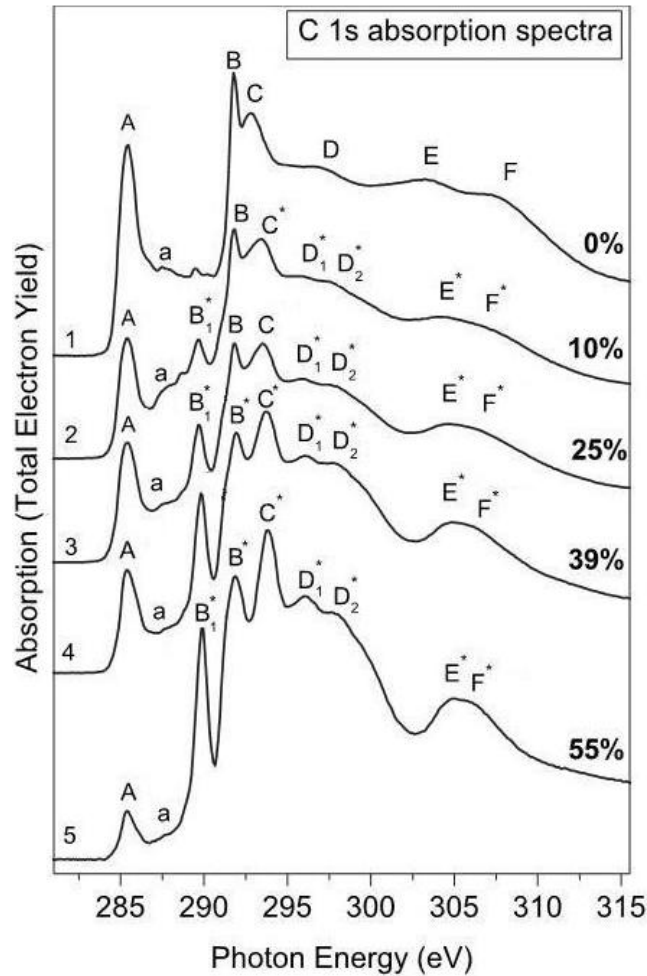


C_3 -symmetry (5%)



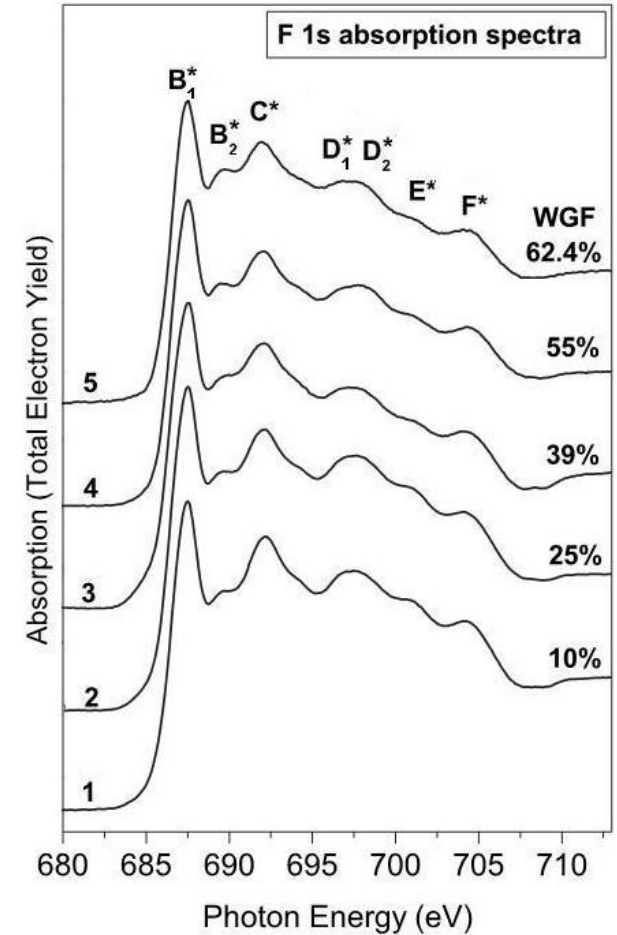
[*] L.G. Bulusheva, A.V. Okotrub, V.V. Shnitov, V. V. Bryzgalov et al.
J. Chem. Phys. **130**, 014704 (2009).

NEXAFS of fluorinated MWCNT [*]



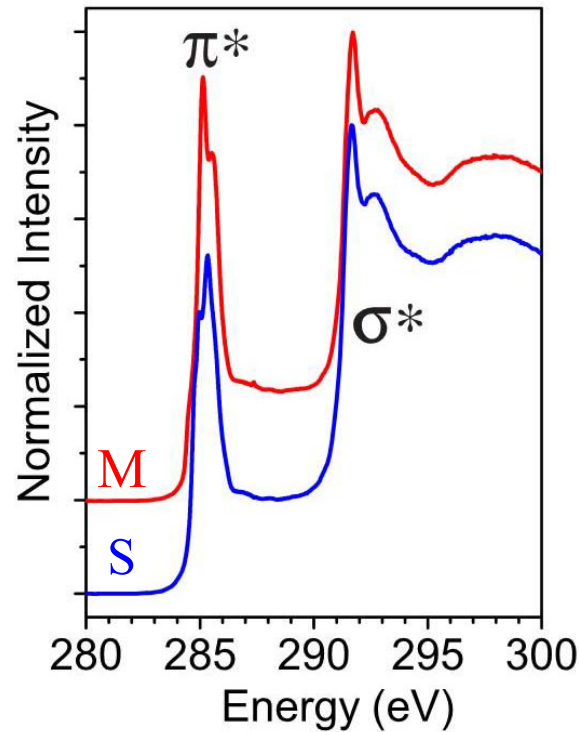
Fluorination dramatically changes MWNT CK-edge, but does not affect their FK-edge

Fluorination "kills"
 π^* - resonances
 \downarrow
 $sp^2 \rightarrow sp^3$

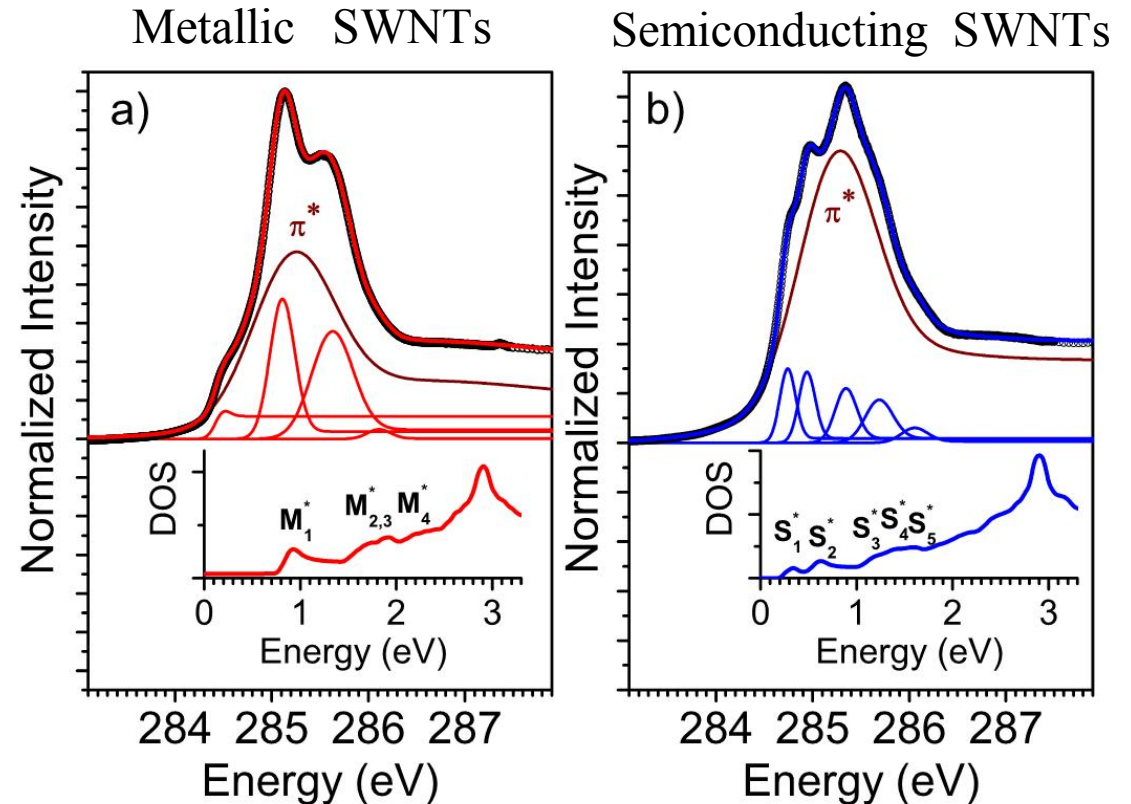


[*] M. M. Brzhezinskaya et al. Phys. Rev. B **79**, 155439 (2009).

Study of metallicity-sorted SWCNT [*]



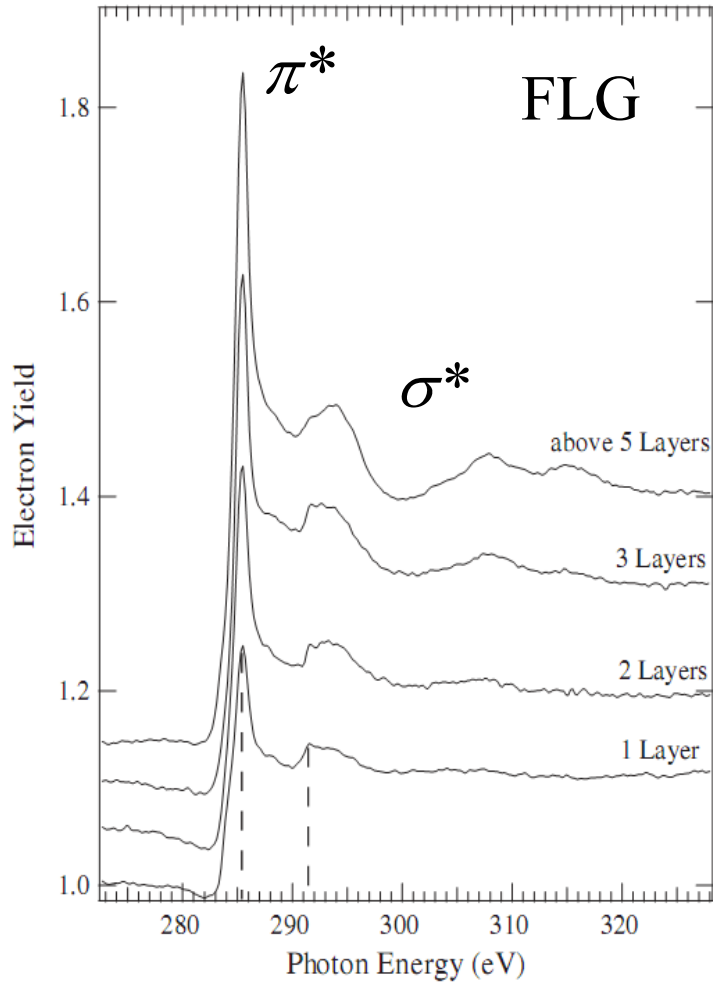
XAS of metallic (M) and semiconducting (S) SWCNTs



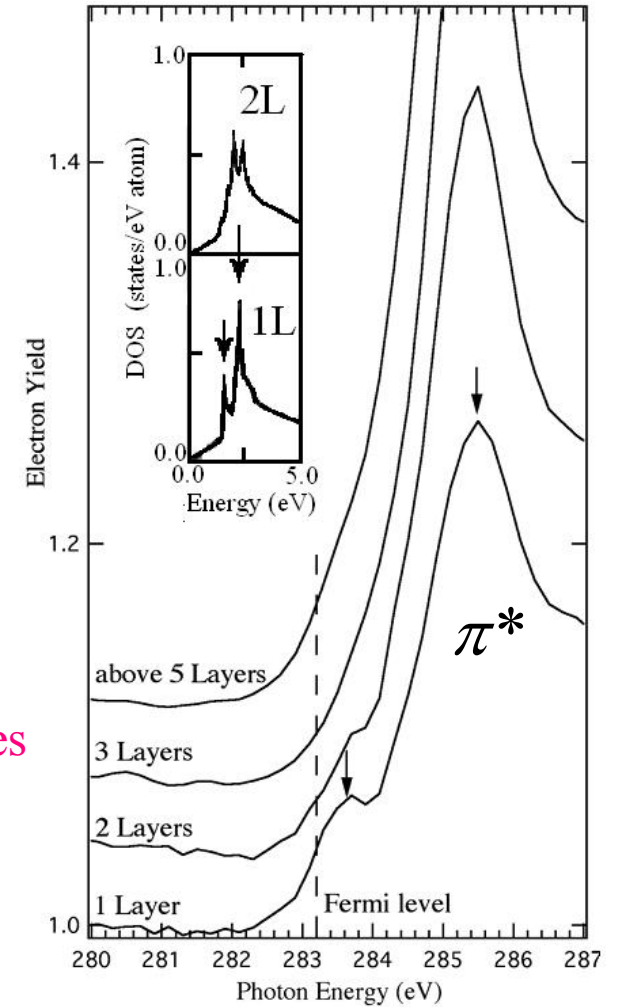
High-resolution XAS C1s absorption edges together with the results of a line shape analysis (thin lines) and TB DOS broadened by the experimental resolution.

[*] P. Ayala et al. Phys. Rev. B **80**, 205427 (2009).

CK-edge NEXAFS of Few Layer Graphene (FLG) [*]



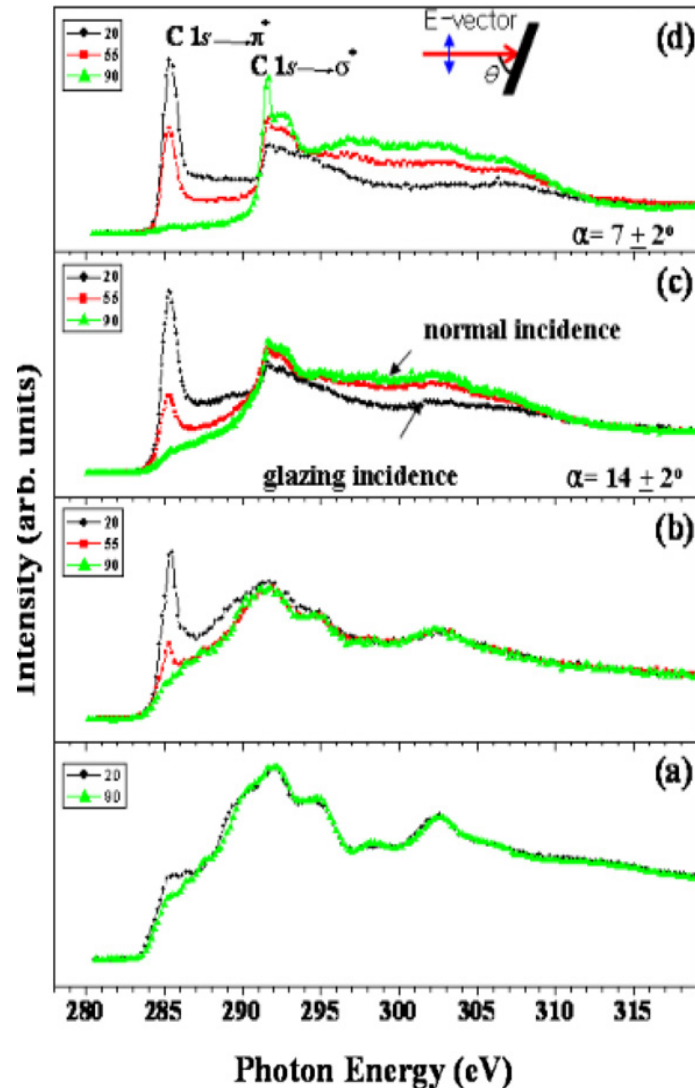
NEXAFS makes possible
to distinguish between graphenes
with different number of layers



[*] D. Pacile et al., Phys. Rev. Lett. **101**, 066806 (2008).

NEXAFS study of FLG Grown on 6H-SiC(0001) [*]

CK-edge NEXAFS spectra measured
at different incident angles



← 4th annealing at T=1400°C
(formation of thick graphene layer)

← 3rd annealing at T=1180°C
(growth of single phase graphene layers)

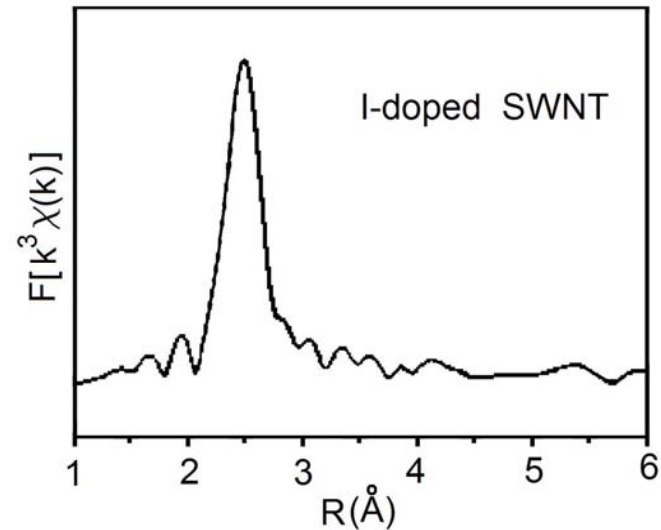
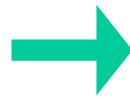
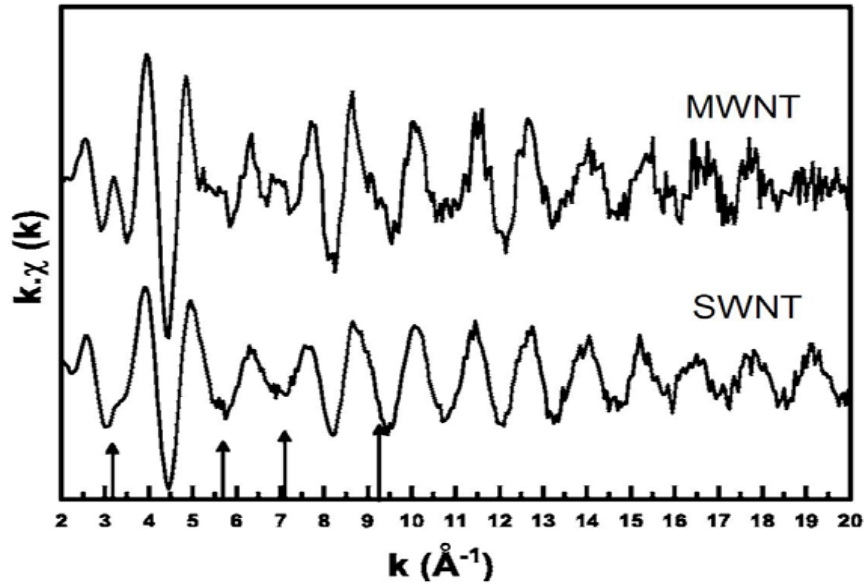
← 2nd annealing at T=1080°C
(formation of mixed phase (buffer) layer)

← 1st annealing at T= 900°C
(for substrate outgasing).

[*]. Ki-jeong Kim. J. Phys.: Condens. Matter 20, 225017 (2008).

EXAFS study of I-doped SWNTs [*]

EXAFS experiment at the ESRF (France)



FEFF calculation



TABLE 1. Structural parameters deduced from the least square fit of the first shells of the I-doped SWNTs samples

	Iodine shell	Carbon shell
N	0.8	2.2
σ^2	0.0016	0.02
ΔE	12.11	2.8
R	2.74	3.02

Measurements made:
in the transmission mode
at the iodine K -edge ($E_0 = 33.169$ keV)
at low temperature ($T = 10$ K)

[*] T. Michel et al. Phys. Rev. B **73**, 195419 (2006).

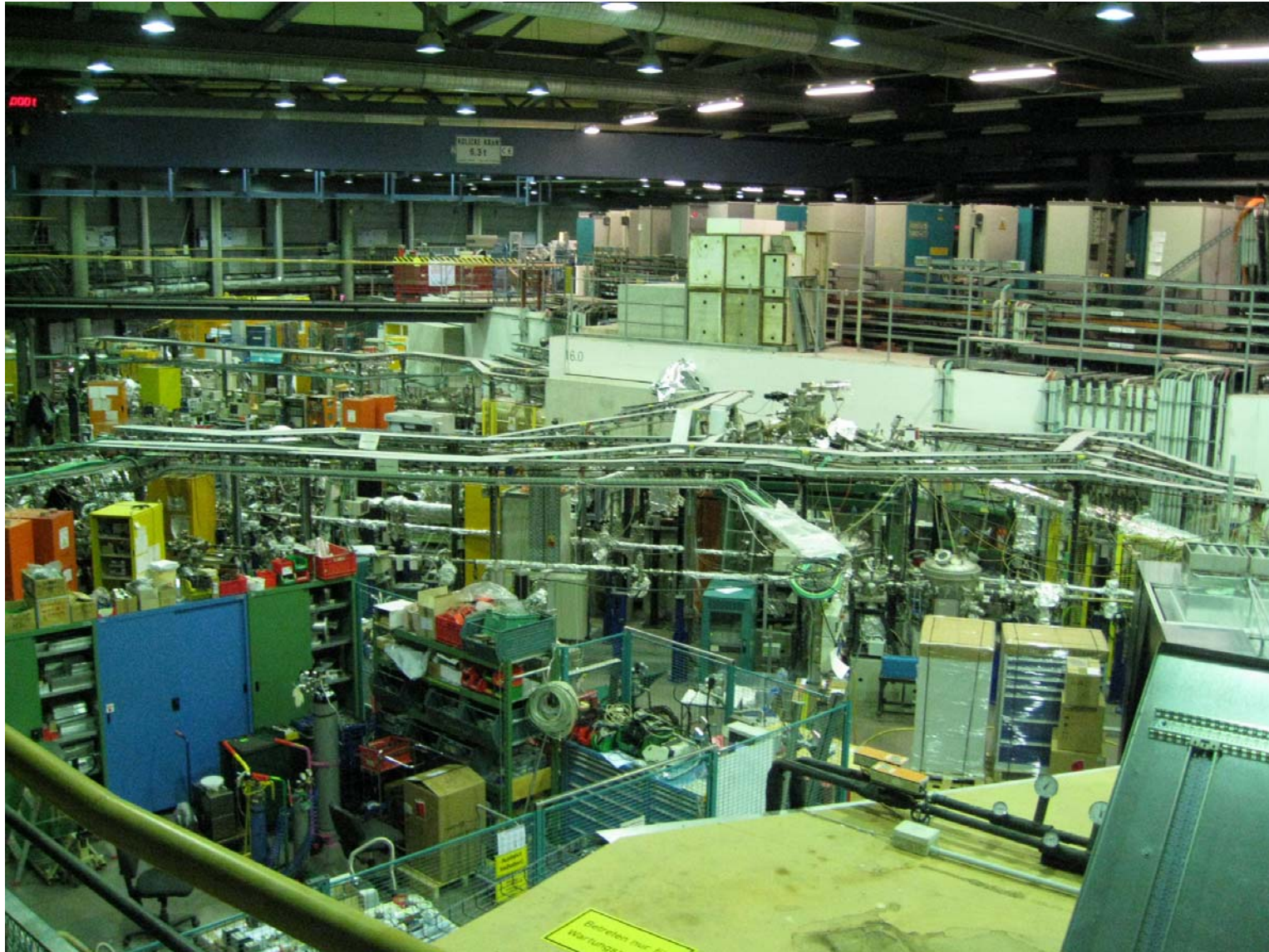
V. CONCLUSIONS

1. Modern **NEXAFS** spectroscopy proved to be one of the most powerful experimental techniques widely used for investigation of nanocarbon materials. It makes possible to probe not only their local electronic structure, but also a chemical composition and even atomic structure.
2. Application of **EXAFS** spectroscopy in this area of research is much more restricted. As a rule, this technique is used for probing a local atomic structure of composite materials, which along with the carbon atoms contain also the atoms of higher Z elements (such Fe, Ru, I) characterizing by much higher values of absorption edge energy and backscattering amplitude.

VI. MAIN SOURCES:

1. J. Stöhr. NEXAFS spectroscopy. Springer, 1996.
2. M. Newville. Fundamentals of XAFS. University of Chicago, 2004.
3. J. J. Rehr, R. C. Albers. Theoretical approaches to x-ray absorption fine structure. *Reviews of Modern Physics*, **72**, 621 (2000).
4. X-ray Absorption: Principles, Applications, Techniques of EXAFS, SEXAFS, and XANES, in *Chemical Analysis*, D. C. Koningsberger and R. Prins, ed., John. Wiley & Sons, 1988.
5. F.W. Lytle. The EXAFS family tree: a personal history of the development of extended X-ray absorption fine structure. *J. Synchrotron Rad.* **6**, 123 (1999).

Interior view of Synchrotron BESSY II



Experimental Station of Russian-German Beam Line

