

# Theory of thermal radiation from isolated neutron stars

**Alexander Y. Potekhin**<sup>1,2</sup>

in collaboration with:

Gilles Chabrier<sup>2</sup>

Andrey Chugunov<sup>1</sup>

Paweł Haensel<sup>3</sup>

Wynn Ho<sup>4</sup>

Alexander Kaminker<sup>1</sup>

Dong Lai<sup>5</sup>

Zach Medin<sup>6</sup>

Forrest Rogers<sup>7</sup>

Peter Shternin<sup>1</sup>

Valery Suleimanov<sup>8,9</sup>

Vadim Urpin<sup>1</sup>

Matt van Adelsberg<sup>10</sup>

Dmitry Yakovlev<sup>1</sup>

affiliations:

<sup>1</sup>*Ioffe Physical-Technical Institute, St.Petersburg (Russia)*

<sup>2</sup>*CRAL, Ecole Normale Supérieure de Lyon (France)*

<sup>3</sup>*CAMK, Warsaw (Poland)*

<sup>4</sup>*University of Southampton (UK)*

<sup>5</sup>*Cornell University (USA)*

<sup>6</sup>*Los Alamos National laboratory (USA)*

<sup>7</sup>*Lawrence Livermore National Laboratory (USA)*

<sup>8</sup>*Universität Tübingen (Germany)*

<sup>9</sup>*Kazan Federal University (Russia)*

<sup>10</sup>*Georgia Institute of Technology (USA)*

and also: Denis Baiko, Victor Bezchastnov, George Pavlov, Chris Pethick,  
Yuri Shibano, Joseph Ventura, ...

# Theory of thermal radiation from isolated neutron stars

Alexander Y. Potekhin

## Outline:

1. Introduction
2. Envelopes: EOS, conductivities, thermal structure, and cooling
3. Atmospheres: EOS, opacities, spectra
4. Radiation from condensed surface and symbiotic models

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# Theory of thermal radiation from isolated neutron stars

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## Outline:

1. Introduction
2. Atmospheres with strong magnetic fields
3. Radiation from condensed surface and symbiotic models

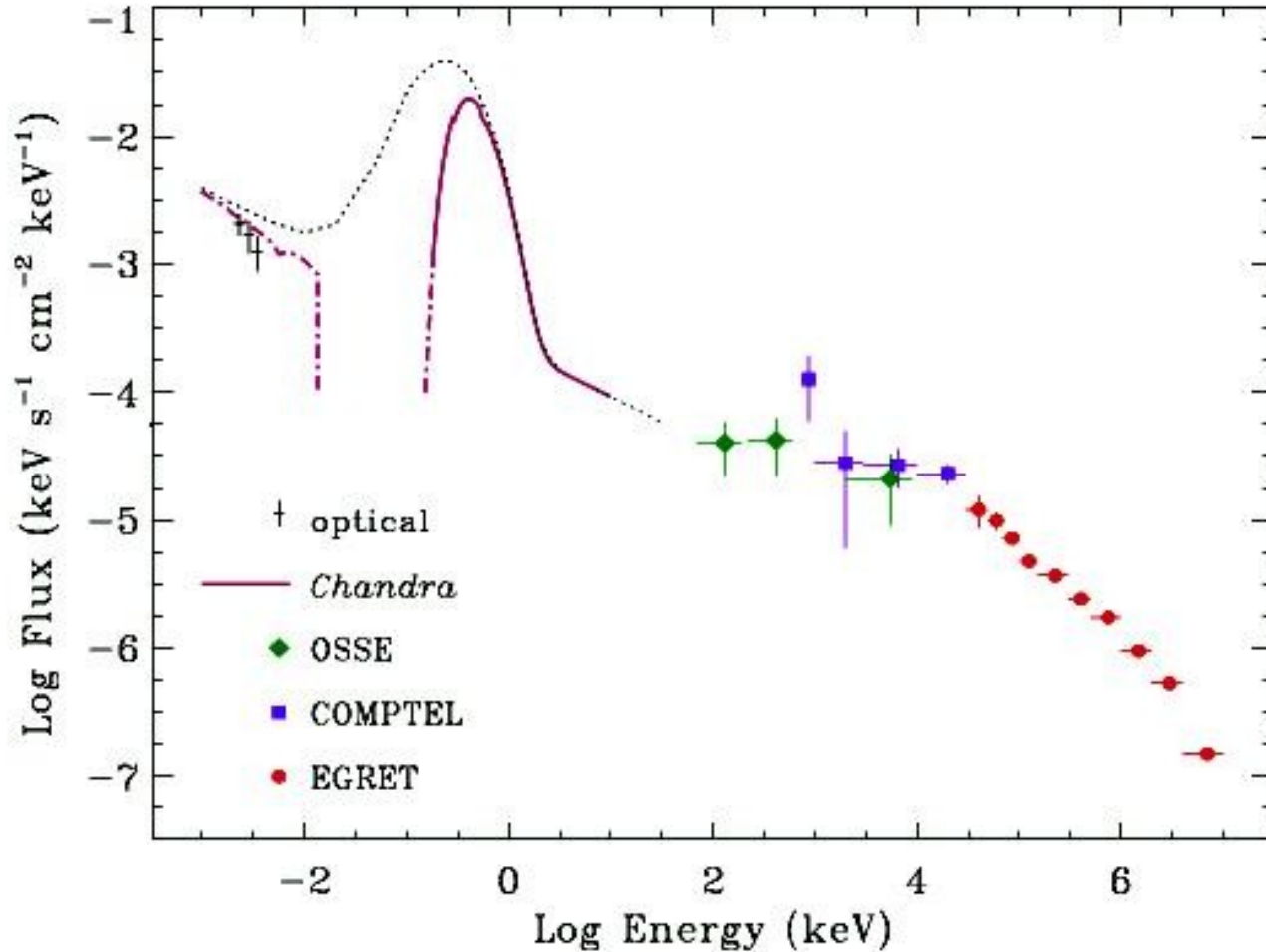
# Theory of thermal radiation from isolated neutron stars

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Plan:

1. Introduction
2. Fully ionized magnetic atmospheres
3. Partially ionized magnetic H atmospheres
4. Radiation from condensed surface
5. Integral spectra, thin and layered atmospheres
6. Heavier-element magnetic atmospheres
7. Challenges from superstrong fields
8. Link with observations. Cyclotron harmonics & the case of 1E 1207.4–5209.

## Typical multiwavelength spectrum of an isolated neutron star

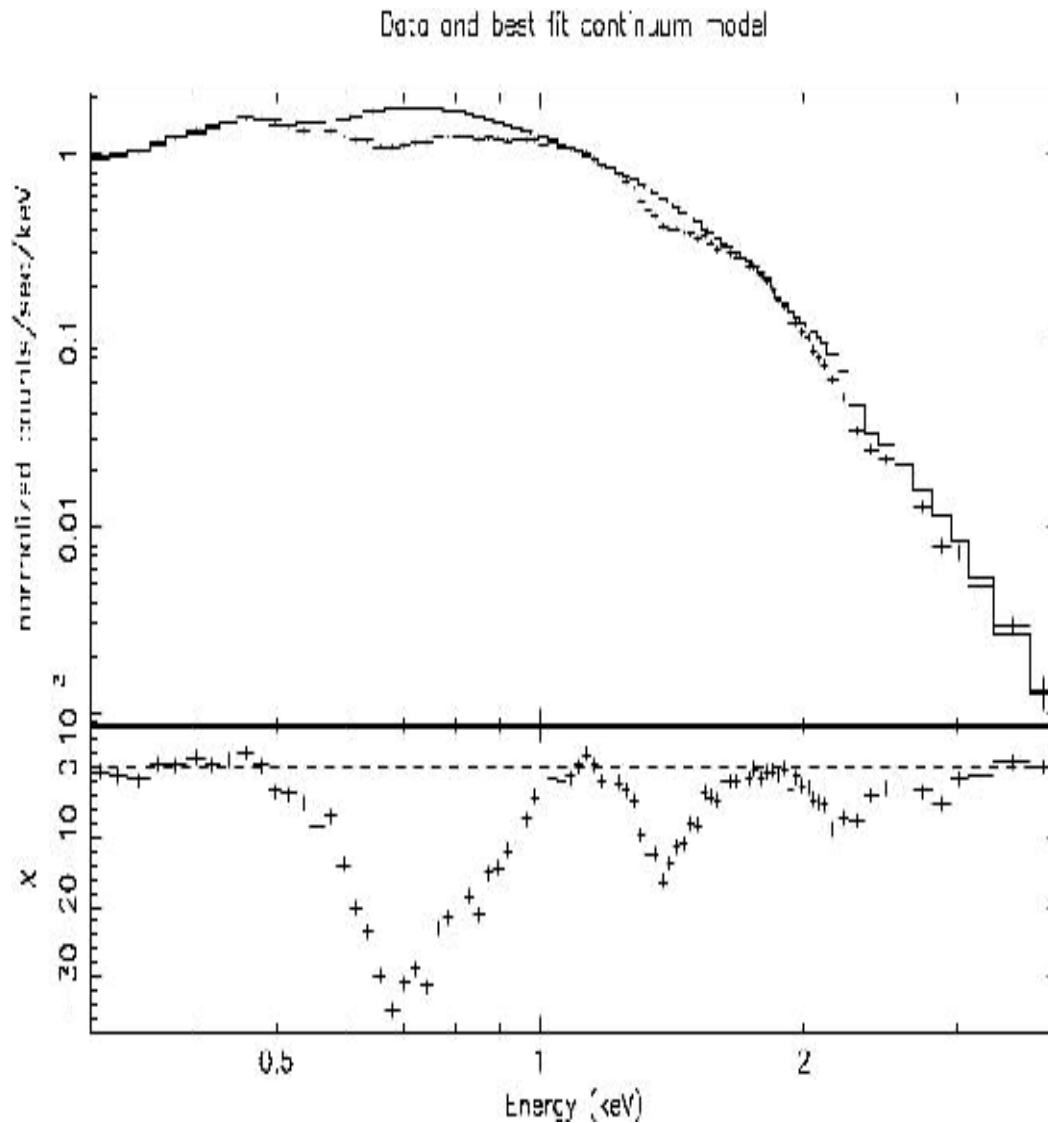


### Multiwavelength spectrum of the Vela pulsar

G.G.Pavlov, V.E.Zavlin, & D.Sanwal (2002) in *Neutron Stars, Pulsars, and Supernova Remnants*, ed. W.Becker, H.Lesch, & J.Trümper, *MPE Report* **278**, 273

# Absorption lines in spectra of thermally emitting neutron stars

CCO 1E 1207.4–5209

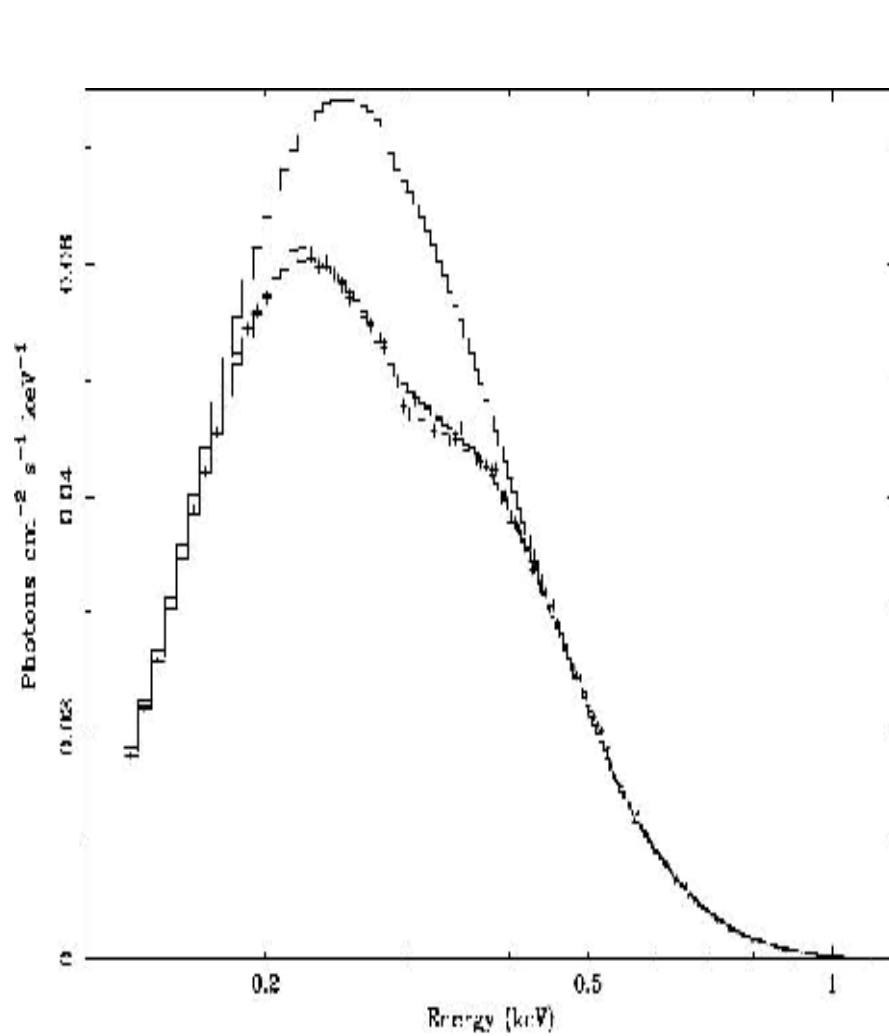


D.Sanwal *et al.* (2002);  
S.Mereghetti *et al.* (2002);  
G.Bignami *et al.* (2003):  
2 (3? 4?) lines in 1E1207.4–5209.

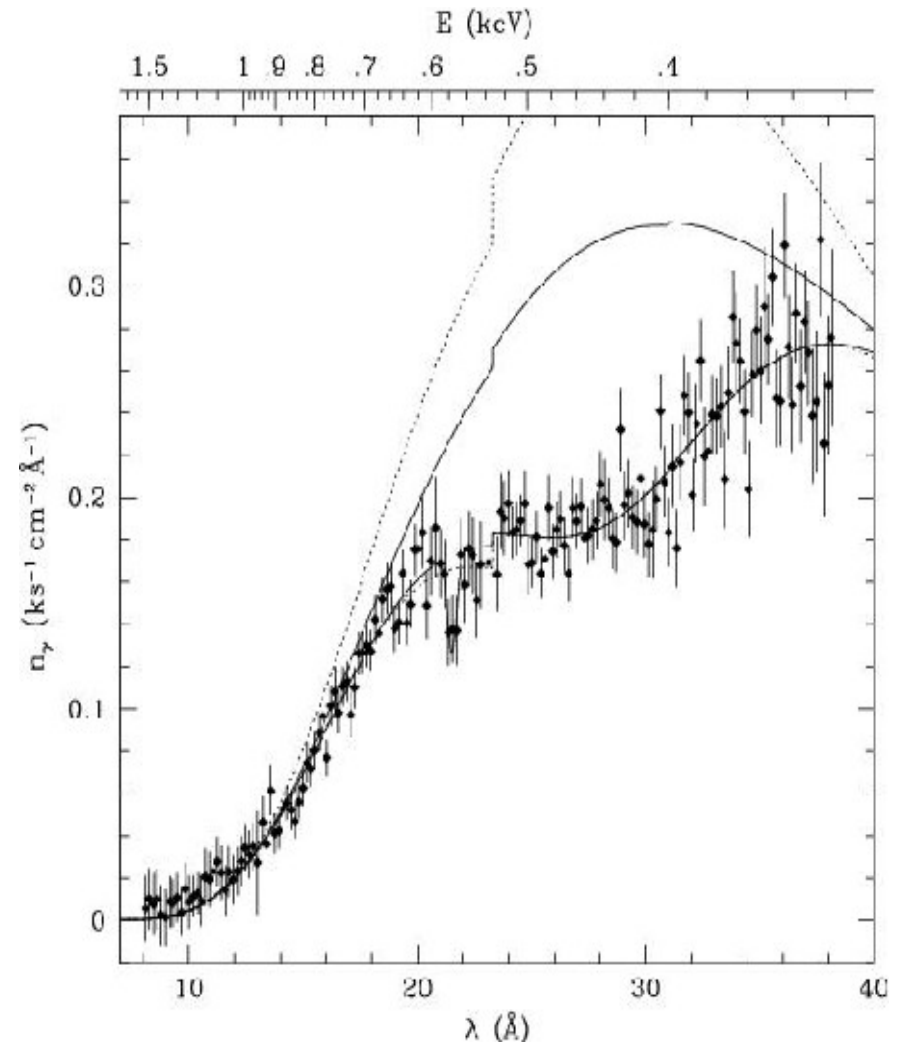
[Figure from Bignami *et al.* (2004)  
*Mem.S.A.It.* 75, 448]

# Absorption lines in spectra of thermally emitting neutron stars

## XDINSs



F.Haberl *et al.* (2004) *A&A* **419**, 1077:  
absorption in RX J0720.4-3125



M. van Kerkwijk *et al.* (2004) *ApJ* **608**, 432:  
absorption in RX J1605.3+3249



XDINS – X-ray dim isolated neutron star

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Magnificent Seven

XDINS – X-ray dim isolated neutron star

Magnificent **Seven**

XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

XDINS – X-ray dim isolated neutron star

Magnificent Seven

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Magnificent Seven

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XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

RQINS – radio quiet isolated neutron star



XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

RQINS – radio quiet isolated neutron star

XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

RQINS – radio quiet isolated neutron star

INS – isolated neutron star (*Vicky Kaspi*)

XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

RQINS – radio quiet isolated neutron star

INS – **isolated** neutron star (*Vicky Kaspi*)

XDINS – X-ray dim isolated neutron star

Magnificent Seven

NTEINS – nearby thermally emitting isolated neutron star (*David Kaplan*)

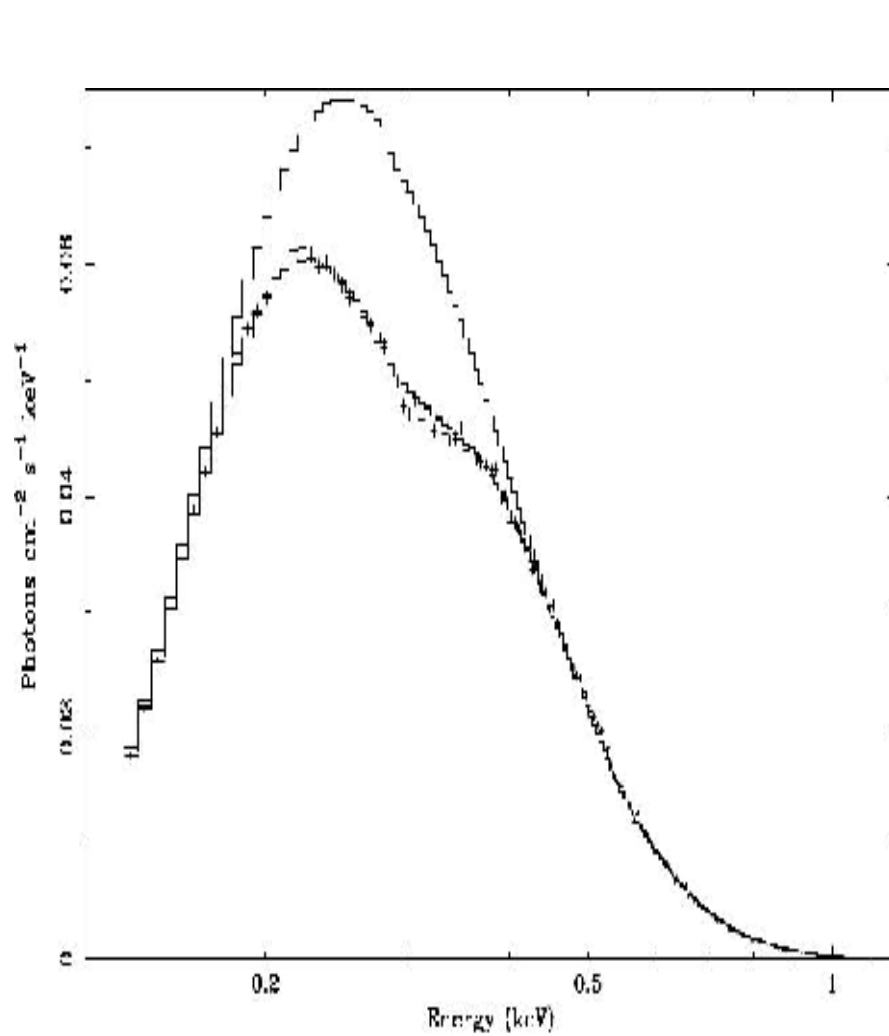
RQINS – radio quiet isolated neutron star

INS – isolated neutron star (*Vicky Kaspi*)

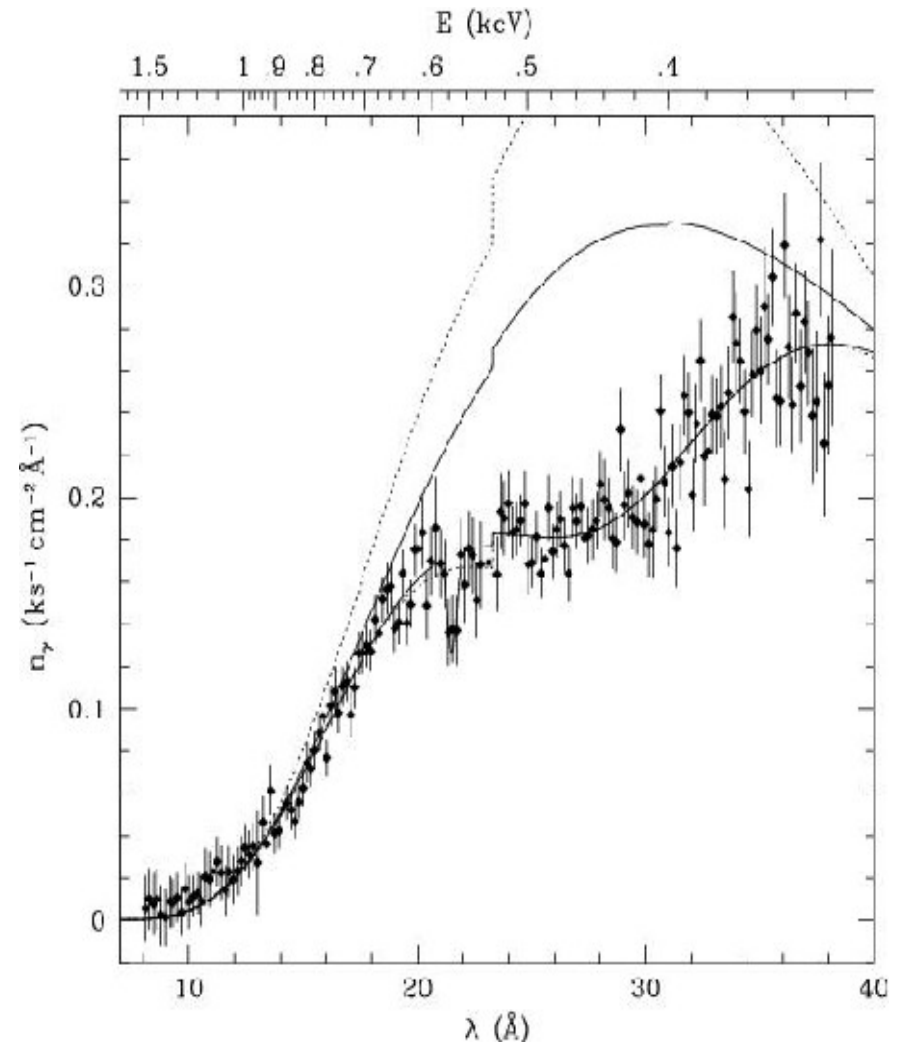
HMTERQINS – highly magnetized thermally emitting radio quiet isolated neutron star

# Absorption lines in spectra of isolated neutron stars

## XDINSs

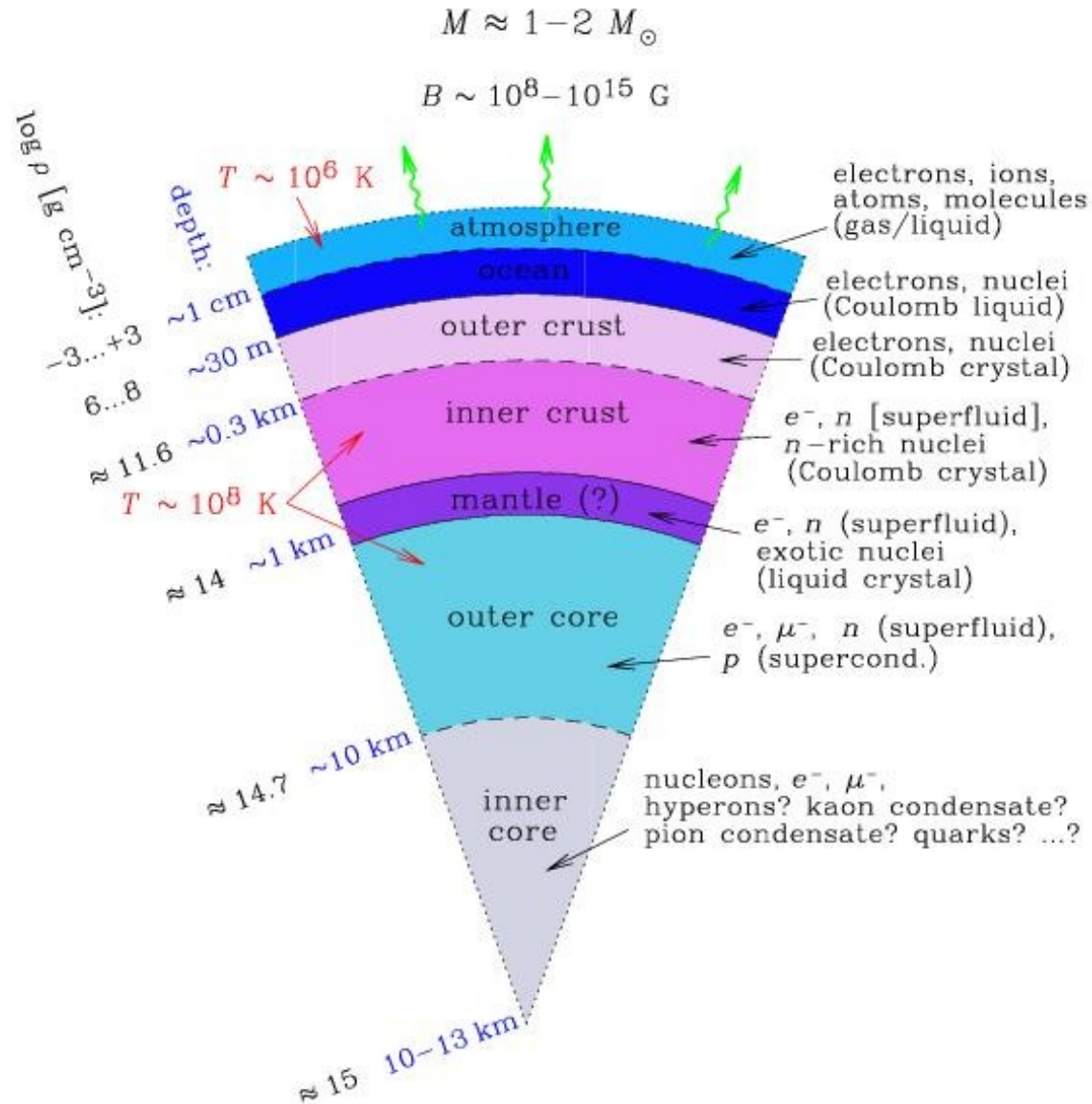


F.Haberl *et al.* (2004) *A&A* **419**, 1077:  
absorption in RX J0720.4-3125

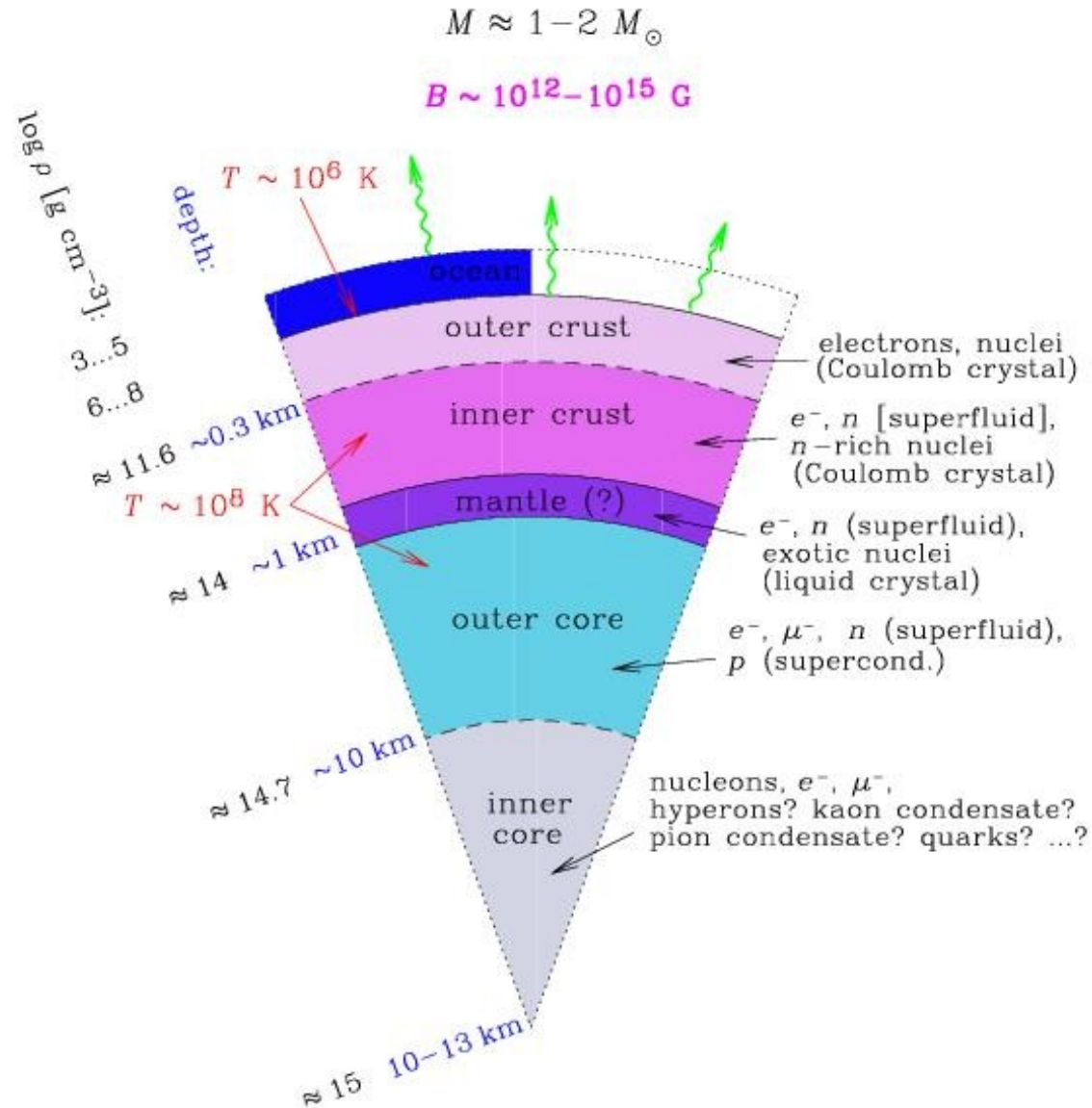


M. van Kerkwijk *et al.* (2004) *ApJ* **608**, 432:  
absorption in RX J1605.3+3249

# Neutron star structure



# Neutron star without atmosphere: possible result of a phase transition



# Characteristic values of the magnetic field

- Strong magnetic field  $B$  :

$$\hbar\omega_c = \hbar eB/m_e c > 1 \text{ a.u.}$$

$$B > m_e^2 c e^3 / \hbar^3 = 2.35 \times 10^9 \text{ G}$$

- Superstrong field :

$$\hbar\omega_c > m_e c^2$$

$$B > m_e^2 c^3 / e \hbar = 4.4 \times 10^{13} \text{ G}$$

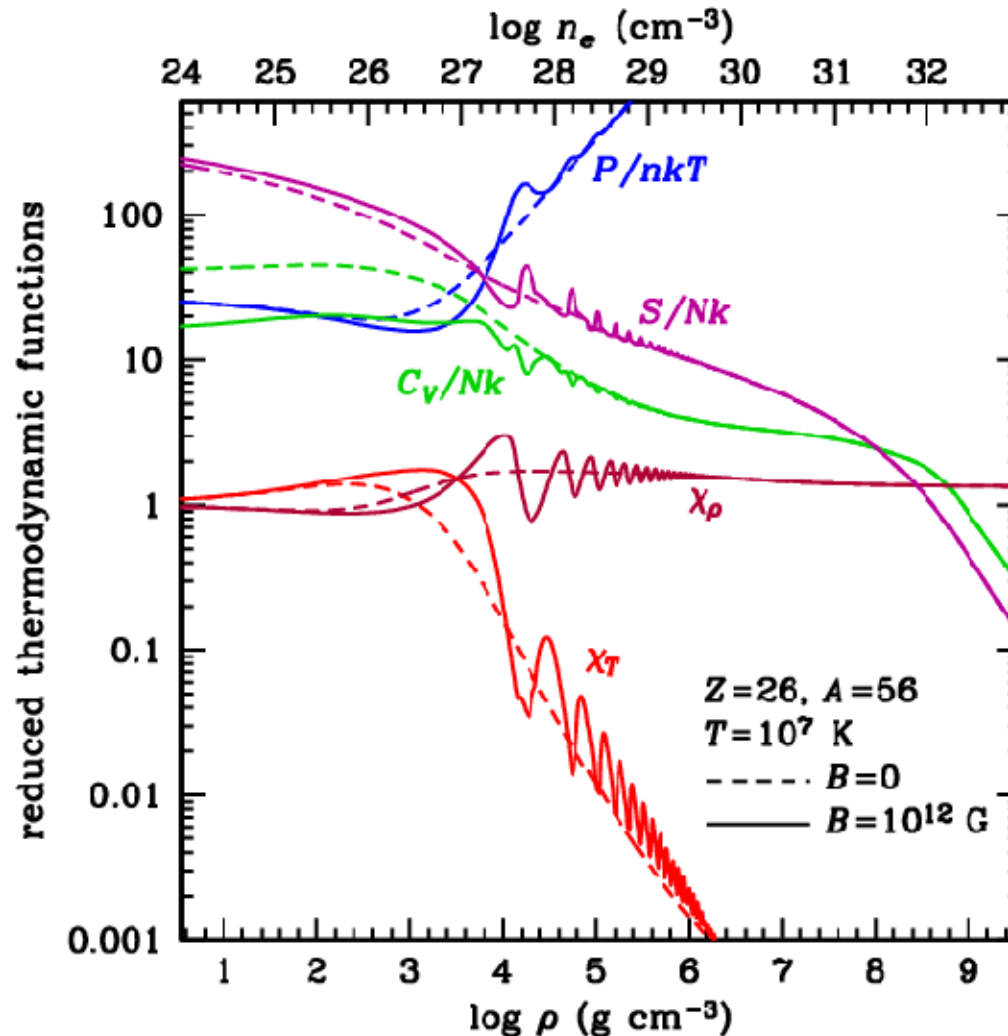
- Strongly quantizing magnetic field :

$$\rho < \rho_B = m_{\text{ion}} n_B \langle A \rangle / \langle Z \rangle \approx 7 \times 10^3 B_{12}^{3/2} (\langle A \rangle / \langle Z \rangle) \text{ g cm}^{-3}$$

$$T \ll T_B = \hbar\omega_c / k_B \approx 1.3 \times 10^8 B_{12} \text{ K}$$



# Equation of state of magnetic neutron star envelopes

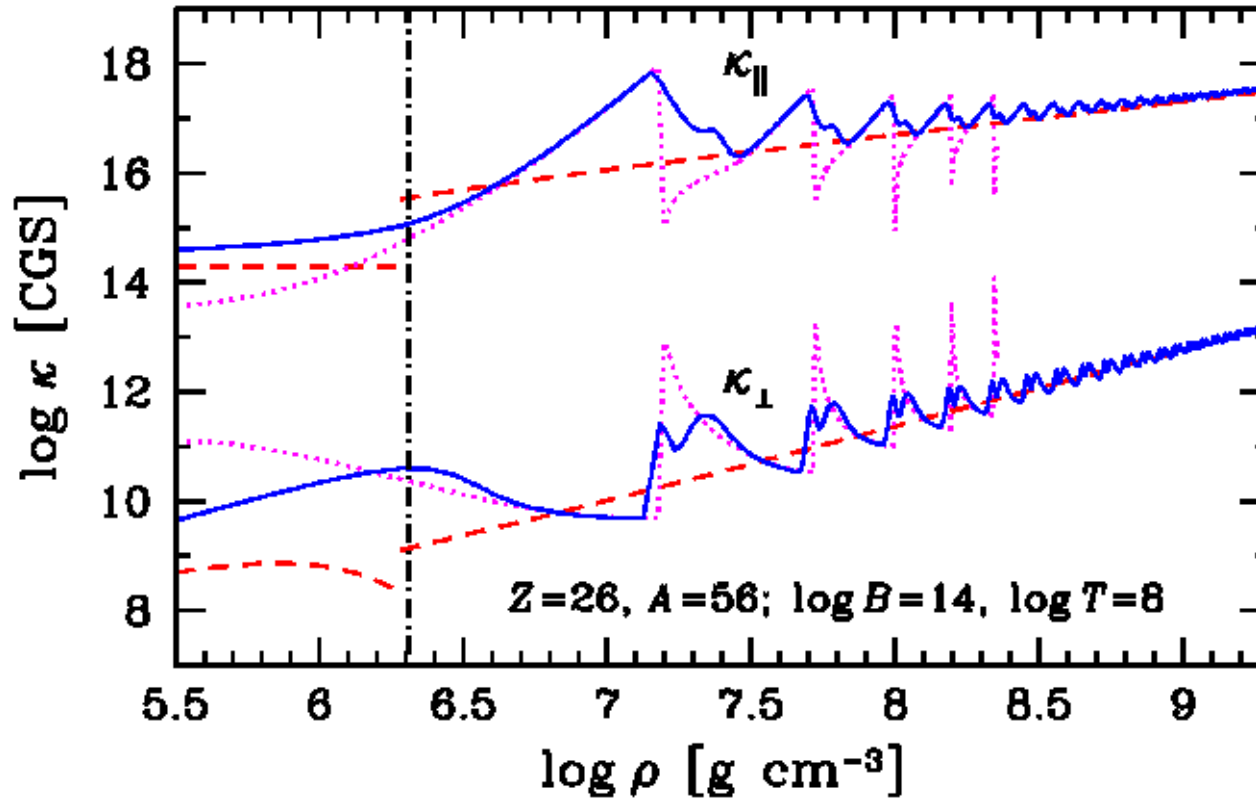


Normalized thermodynamic functions of fully ionized iron without magnetic field (dashed lines) and in a strong magnetic field (solid lines)

[Haensel et al., *Neutron Stars. 1. Equation of State and Structure* (Springer, New York, 2007), Chap.4, + refs. therein]

# Thermal conductivities in a strongly magnetized envelope

<http://www.ioffe.ru/astro/conduct/>



Solid – exact, dots – without  $T$ -integration, dashes – magnetically non-quantized

Ventura & Potekhin (2001), in *The Neutron Star – Black Hole Connection*, ed. Kouveliotou *et al.* (Dordrecht: Kluwer) 393

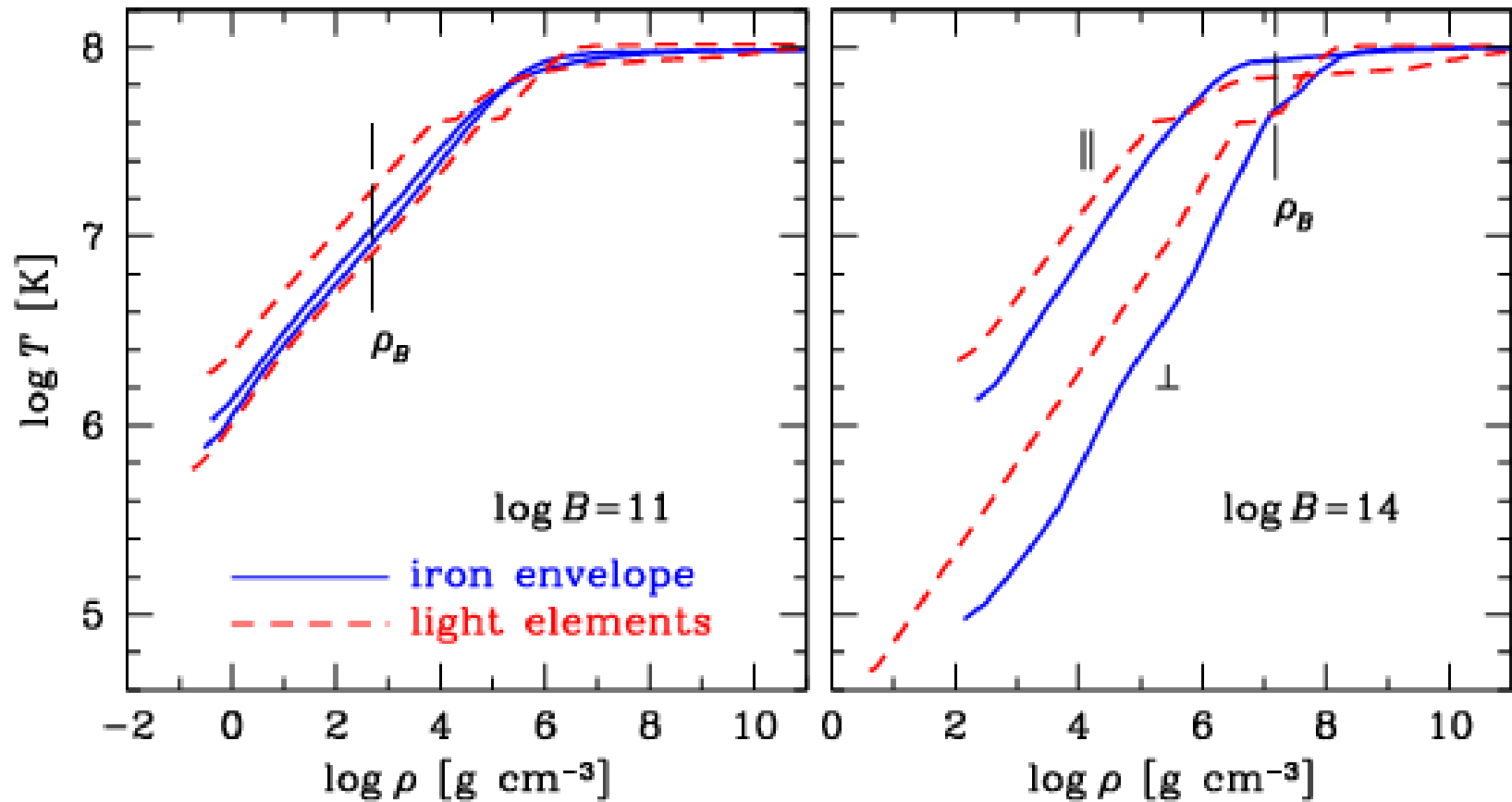
**Summary and update:** Cassisi, Potekhin, Pietrinferni, Catelan, & Salaris (2007) *Astrophys.J.* **661**, 1094  
[+ references!]

**Heat conduction by ions:** Chugunov & Haensel (2009) *MNRAS* **381**, 1143

**Heat conduction by neutrons:** Aguilera *et al.* (2009) *Phys. Rev. Lett.* **102**, 091109

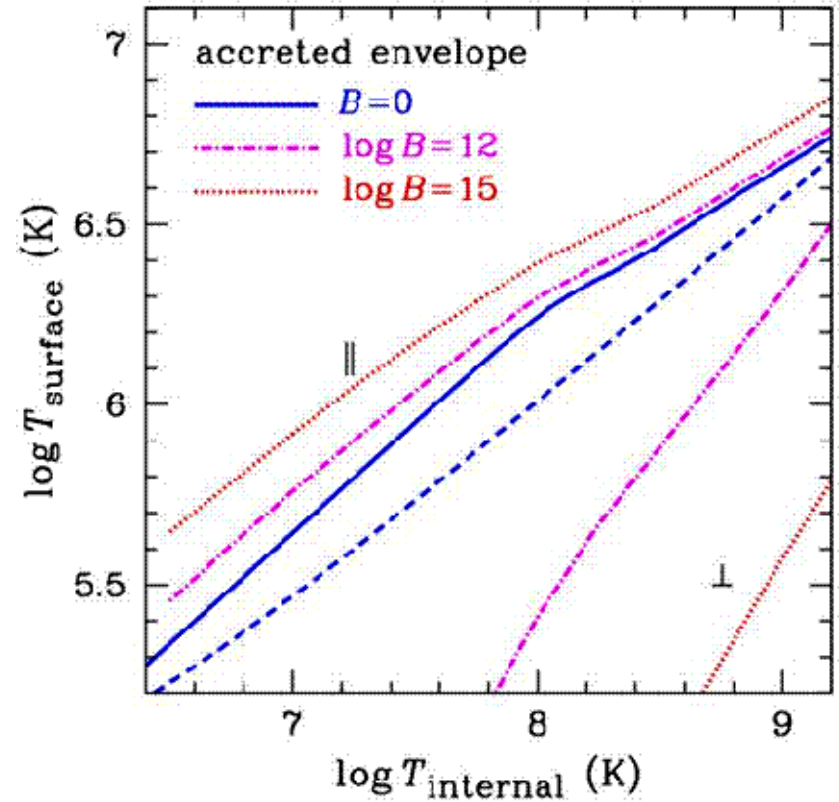
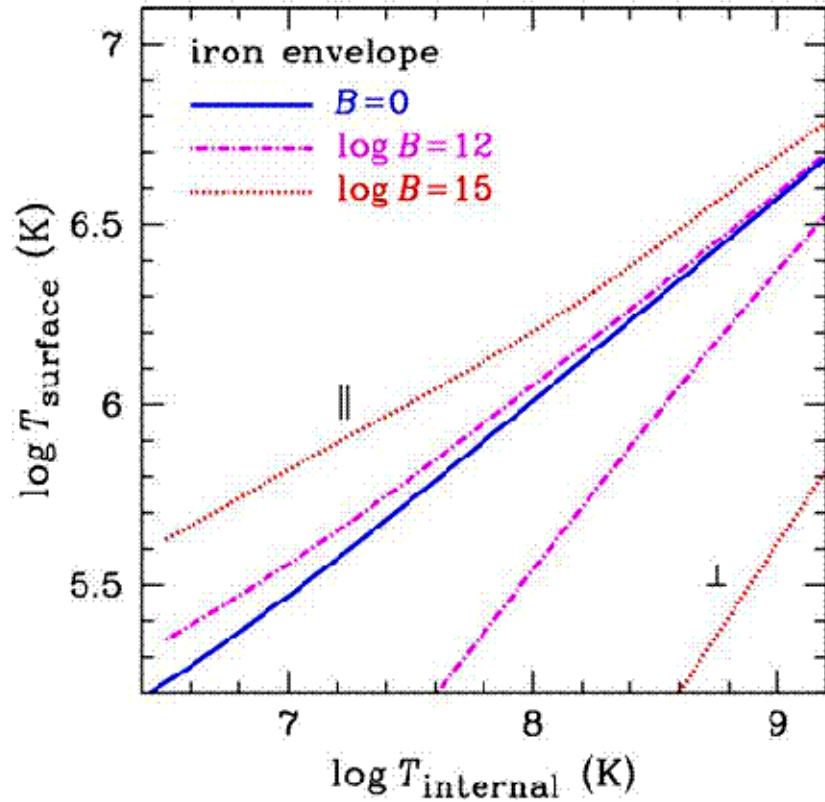
**Electron conduction at very low temperatures:** Chugunov (2011), to be published

*Temperature profiles  
in envelopes of neutron stars with strong magnetic fields*



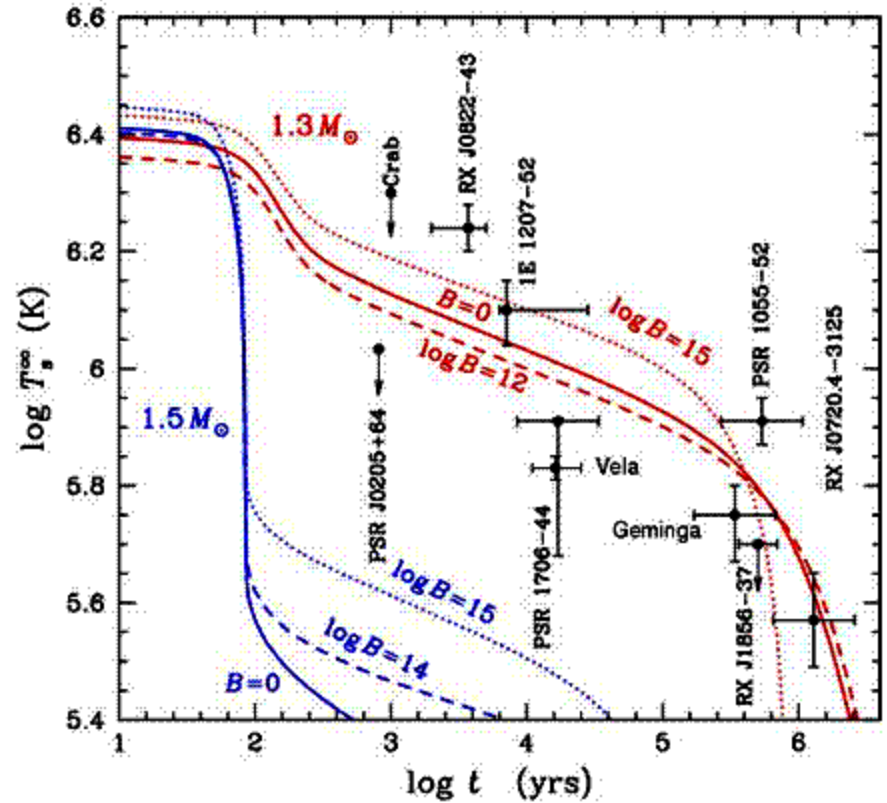
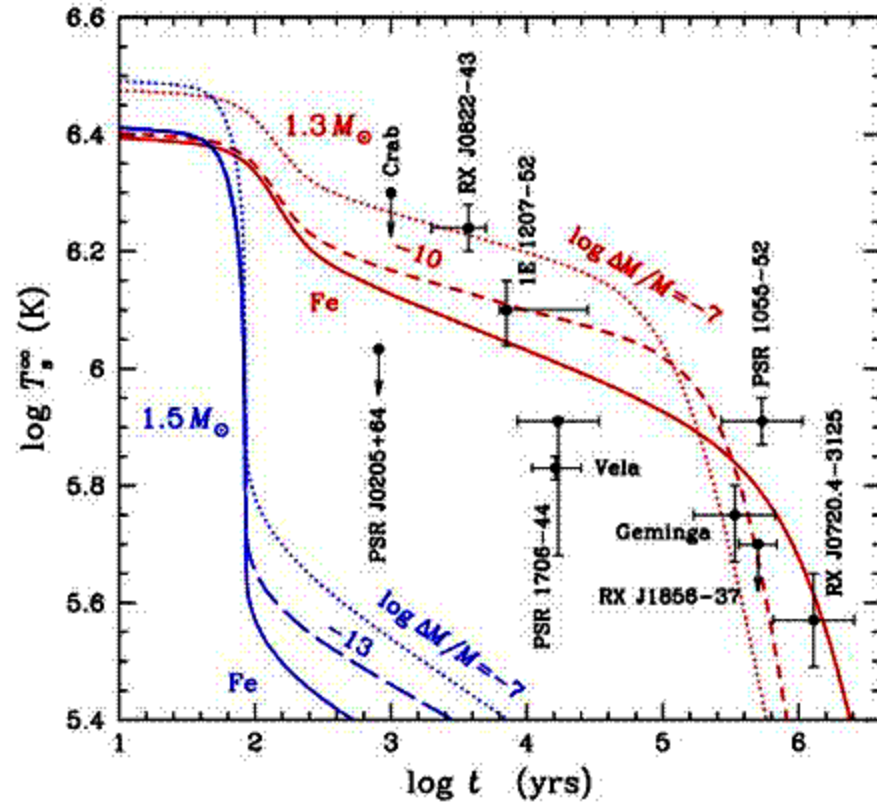
$$T_s - T_b$$

## Temperature drops in magnetized envelopes of neutron stars



## Cooling of neutron stars with accreted envelopes

## Cooling of neutron stars with magnetized envelopes



# *Atmospheres: general*

Standard methods – D.Mihalas (1978) *Stellar Atmospheres*

General algorithm - solution of coupled equations:

- Hydrostatic equilibrium
- Energy balance
- Radiative transfer

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Basic ingredients:

- Equation of state
- Radiative opacities

# *Atmospheres: general*

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Basic ingredients:

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- Radiative opacities

This generally requires:

- Atomic and molecular data (binding energies, cross sections)
- Ionization and dissociation equilibrium
- Thermodynamic quantities
- Treatment of plasma effects (line broadening, pressure ionization, etc.)

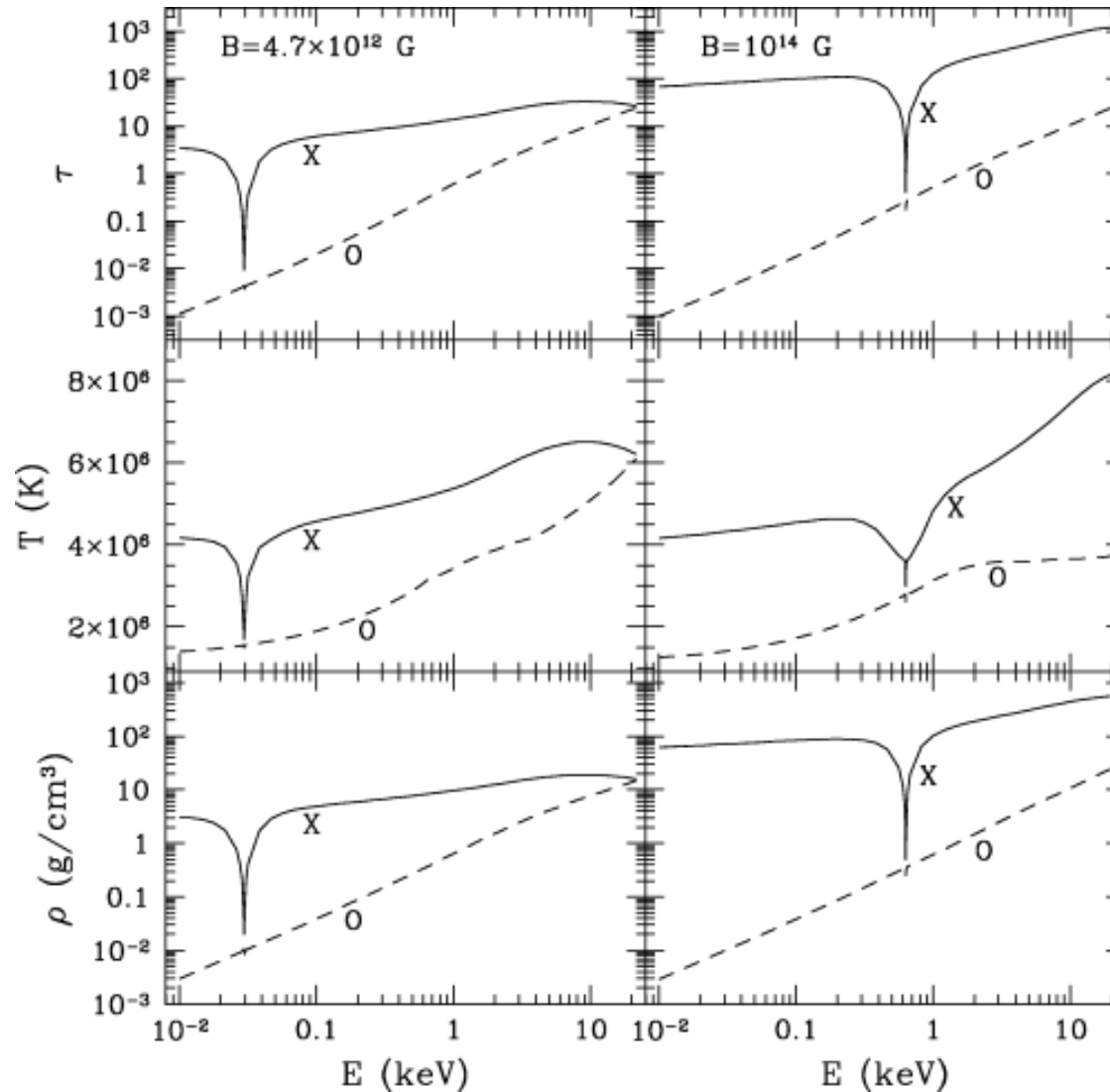


# *Fully ionized neutron star atmospheres with strong magnetic fields*

Yu.N.Gnedin,  
G.G.Pavlov,  
Yu.A.Shibanov,  
A.D.Kaminker,  
D.G.Yakovlev,  
(1970s – 1980s)

V.E.Zavlin,  
Yu.A.Shibanov,  
G.G.Pavlov,  
J.Ventura  
(1990s)

W.C.G.Ho & D.Lai  
(2000s)



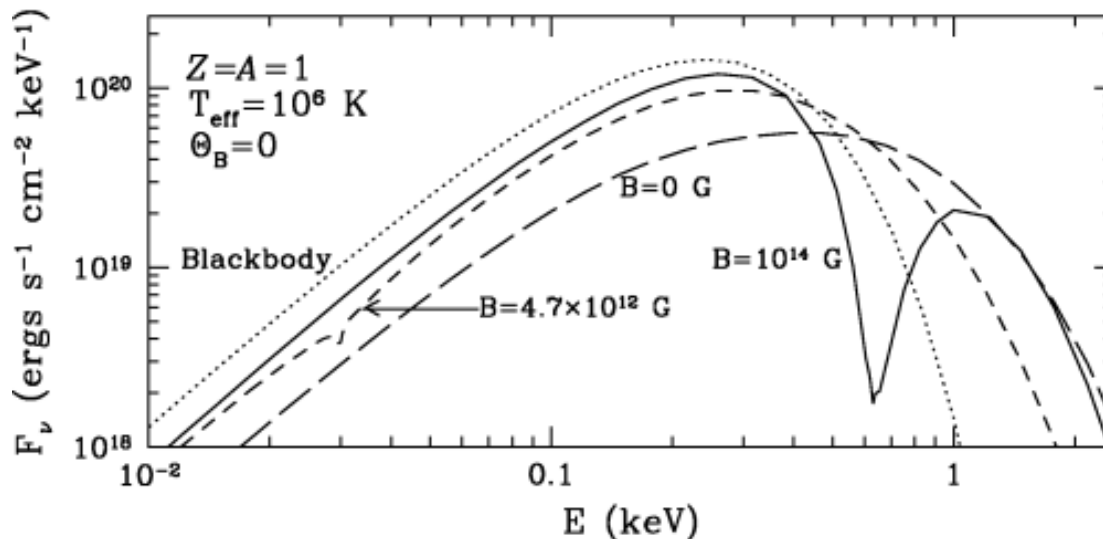
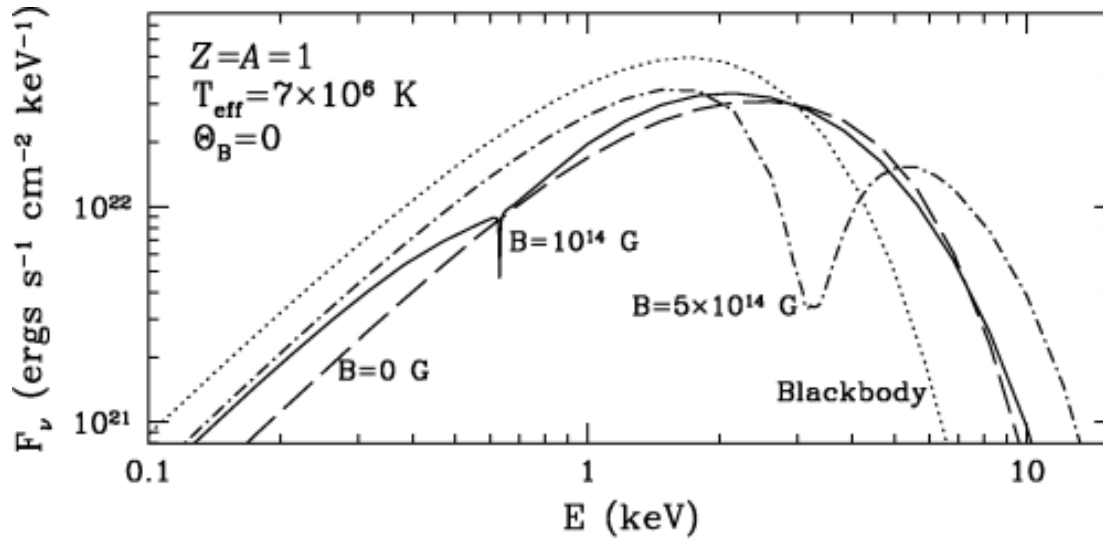
Bottom of the atmosphere for X- and O-modes of polarization in strong magnetic fields

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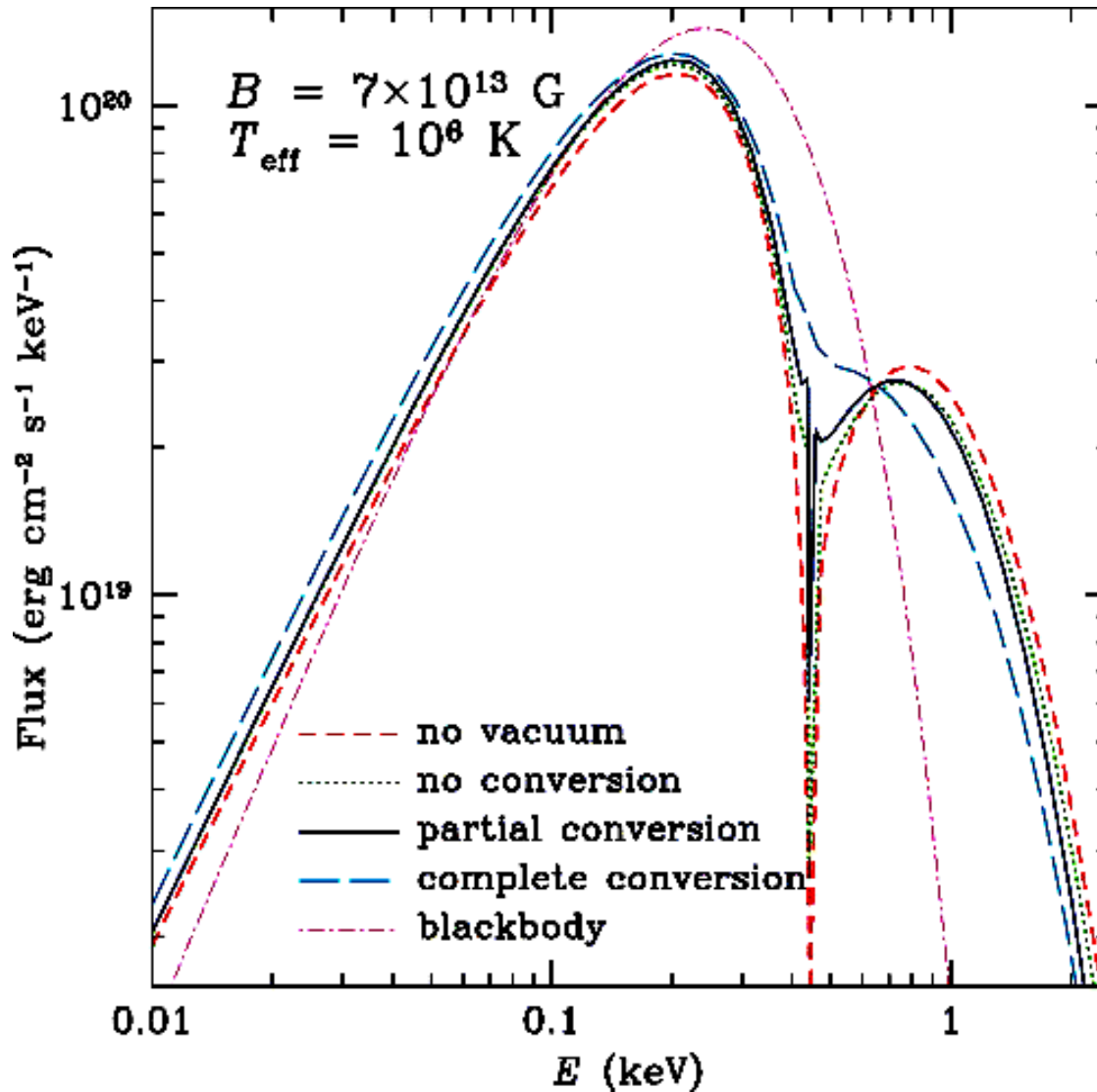
Comparison of spectra for non-magnetic and magnetic H atmospheres

# The effect of vacuum polarization

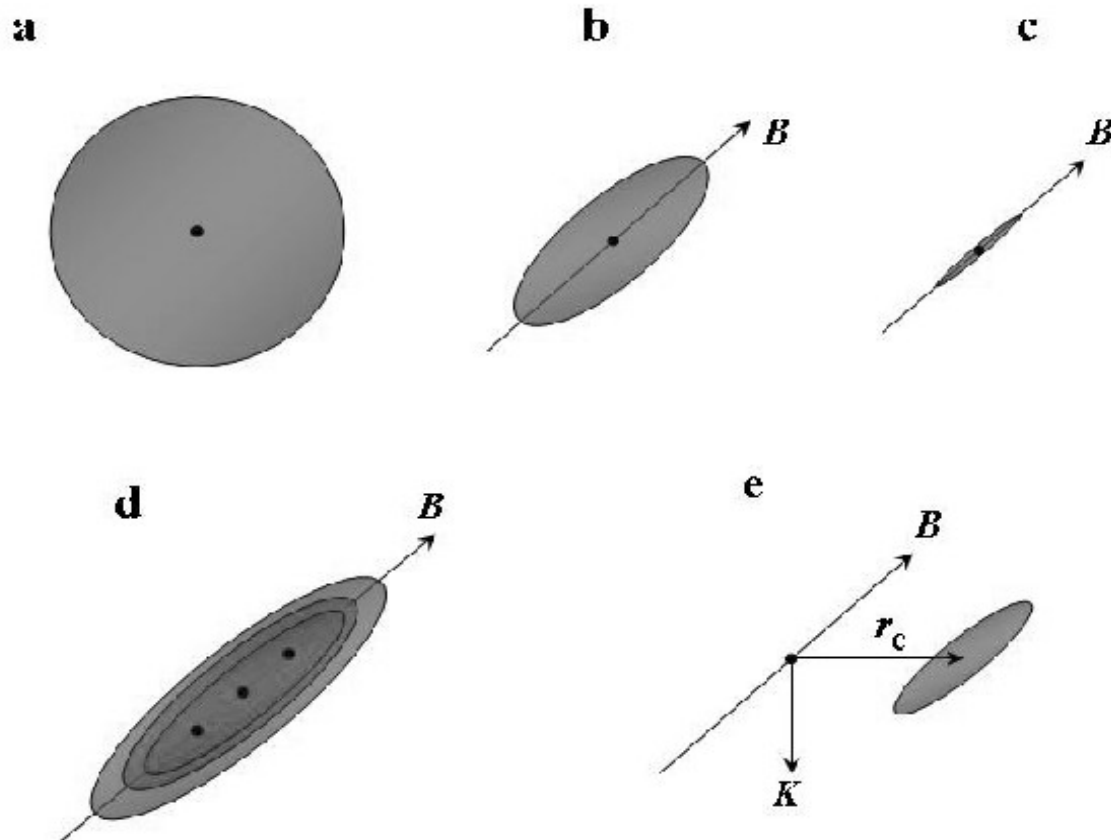
Yu.N.Gnedin & G.G.Pavlov  
(1970s – 1984)

W.C.G.Ho & D.Lai (2003)  
*MNRAS* 338, 233

M.van Adelsberg & D.Lai  
(2007) *MNRAS* 373, 495



## *Bound species in a strong magnetic field*



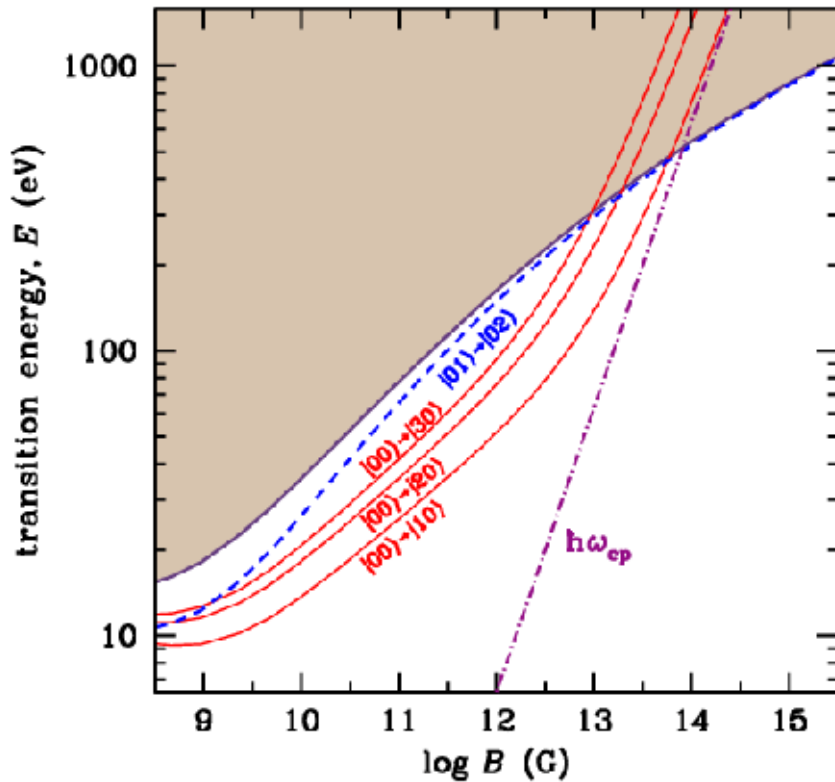
The effects of a strong magnetic field on the atoms and molecules.

**a–c:** H atom in the ground state (**a:**  $B \ll 10^9$  G, **b:**  $B \sim 10^{10}$  G, **c:**  $B \sim 10^{12}$  G).

**d:** The field stabilizes the molecular chains ( $H_3$  is shown).

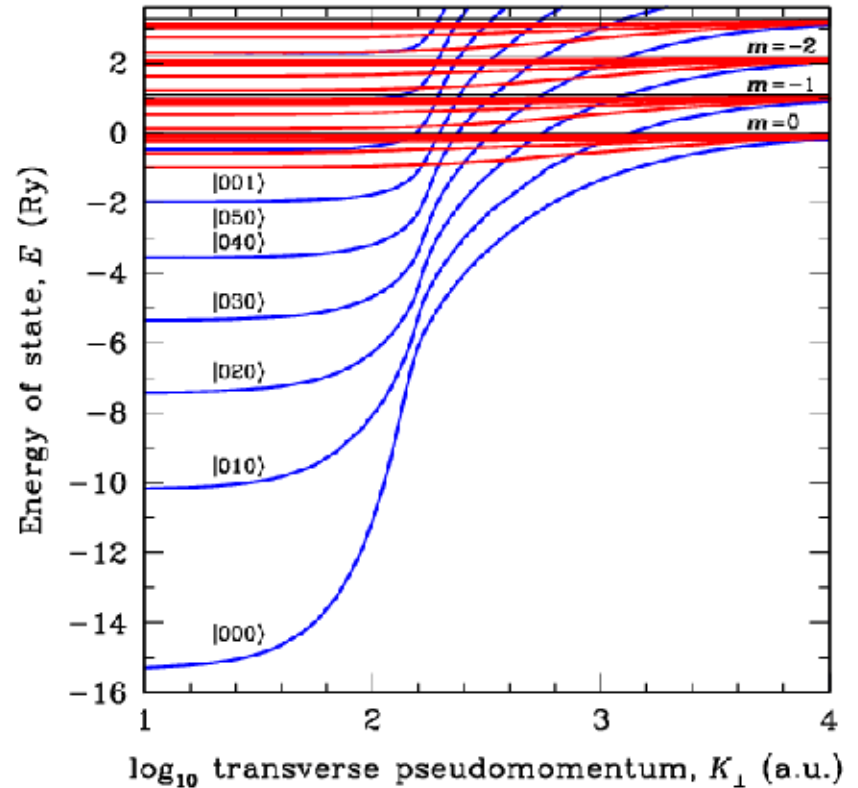
**e:** H atom moving across the field becomes decentered.

## Bound species in a strong magnetic field



Main transition energies of the hydrogen atom in a magnetic field

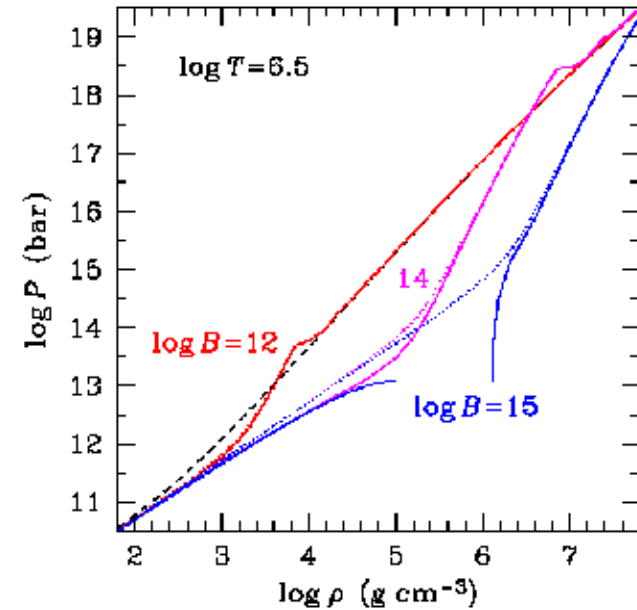
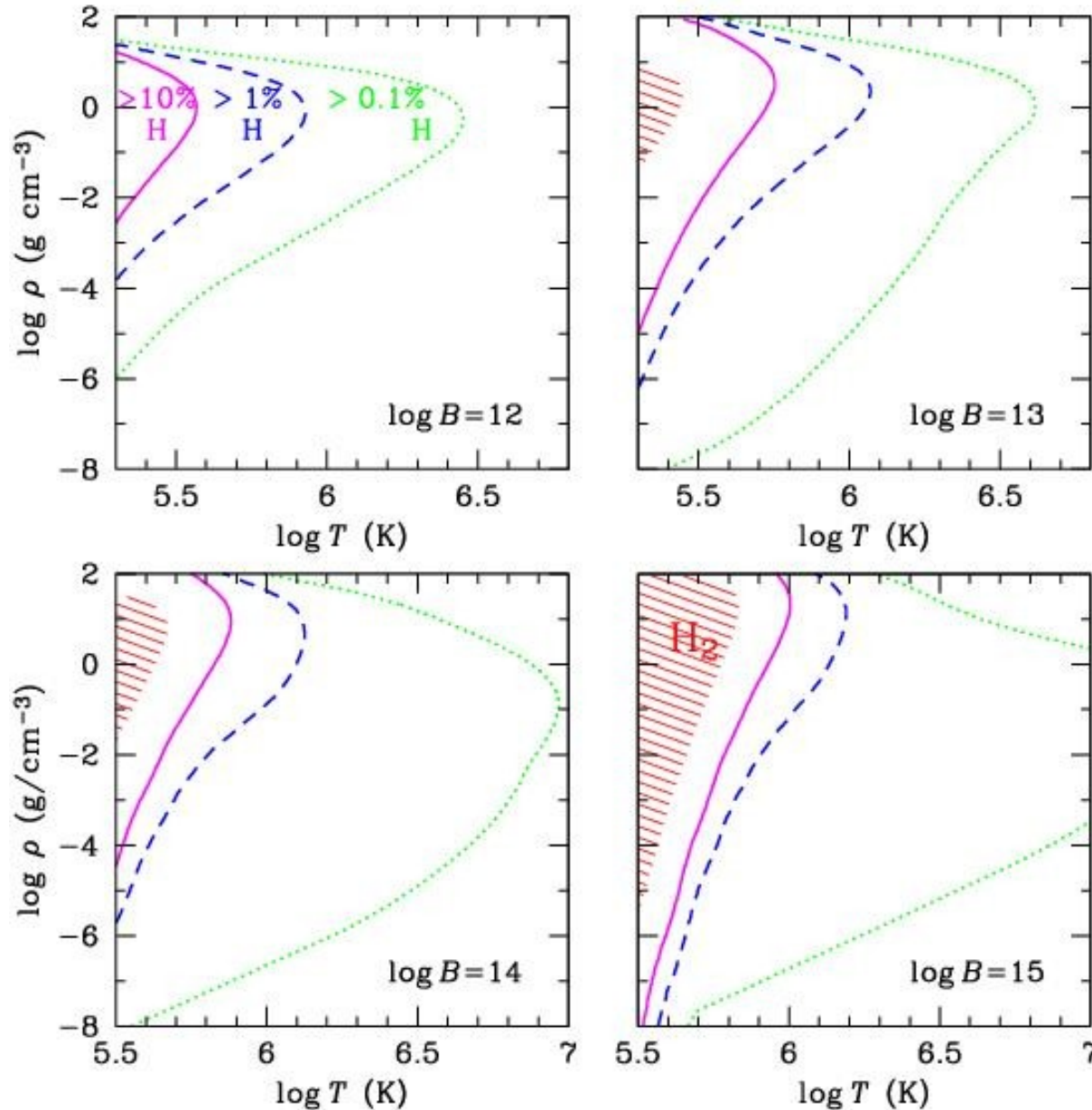
[Potekhin & Chabrier (2004) *ApJ*, **600**, 317]



Binding energies of the hydrogen atom in the magnetic field  $B=2.35 \times 10^{12}$  G as functions of its state of motion across the field

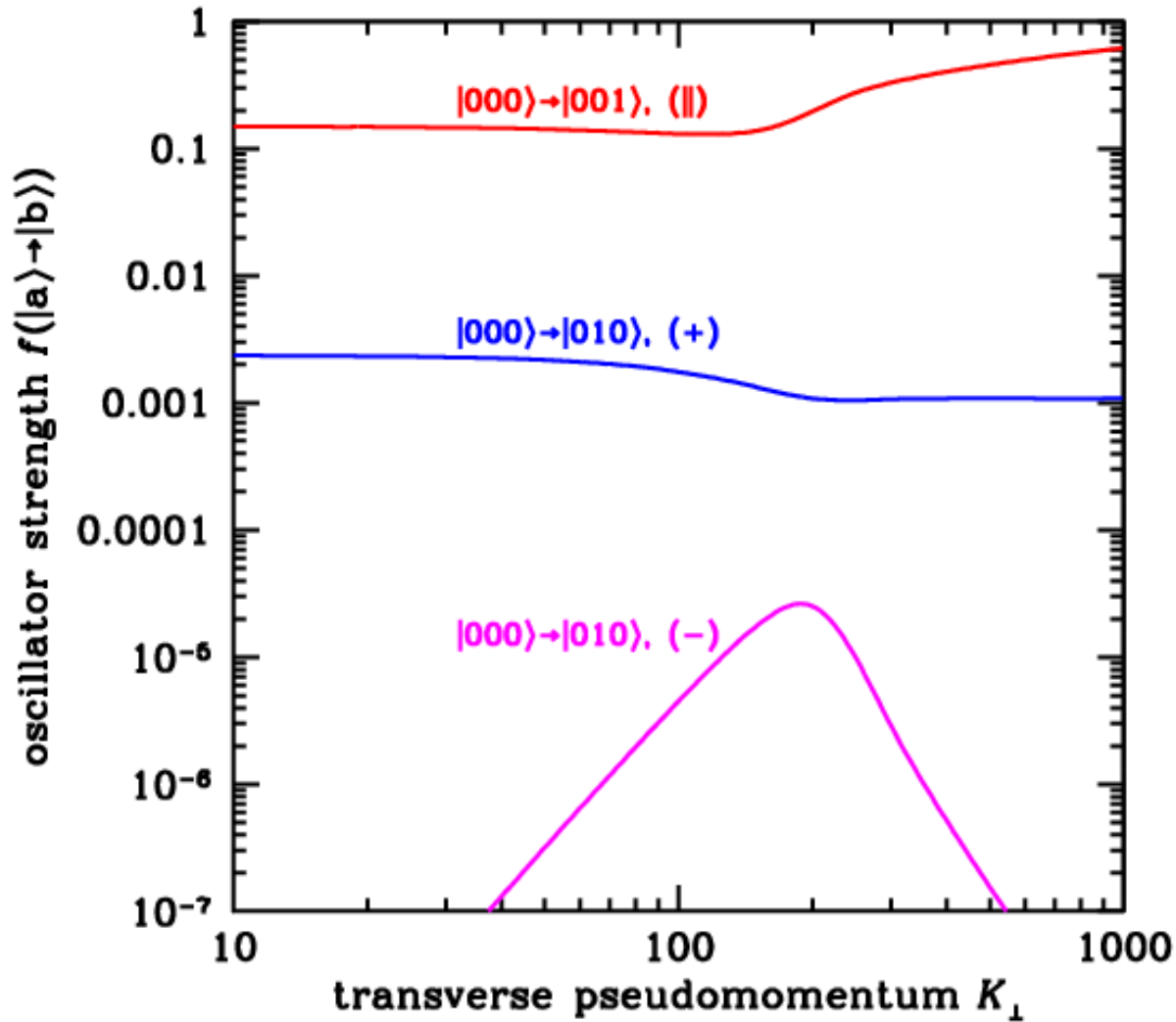
[Potekhin (1994) *J.Phys.B: At. Mol. Opt. Phys.* **27**, 1073]

# ***Ionization equilibrium and the equation of state of hydrogen in strong magnetic fields: the effects of nonideality and partial ionization***



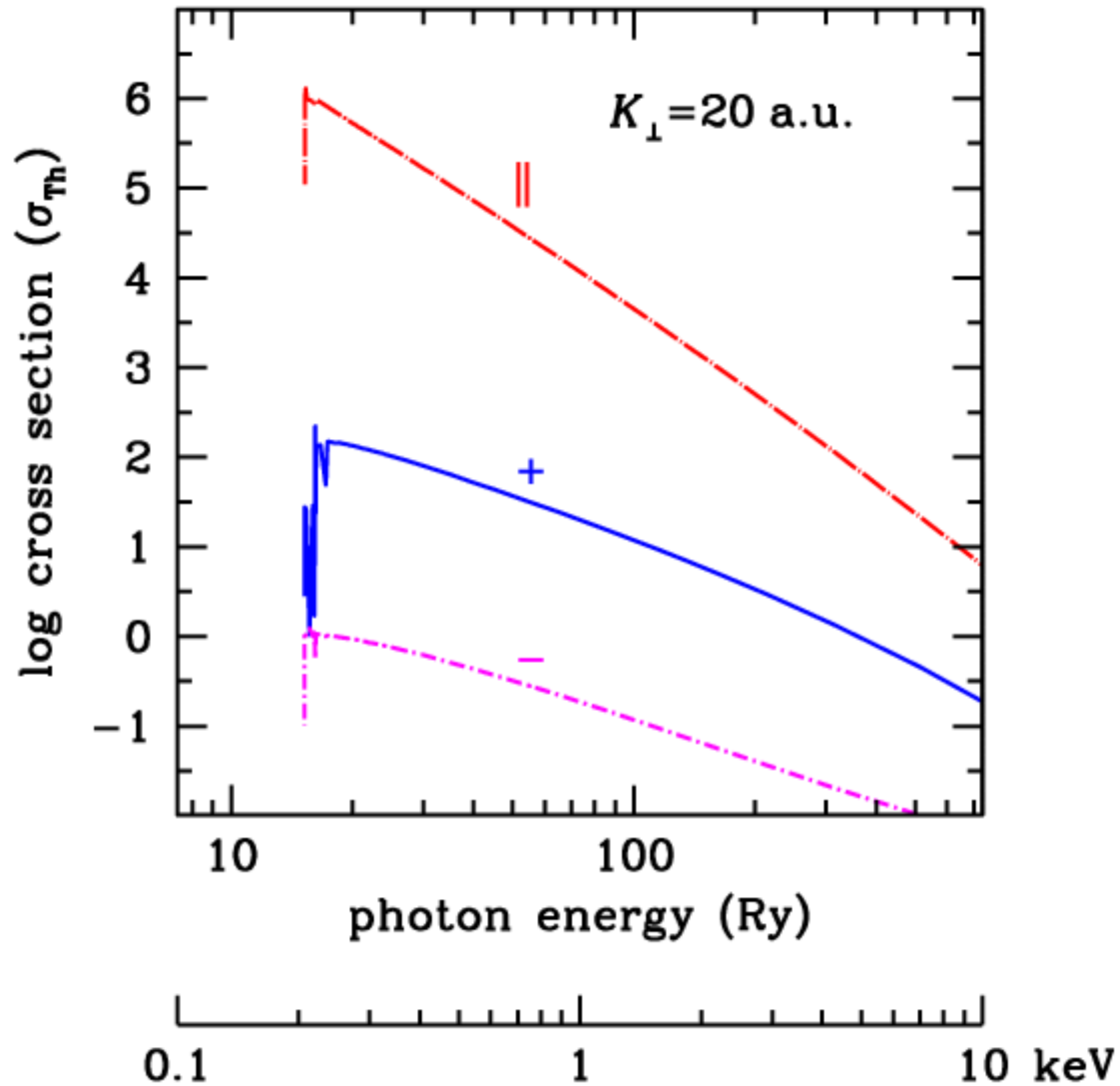
EOS of ideal (dotted lines) and nonideal (solid lines) H plasmas at various field strengths [Potekhin & Chabrier (2004) *Astrophys.J.* **600**, 317]

## Bound-bound transitions in strong magnetic field



Oscillator strengths for transitions between 2 levels of the hydrogen atom at  $B=2.35 \times 10^{12}$  G, as functions of pseudomomentum [Potekhin (1994) *J.Phys.B: At. Mol. Opt. Phys.* 27, 1073]

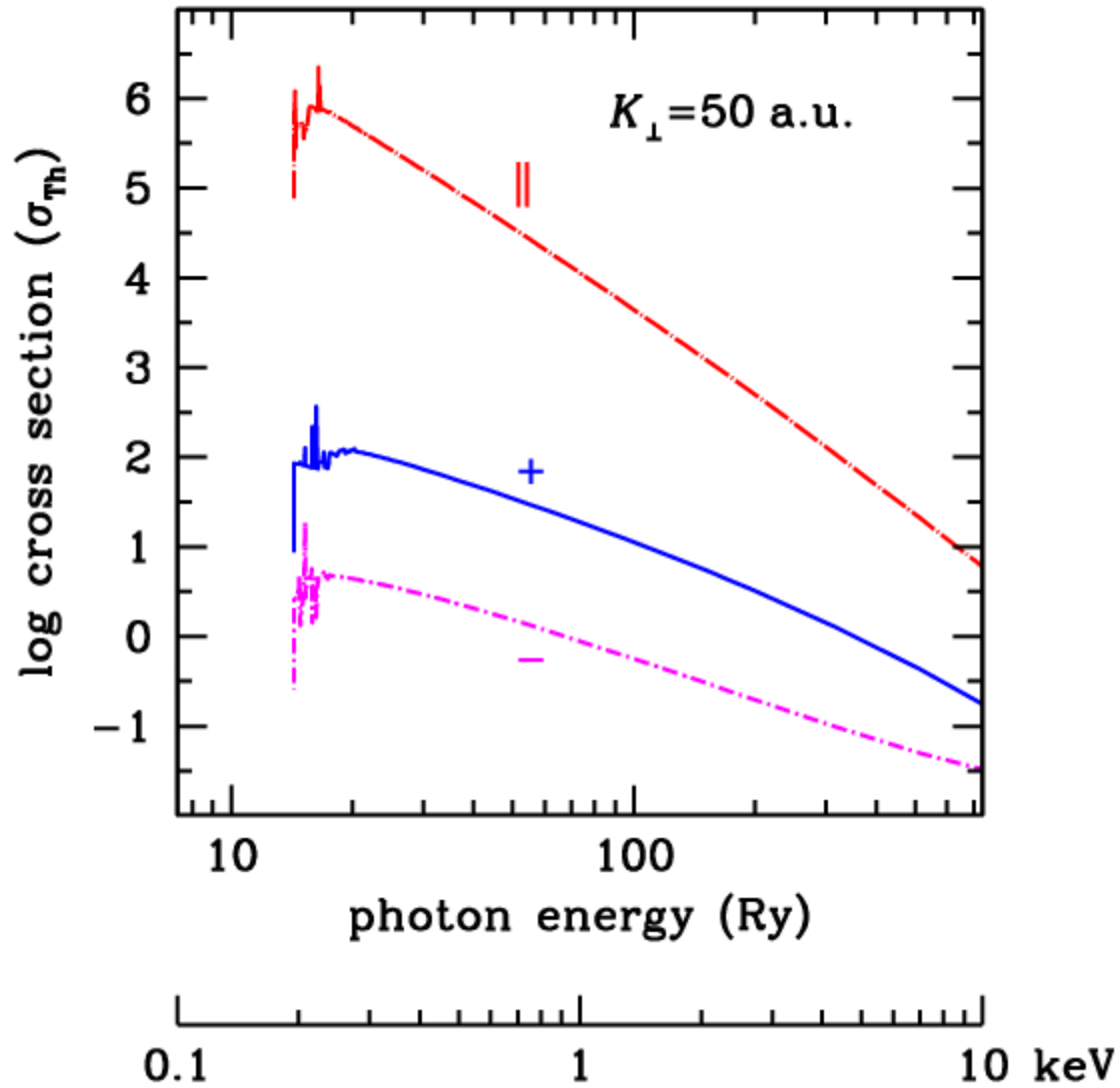
# Bound-free transitions in strong magnetic field



Photoionization cross sections for the ground-state H atom at  $B=2.35 \times 10^{12}$  G  
[Potekhin & Pavlov (1997) *Astrophys. J.* **483**, 414]

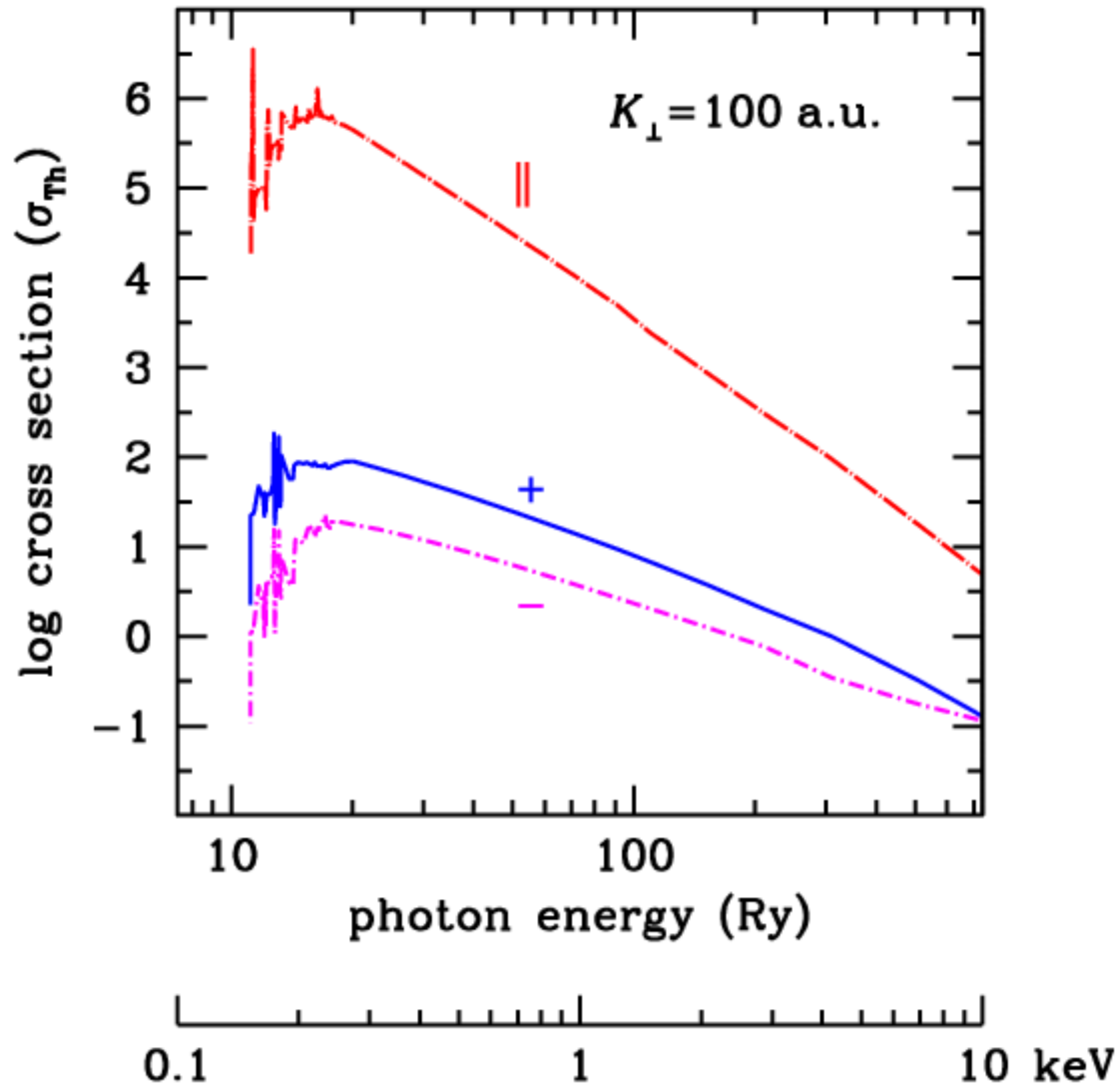


# Bound-free transitions in strong magnetic field



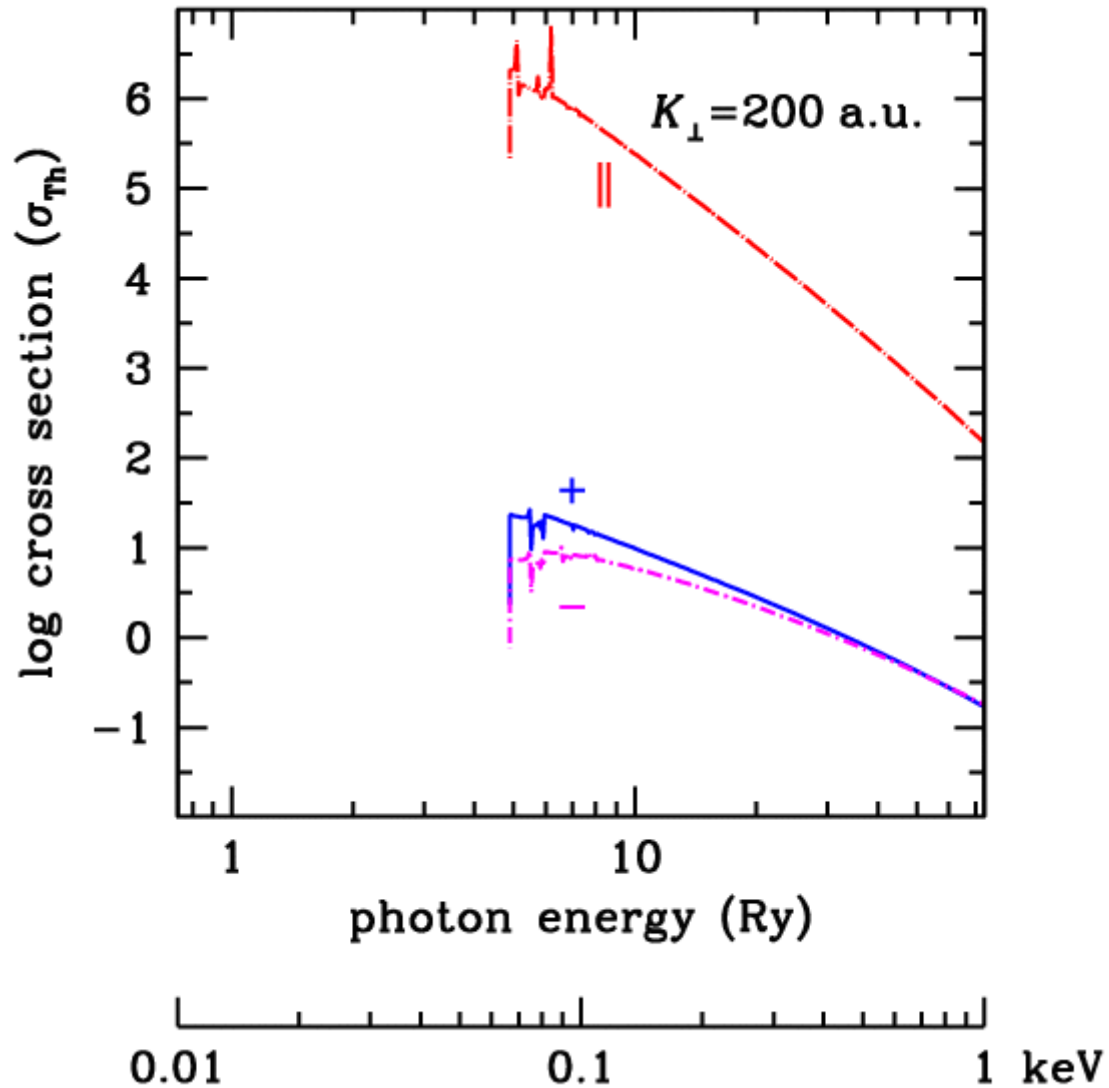
Photoionization cross sections for the ground-state H atom at  $B = 2.35 \times 10^{12} \text{ G}$   
[Potekhin & Pavlov (1997) *Astrophys. J.* **483**, 414]

# Bound-free transitions in strong magnetic field



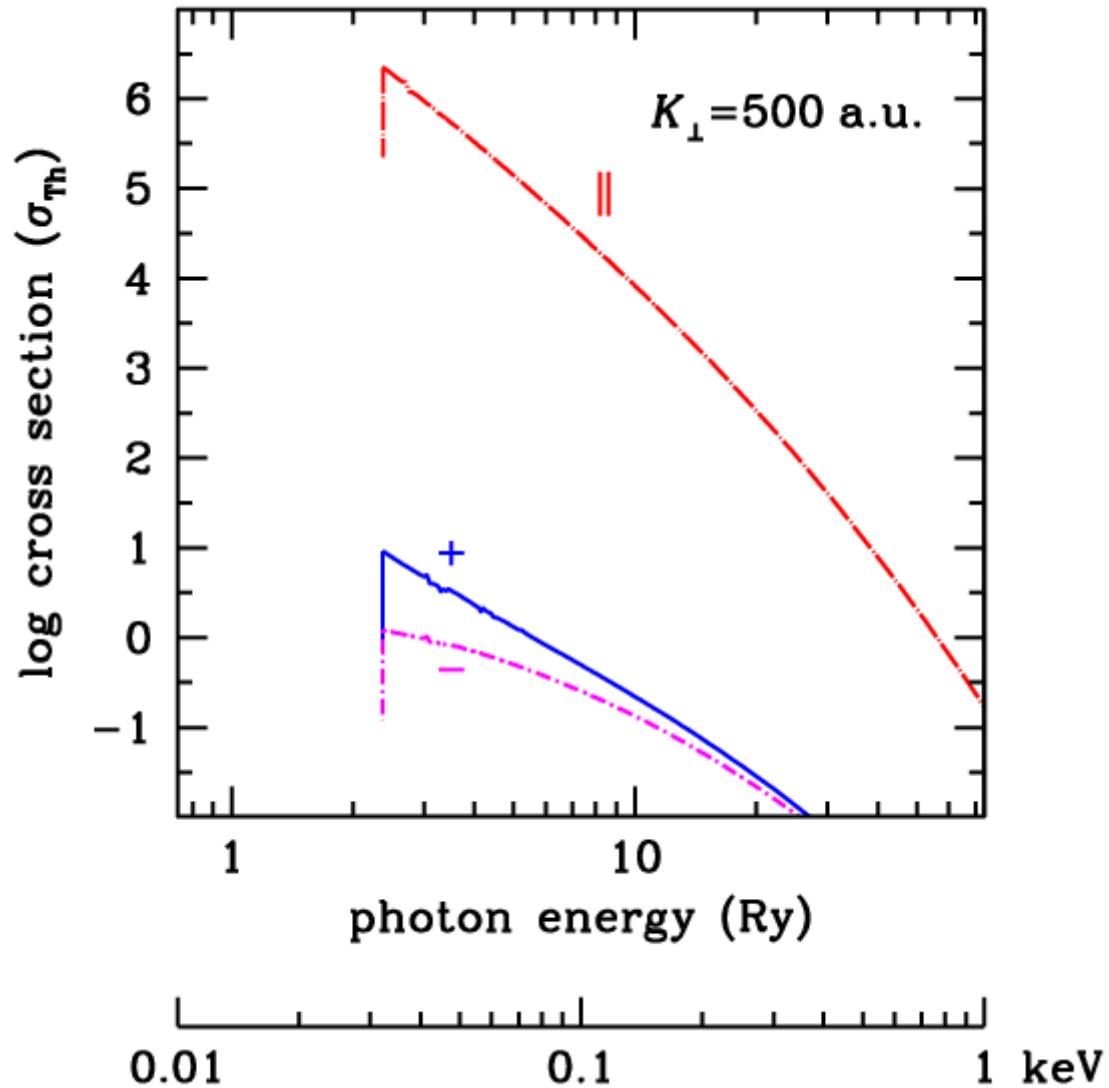
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# Bound-free transitions in strong magnetic field



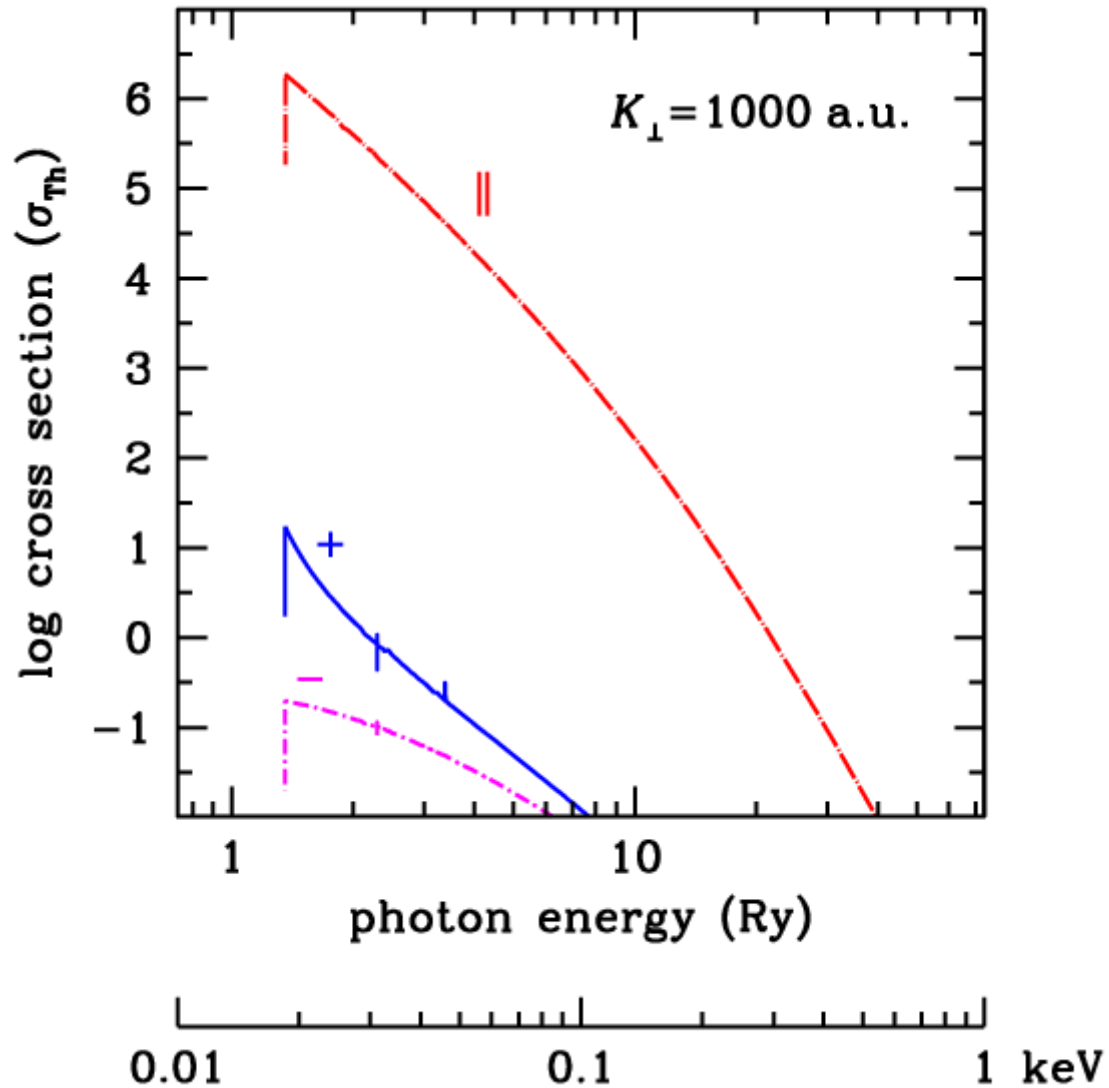
Photoionization cross sections for the ground-state H atom at  $B=2.35 \times 10^{12} \text{ G}$   
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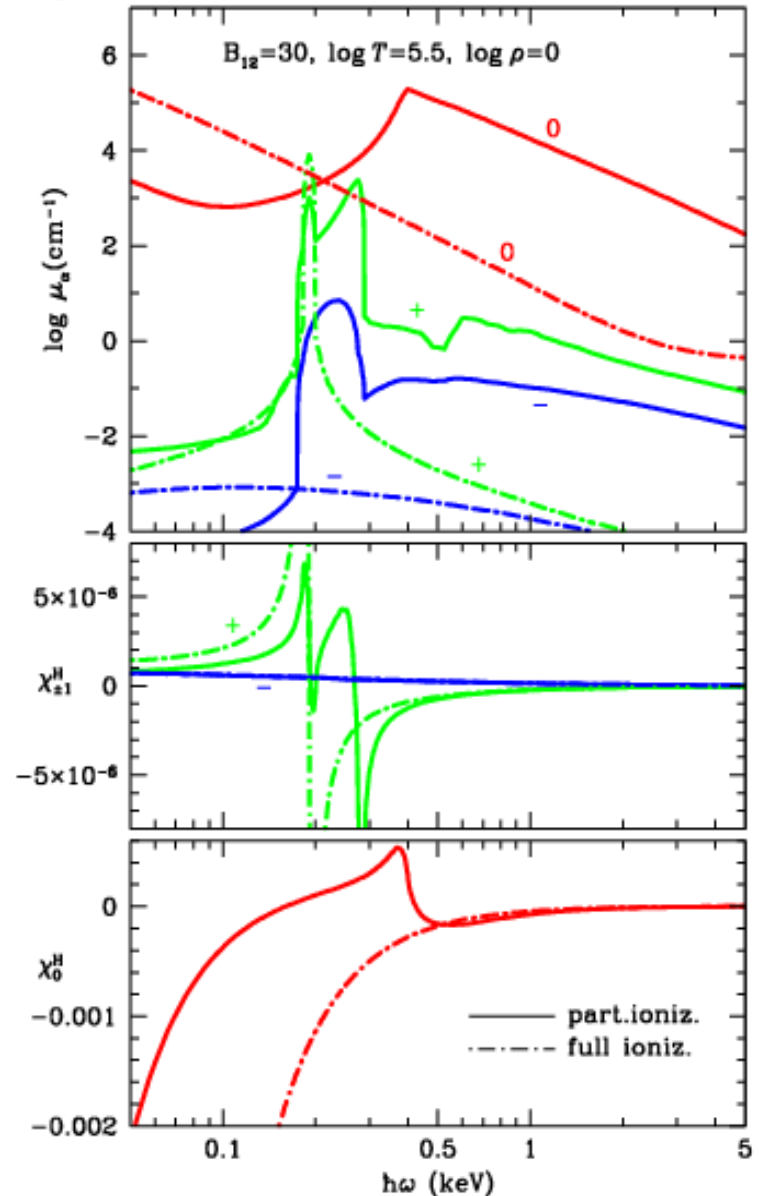
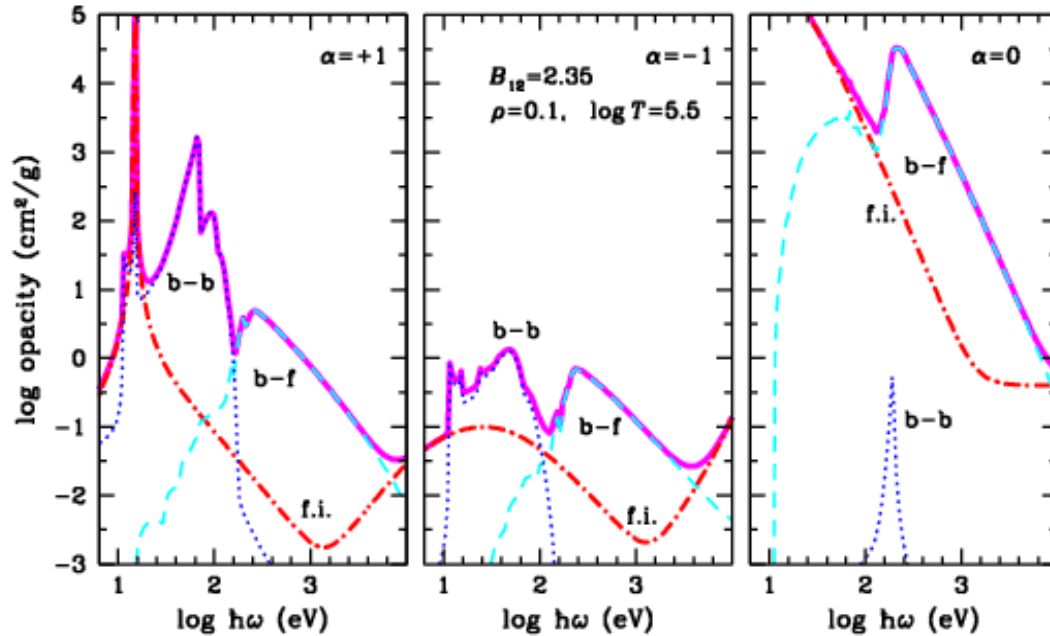


Photoionization cross sections for the ground-state H atom at  $B=2.35 \times 10^{12}$  G  
[Potekhin & Pavlov (1997) *Astrophys. J.* **483**, 414]

# Plasma absorption and polarizabilities in strong magnetic fields:

## The effects of nonideality and partial ionization

$$\kappa_j(\omega, \theta_B) = \sum_{\alpha=-1}^1 |e_{\alpha}^j(\omega, \theta_B)|^2 \hat{\kappa}_{\alpha}(\omega), \quad j = 1, 2 \text{ (X,O)}$$



Spectral opacities for 3 basic polarizations.

Solid lines – taking into account bound states,

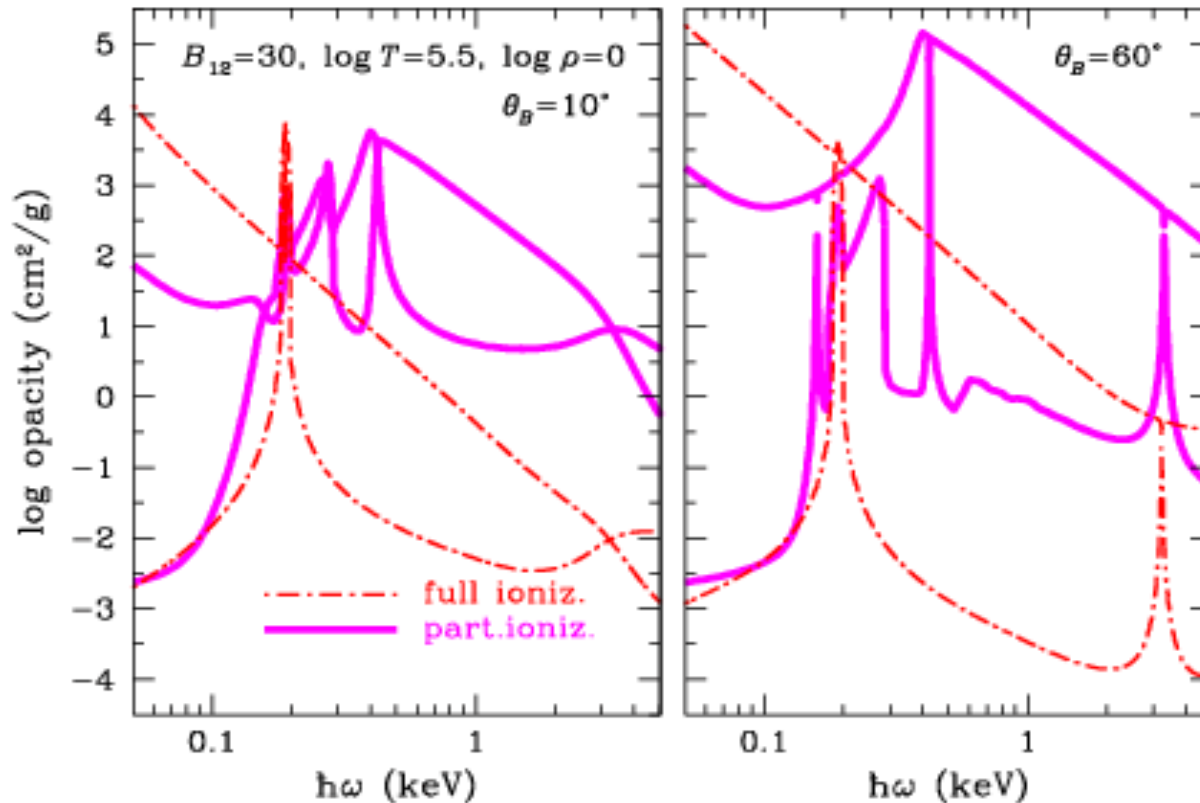
dot-dashes – full ionization

[Potekhin & Chabrier (2003) *ApJ* 585, 955]

To the right: *top panel* – basic components of the absorption coefficients; *middle and bottom* – components of the polarizability tensor

[Potekhin, Lai, Chabrier, & Ho (2004) *ApJ* 612, 1034]

# Opacities for normal modes in a strongly magnetized plasma: The effects of nonideality and partial ionization



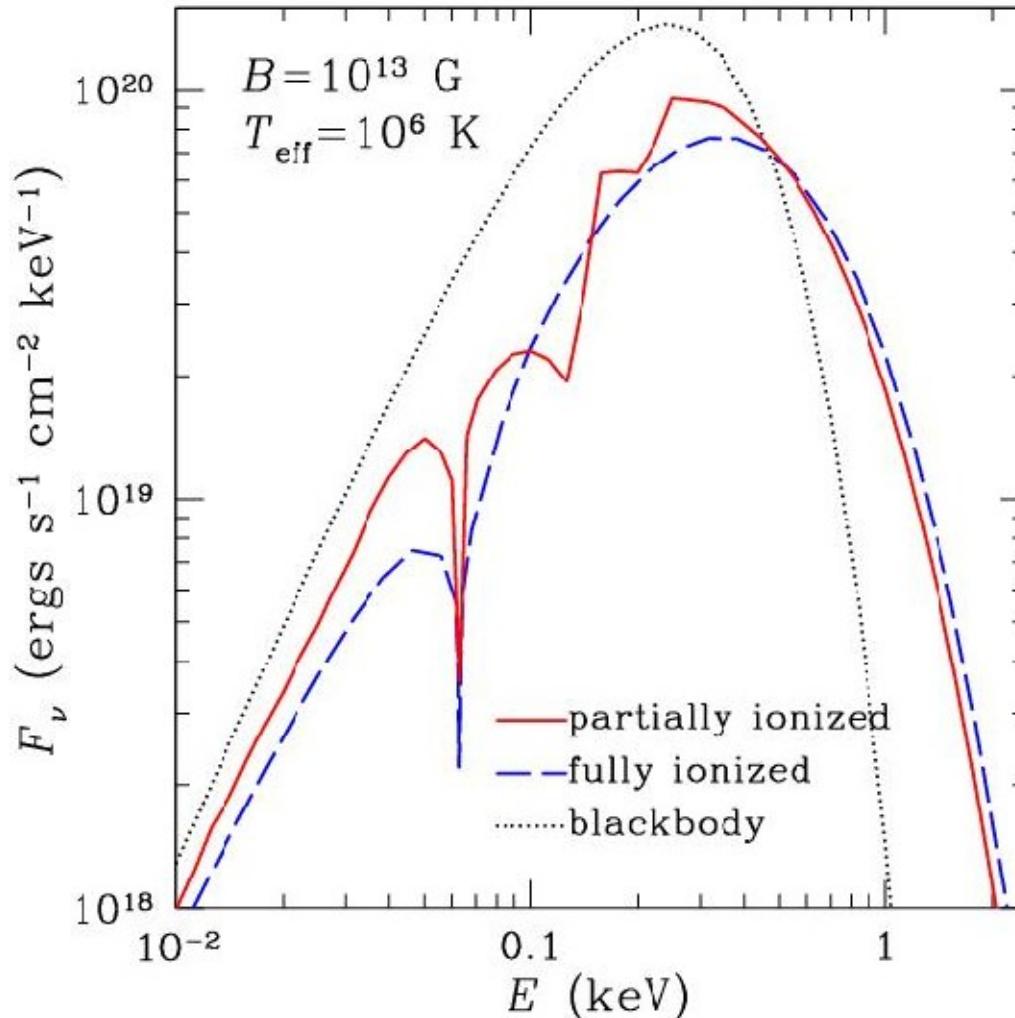
Opacities for two normal modes of electromagnetic radiation in models of an **ideal fully ionized (dash-dot)** and **nonideal partially ionized (solid lines)** plasma

at the magnetic field strength  $B=3 \times 10^{13}$  G, density 1 g/cc, and temperature  $3.16 \times 10^5$  K.

The 2 panels correspond to 2 different angles of propagation with respect to the magnetic field lines. An upper/lower curve of each type is for the extraordinary/ordinary polarization mode, respectively [Potekhin, Lai, Chabrier, & Ho (2004) *ApJ* **612**, 1034]

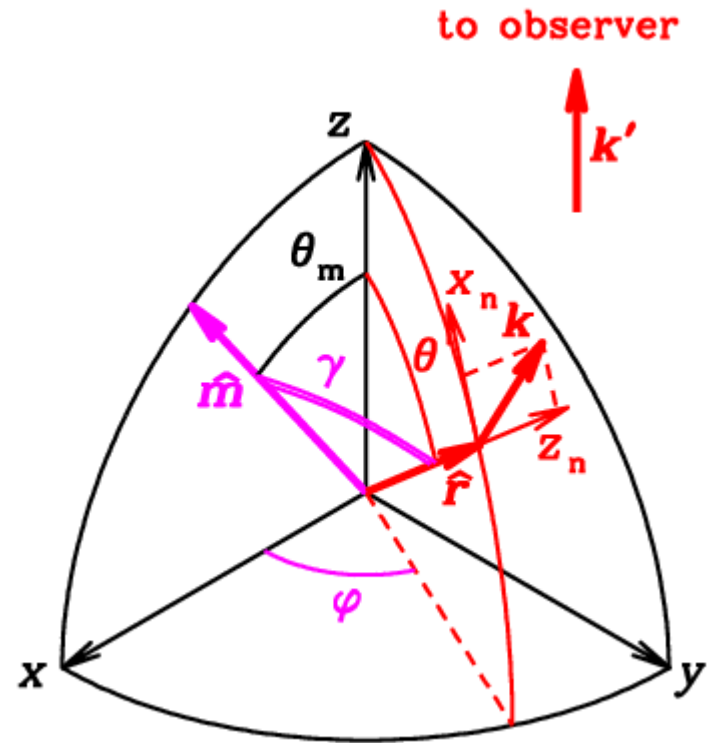
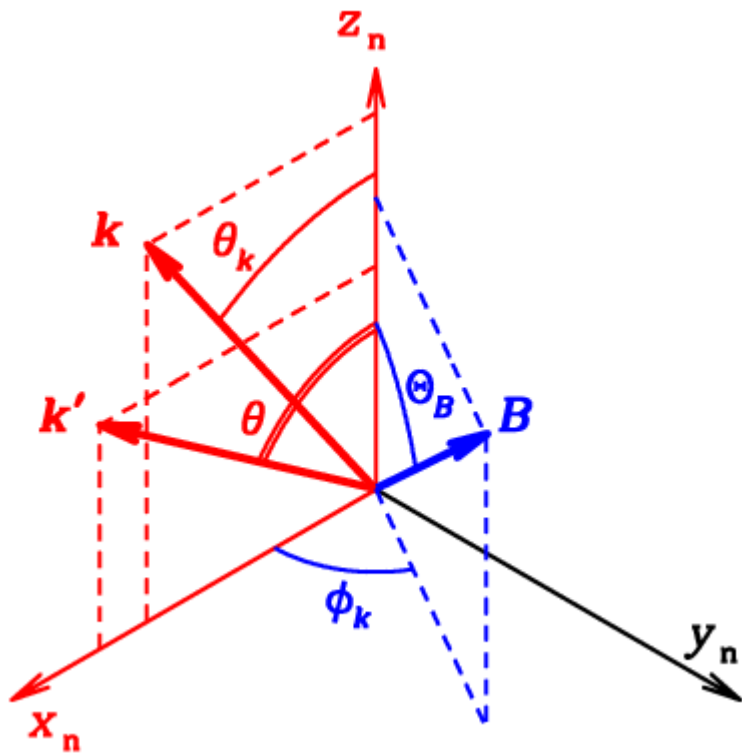
## Result: the spectrum

Potekhin, Lai, Chabrier, Ho,  
& van Adelsberg (2006)  
*J.Phys.A: Math. Gen* **39**, 4453



The effect of the atmosphere and its partial ionization on the spectrum of thermal radiation of a neutron star with  $B=10^{13}$  G,  $T=10^6$  K  
(the field is normal to the surface, the radiation flux is angle-averaged)





Parameters:  $T_{\text{eff}}$ ,  $B$ ,  $g$ ,  $\theta_k$ ,  $\phi_k$ ,  $\theta_B$

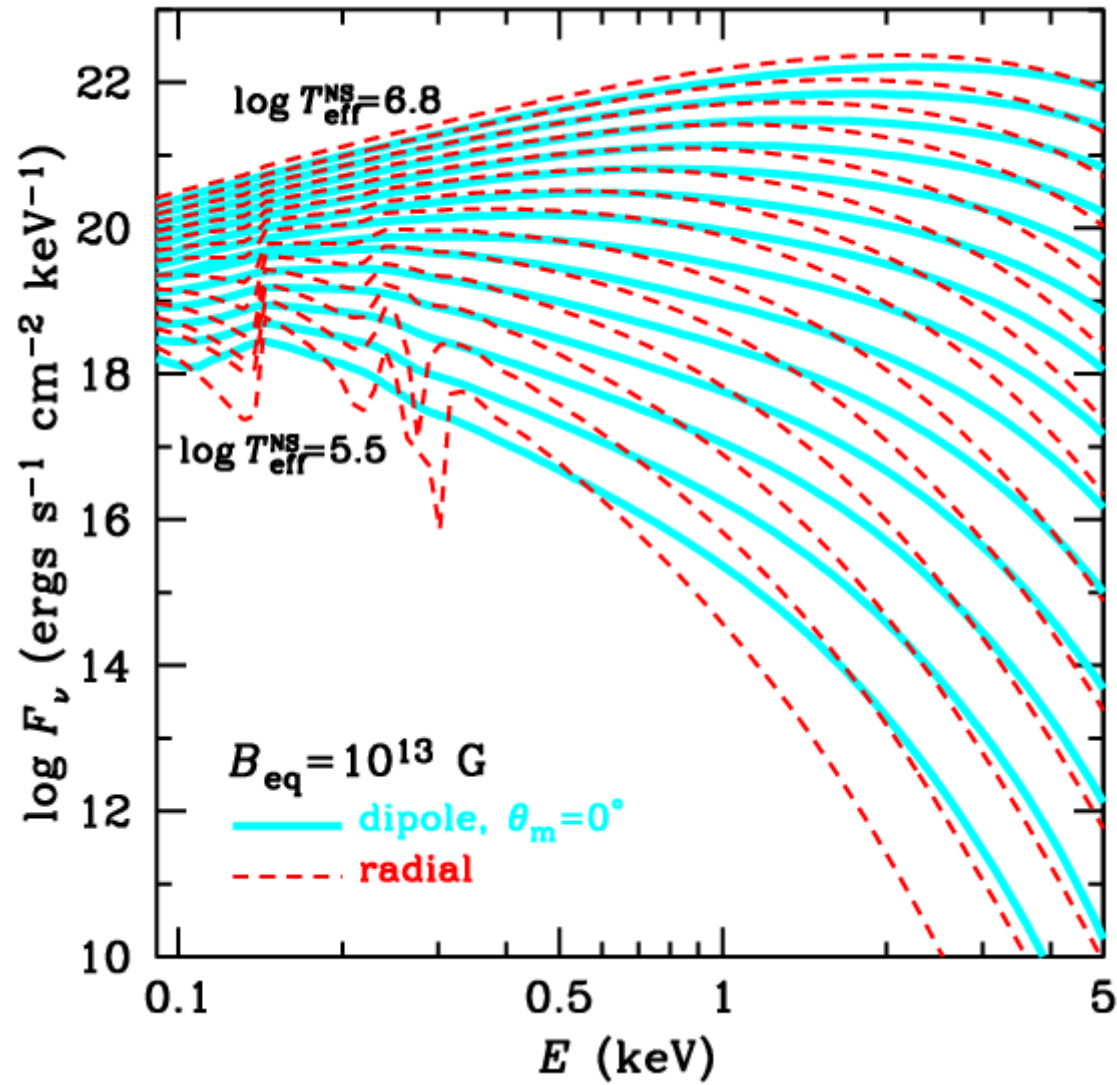
Pavlov & Zavlin (2000):

$$\theta = a \int_0^u \frac{dx}{\sqrt{1 - a^2(1-x)x^2}} \quad \text{for } \theta \leq \pi \quad (z_g \leq 0.54)$$

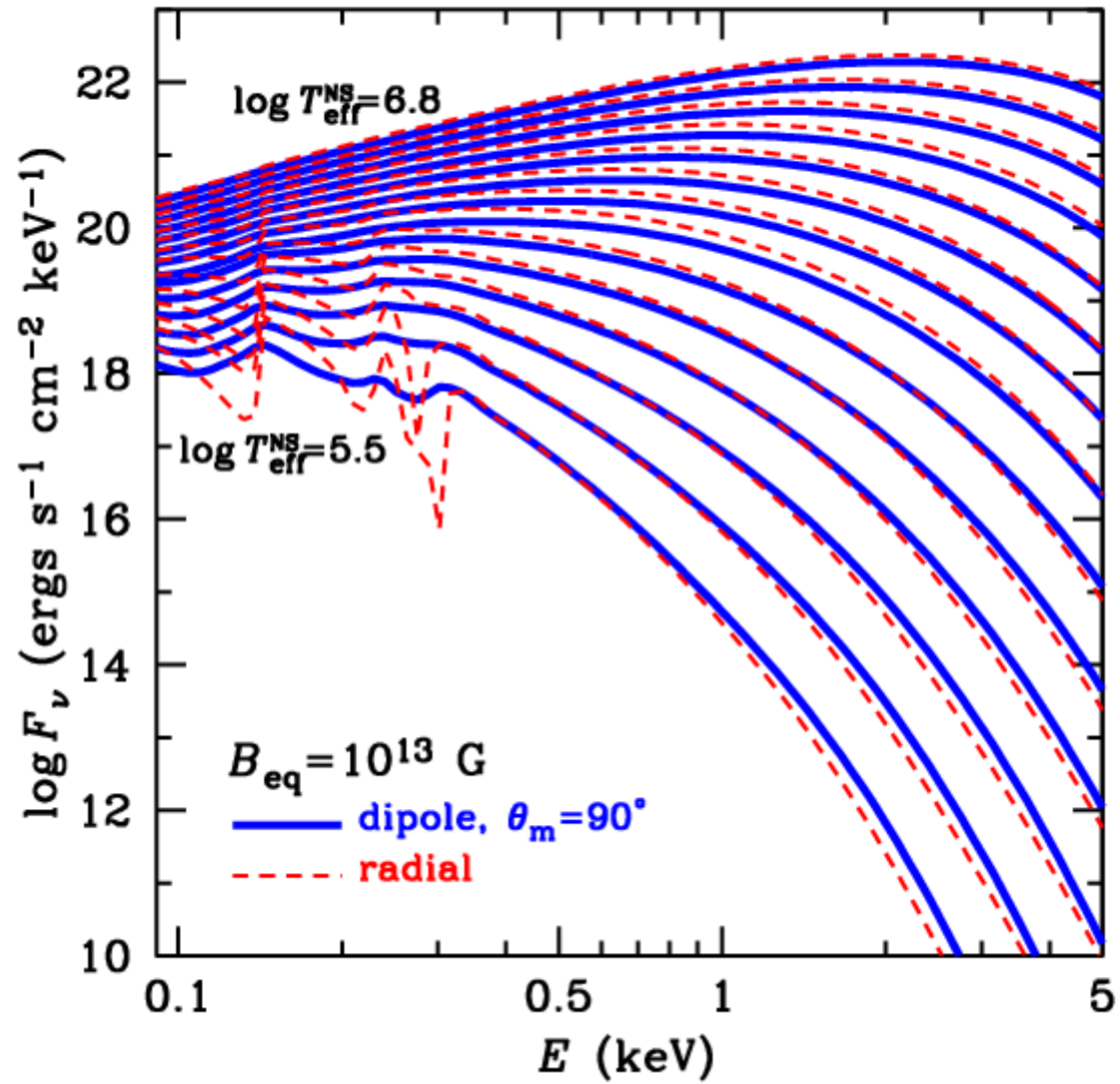
$$a = u(1 + z_g) \sin \theta_k \quad u \equiv \frac{r_g}{R}$$

Beloborodov (2002):  $1 - \cos \theta \approx \frac{1 - \cos \theta_k}{1 - u}$

## Result of modelling: spectra, dipole model

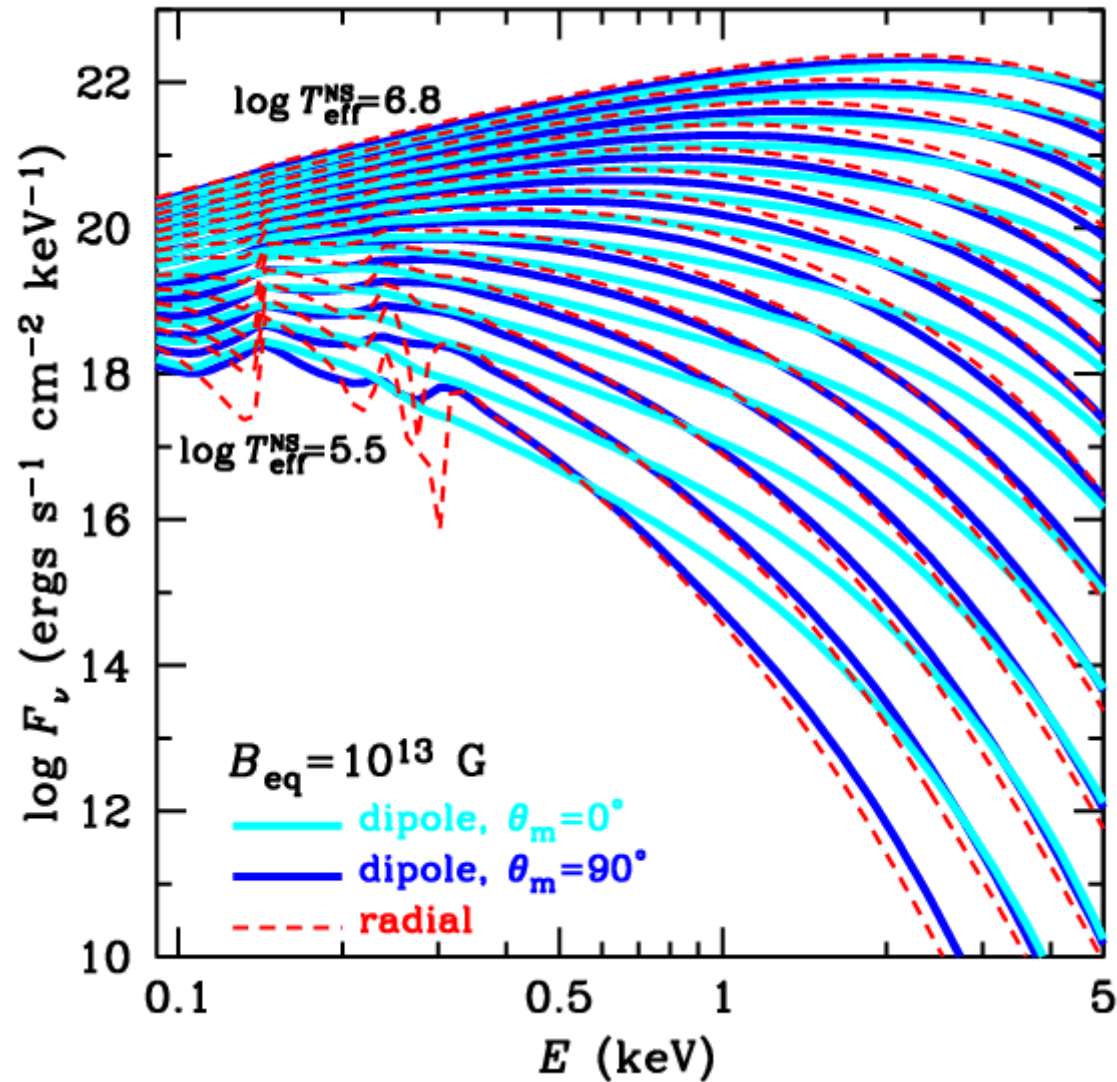


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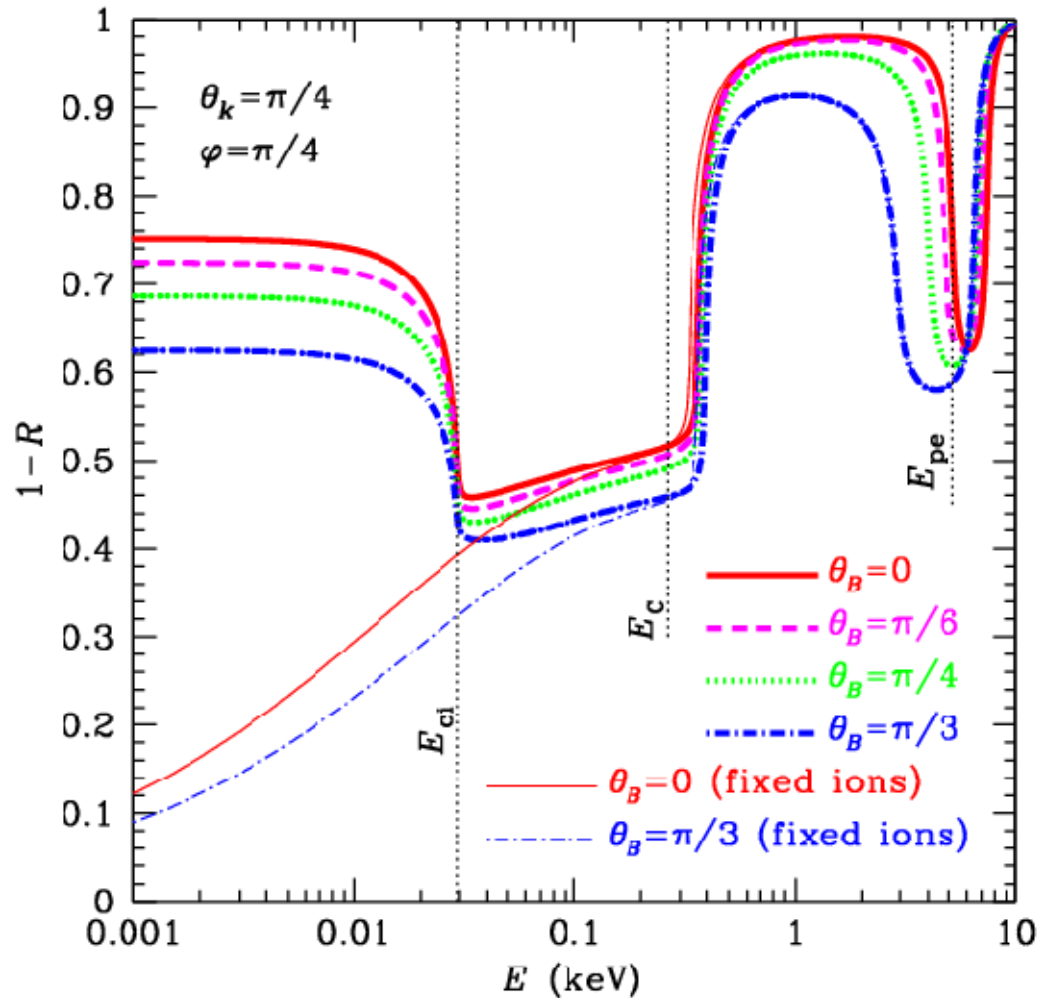
Ho, Potekhin, & Chabrier  
(2008) *ApJS* 178, 102



Spectral features are smoothed by surface field distribution.

XSPEC: NSMAX – <http://heasarc.gsfc.nasa.gov/docs/xanadu/xspec/models/nsmax.html>

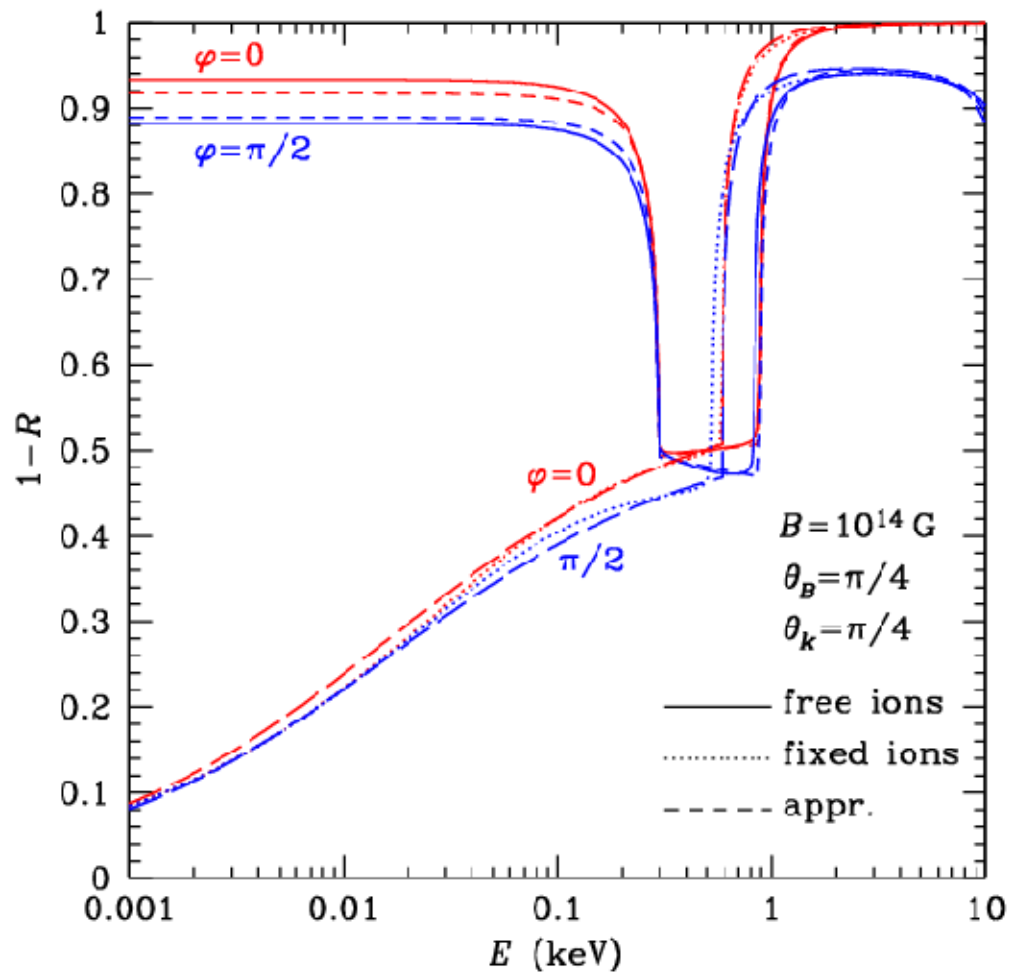
# Radiation from condensed surface



Dimensionless emissivity of iron surface as function of photon energy at  $B=10^{13}$  G.

Method of M. van Adelsberg, D. Lai, et al. (2005) *ApJ* 628, 902; improved in 2011.

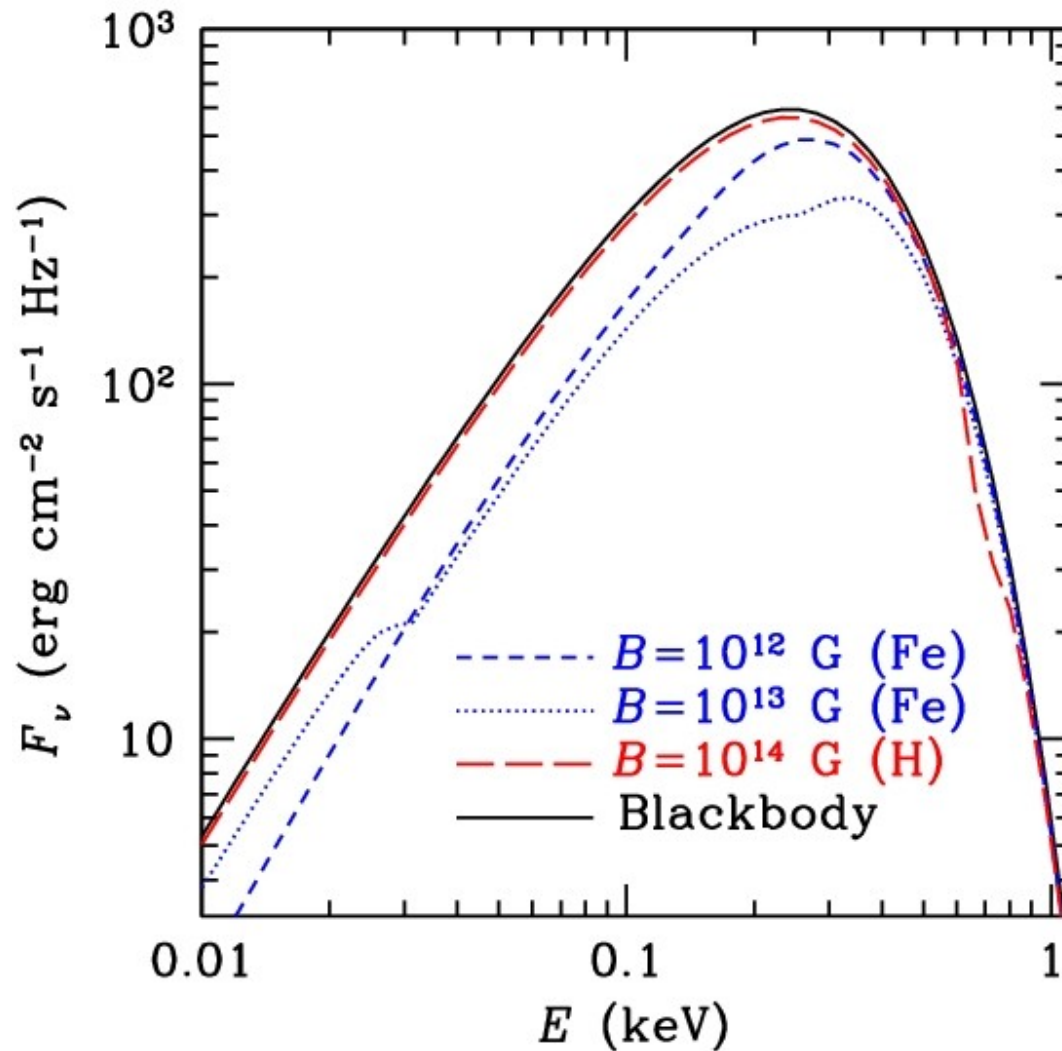
## Radiation from condensed surface



Dimensionless emissivity of iron surface as function of photon energy at  $B=10^{13}$  G.

Method of M. van Adelsberg, D. Lai, et al. (2005) *ApJ* **628**, 902; improved in 2011. Numerical results **and fit**.

## Radiation from condensed surface



Monochromatic flux from the condensed surface in various cases

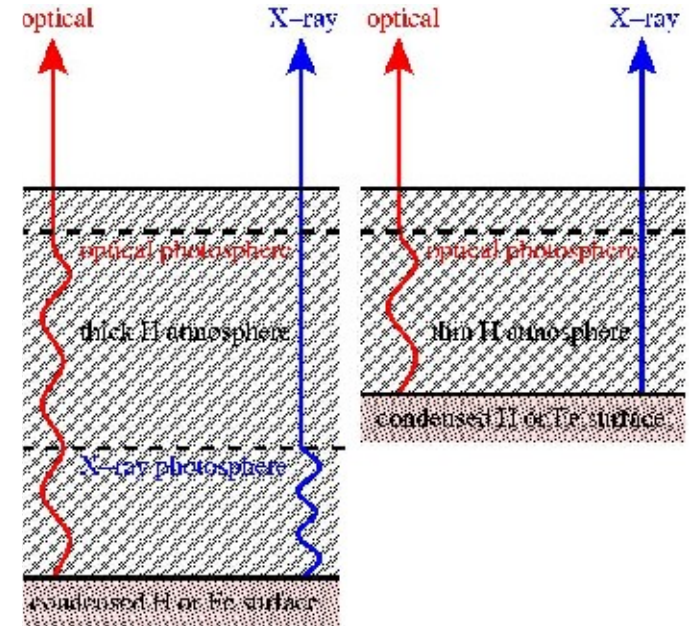
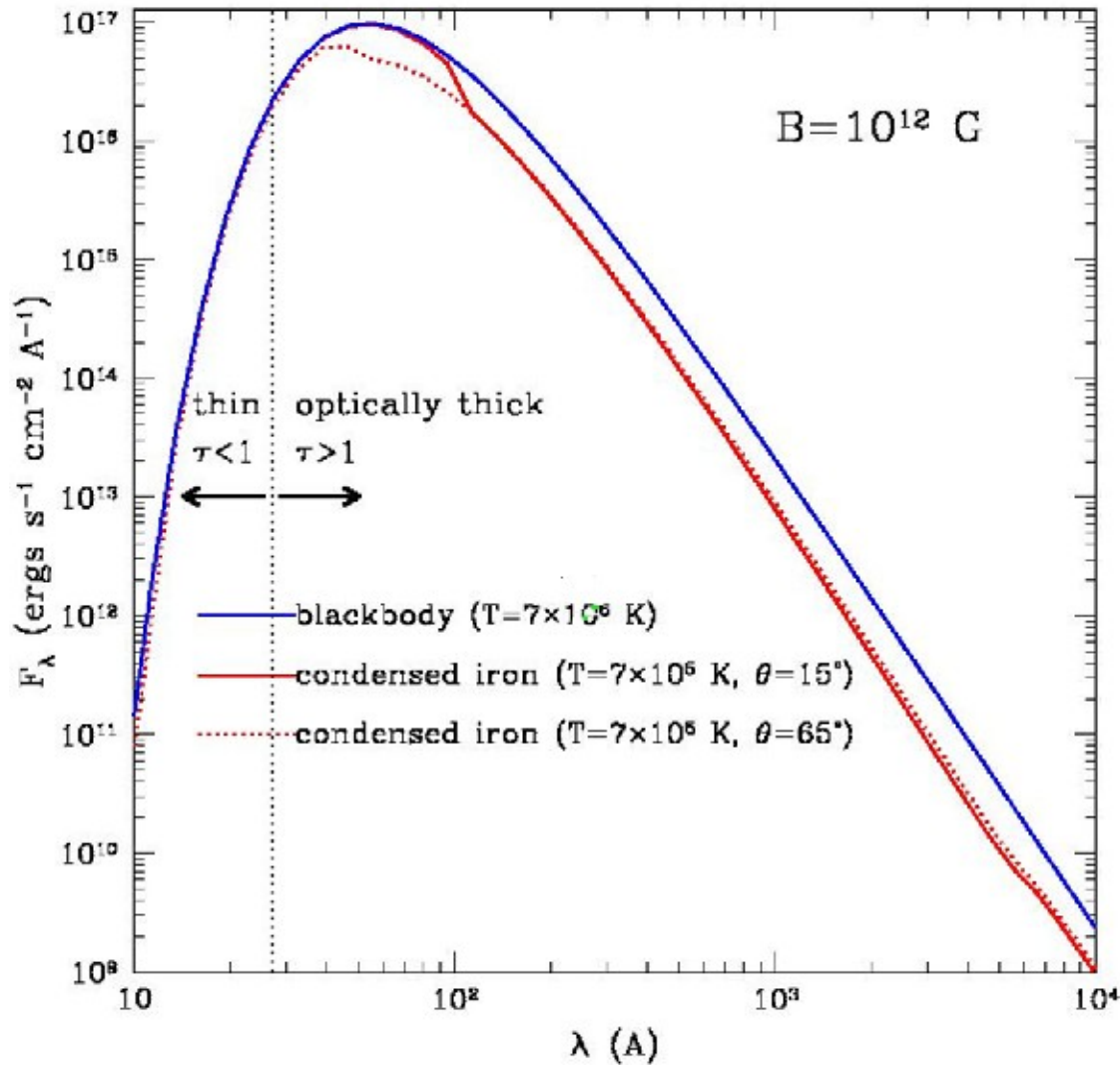
[Matt van Adelsberg, for Potekhin *et al.* (2006) *J.Phys.A: Math. Gen.* **39**, 4453]

# “Thin atmospheres”

= condensed surface covered by an atmosphere, so that neither is negligible

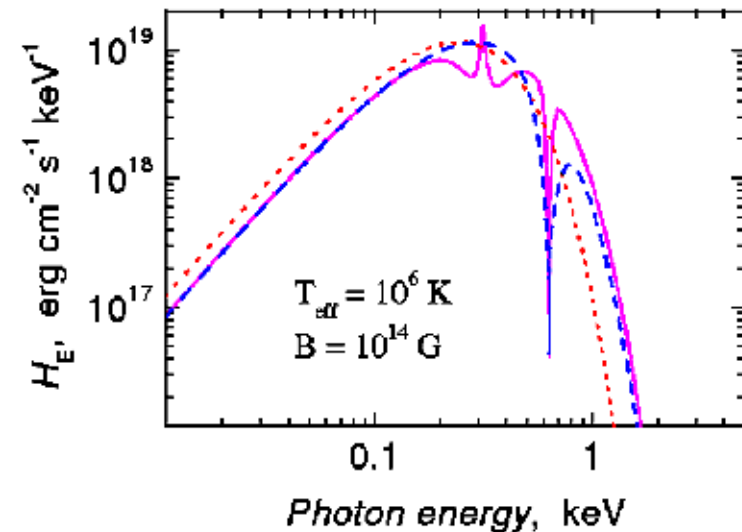
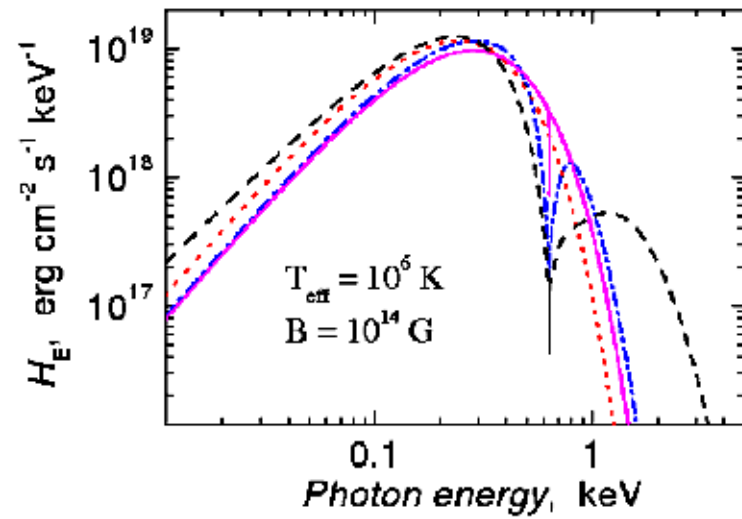
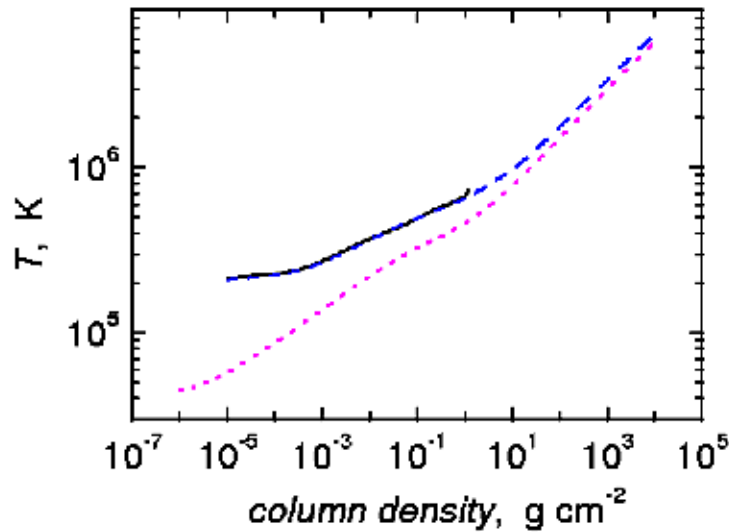
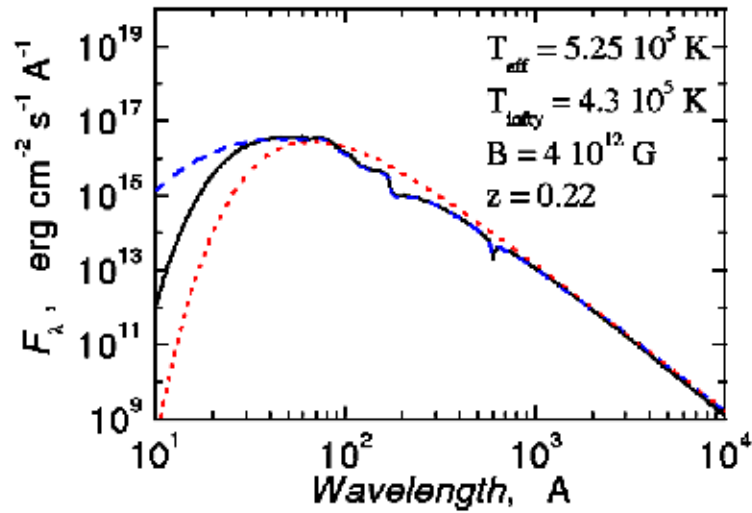
Idea by Motch, Zavlin, & Haberl (2003);

realized by Wynn Ho (2004 – 2007) and by Valery Suleimanov (2008 – 2011) with coauthors





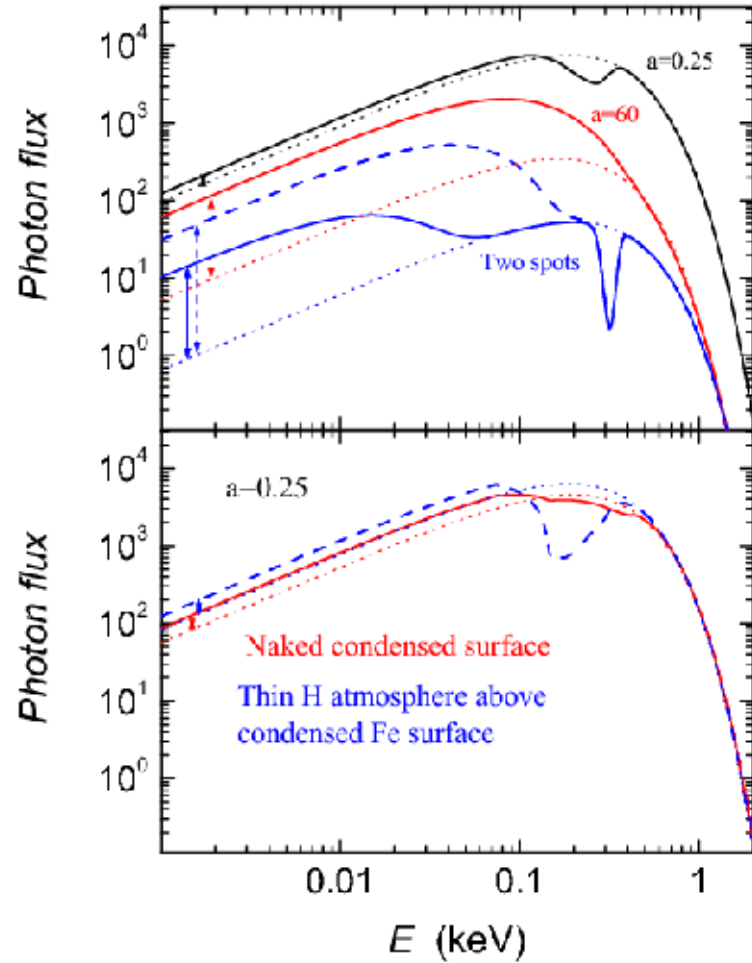
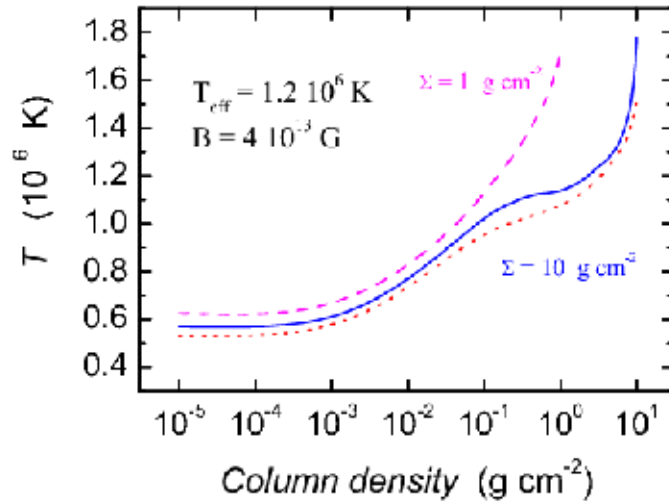
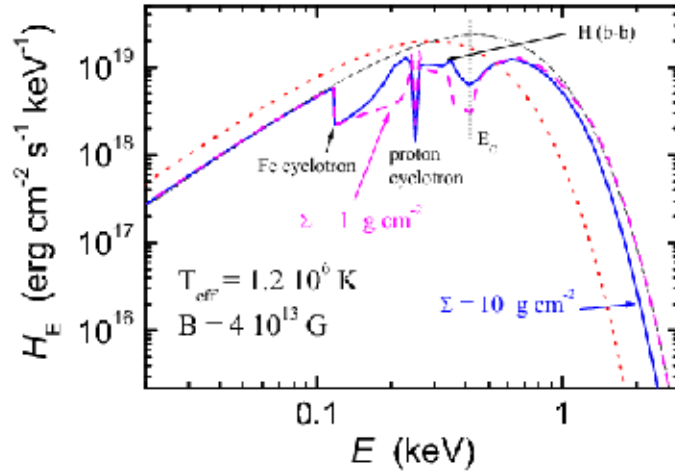
## Thin and layered atmospheres



Emergent spectra (top) and temperature profiles (bottom) for partially ionized H atmospheres: semi-infinite (dashed line) or thin (column density 1.2 g cm<sup>-2</sup>) atmospheres vs. fully ionized model (dotted)

Emergent spectra of fully ionized atmospheres. Top – H (semi-infinite – dashes, 100 g cm<sup>-2</sup> – dot-dash, 1 g cm<sup>-2</sup> – solid); bottom – H/He (25/75 g cm<sup>-2</sup>). Dotted lines – blackbody.

# Thin atmospheres: approximate formulae

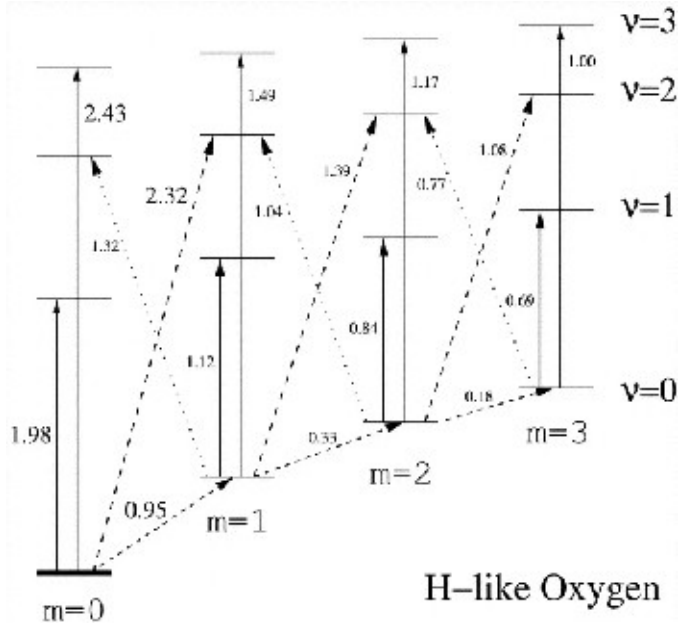


Emergent spectra (top) and temperature profiles (bottom) of thin partially ionized H atmospheres

Integral spectra for different models, compared with the BB spectra that fit the model at  $E > 0.5$  keV

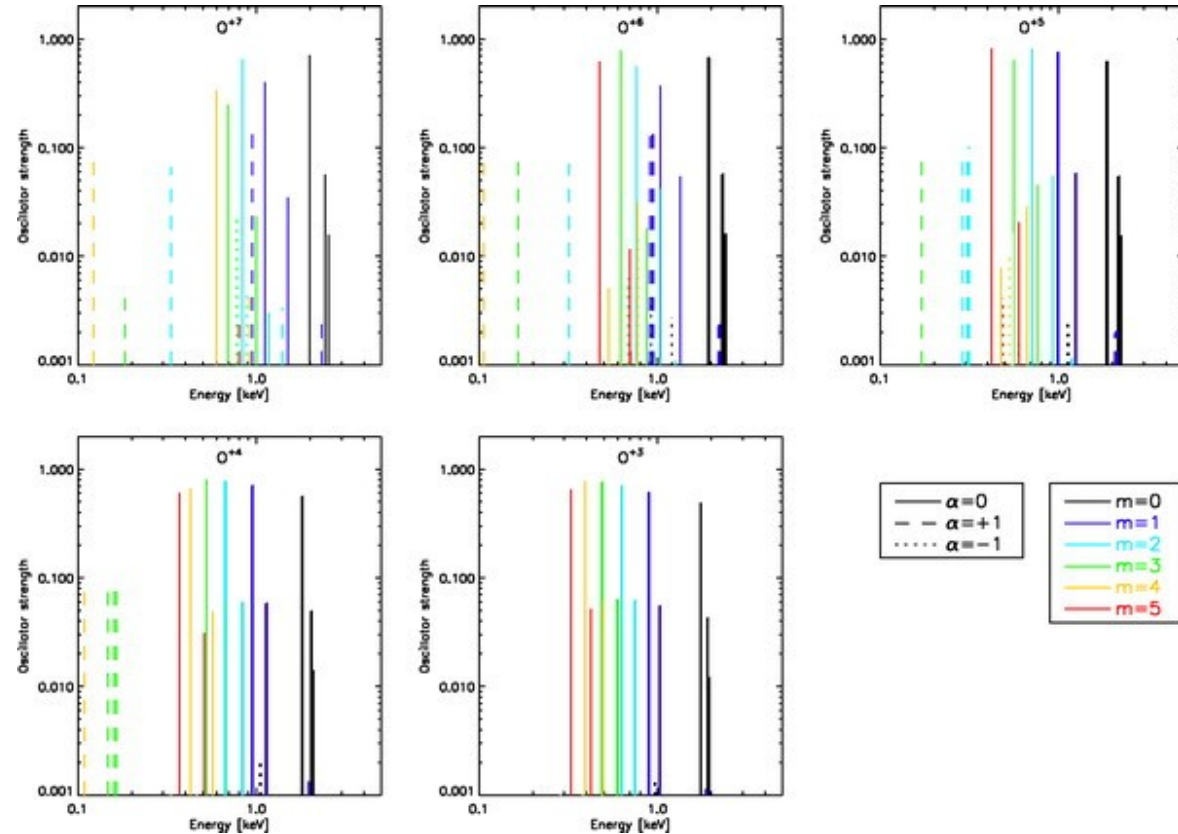
# Atmosphere models for heavier elements

K.Mori, C.Hailey (2006) *ApJ* 648, 1139



H-like Oxygen

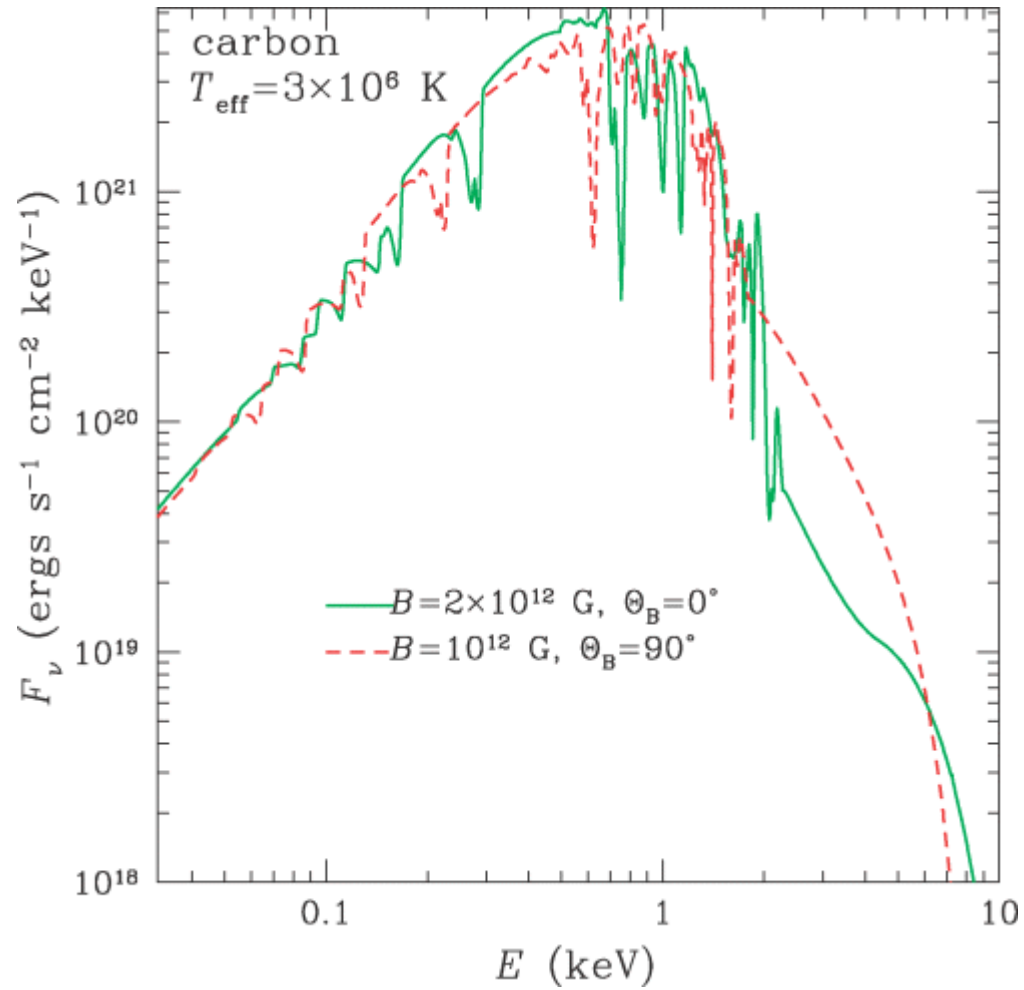
Energies of allowed transitions from the ground state, at  $B=10^{12}$  G



Energies and oscillator strengths of allowed transitions from the various tightly bound states

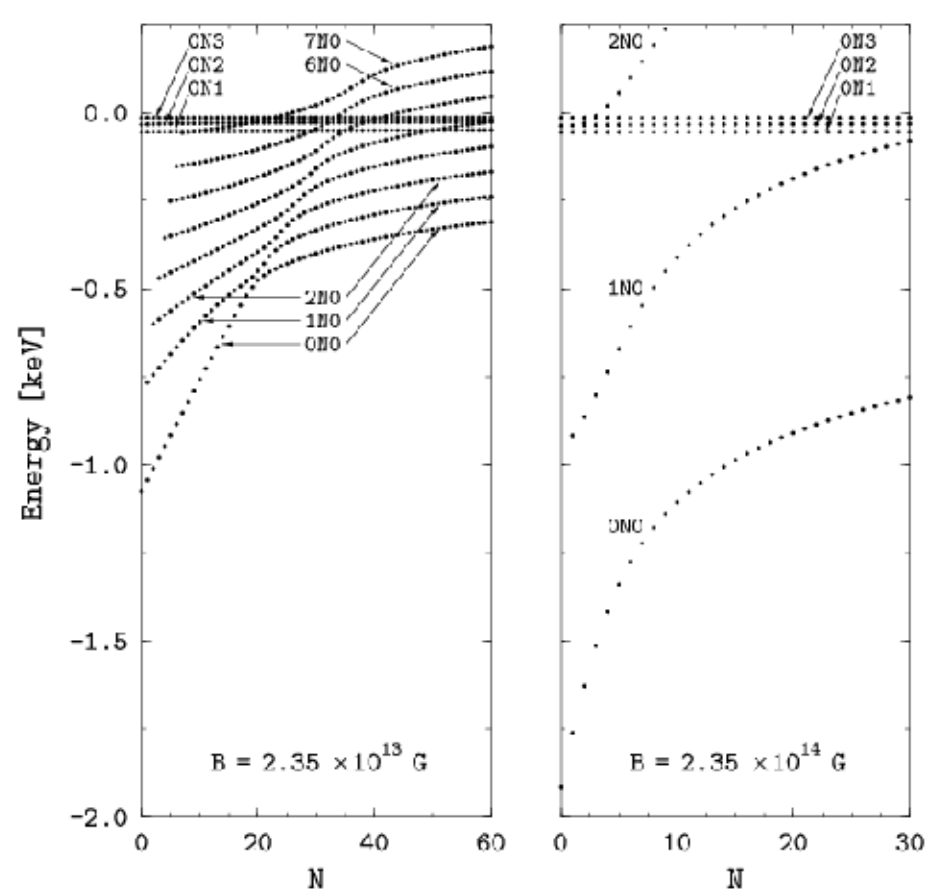
# Atmosphere models for heavier elements

K.Mori & W.C.G.Ho (2007) *MNRAS* 377, 905

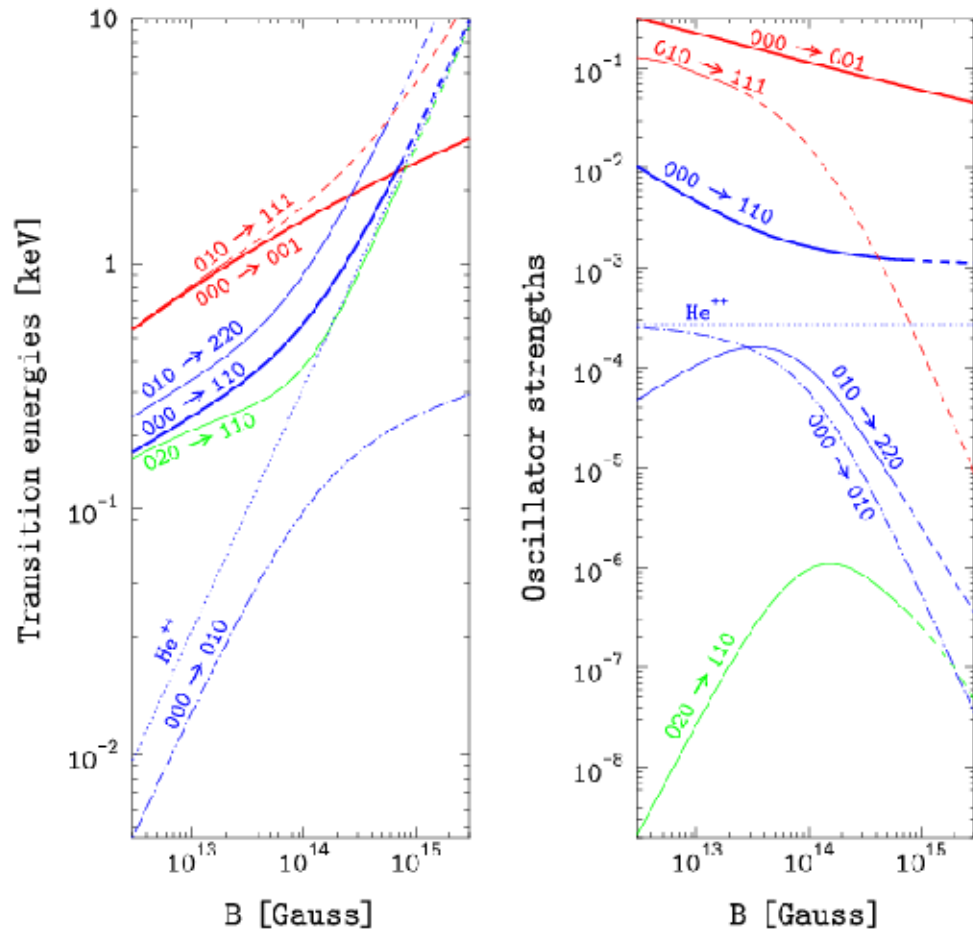


# Helium ion moving in a strong magnetic field

G.G.Pavlov & V.G.Bezchastnov (2005) *ApJ* 635, L61



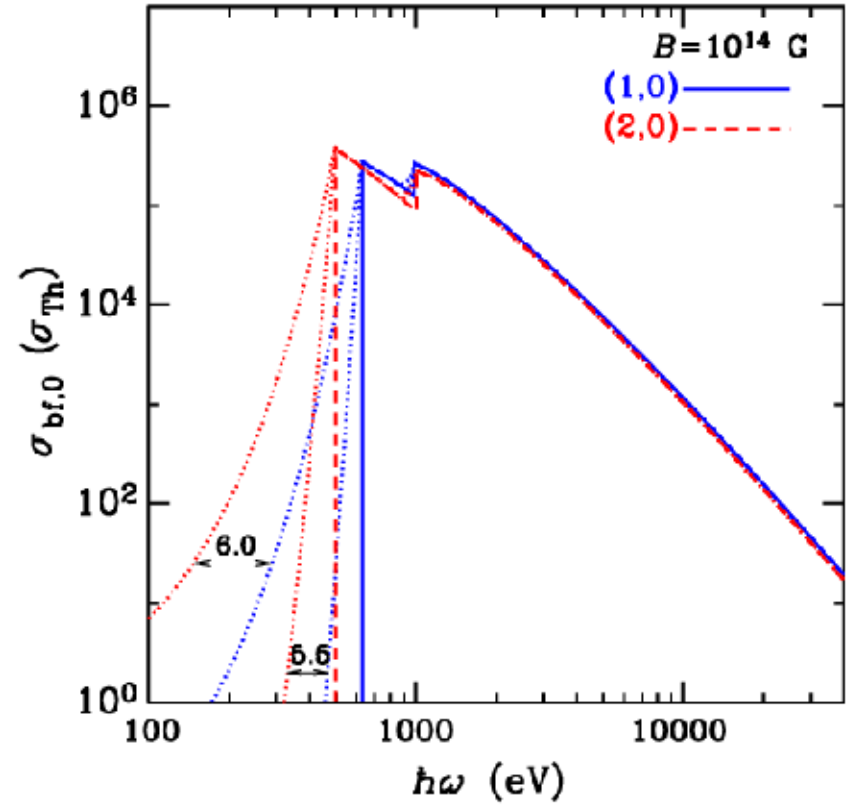
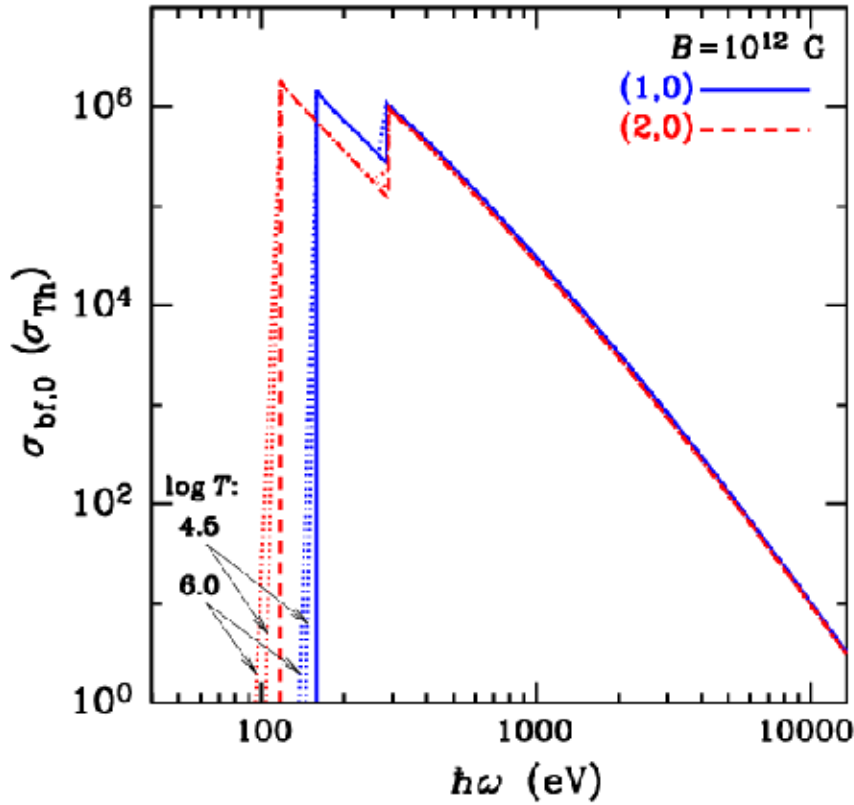
Energies of the ion as functions of  $N$ , which characterizes the state of motion across the magnetic field



Transition energies and oscillator strengths as functions of  $B$

# Helium atom: photoionization

Z.Medin, D.Lai, A.Y.Potekhin (2008) *MNRAS* 383, 161



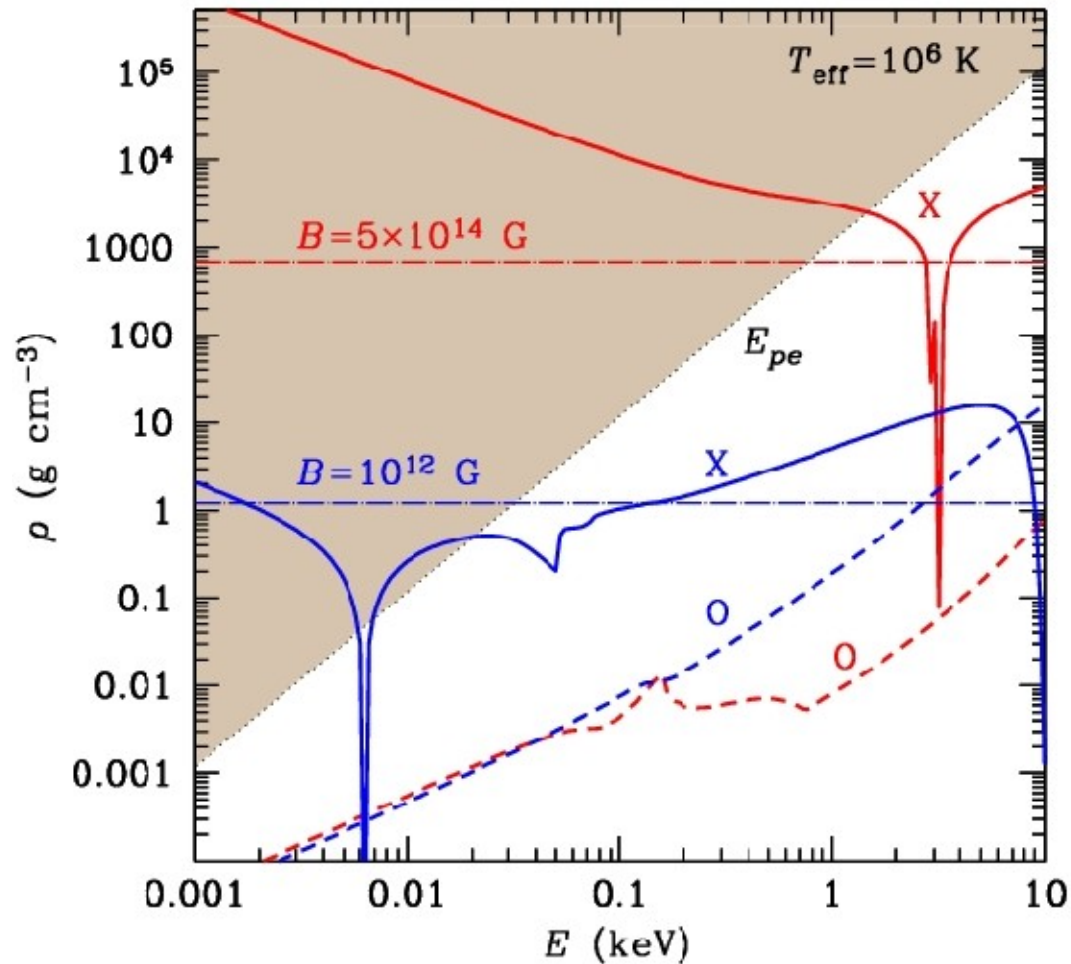
Photoionization cross sections for polarization along  $B$  without (solid and dashed lines) and with (dots) account of magnetic broadening.

$$\sigma(\omega) \approx \sigma(\omega_{\text{thr}}) \exp \left[ -\frac{M_{\perp} \omega_{\text{thr}} - \omega}{M \Omega_c} - \frac{\hbar(\omega_{\text{thr}} - \omega)}{k_B T} \right]$$

## Challenges from superstrong fields

1. *Mechanical structure: field affects EOS*
2. *Thermal structure: field affects luminosity*
3. *Non-isotropic heat transport in the inner crust*
4. *Surface layers: molecules, chains, and magnetic condensation*
5. *Nonperturbative finite-mass effects for bound species*
6. *Radiative transfer: vacuum polarization and mode conversion*
7. *Energy transport below the plasma frequency*

## Energy transport below the plasma frequency can be especially important for superstrong fields



Photon-decoupling densities for X- and O-modes for a partially ionized H atmosphere, for magnetic field strengths typical of pulsars (blue lines) and magnetars (red lines).

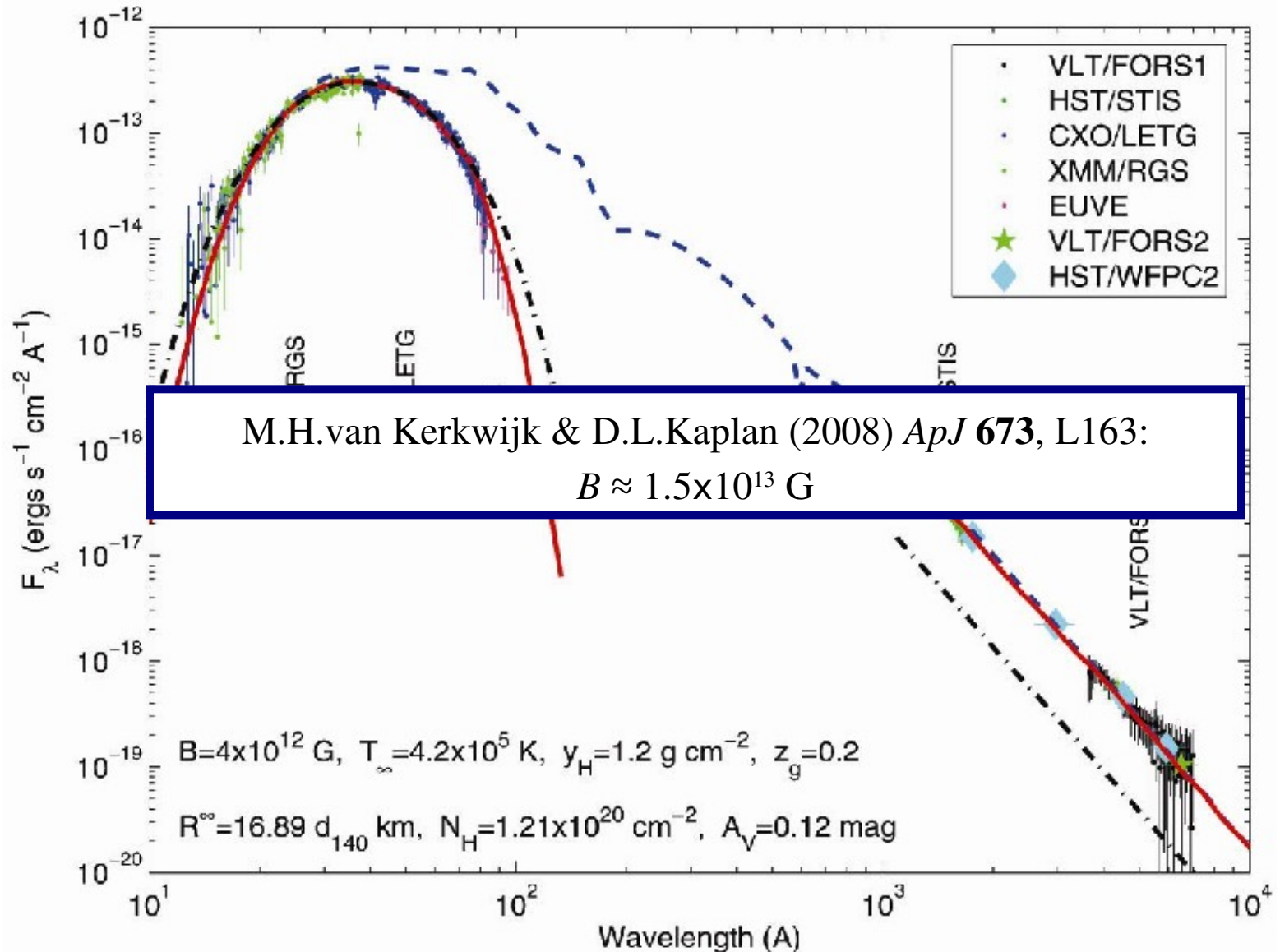
Dot-dashed lines correspond to the radiative surface, the shadowed region corresponds to  $E < E_{pl}$ .



# Link of the theory with observations

## Case of RX J1856.4-3754

W.C.G.Ho *et al.* (2007) *MNRAS*, **375**, 821

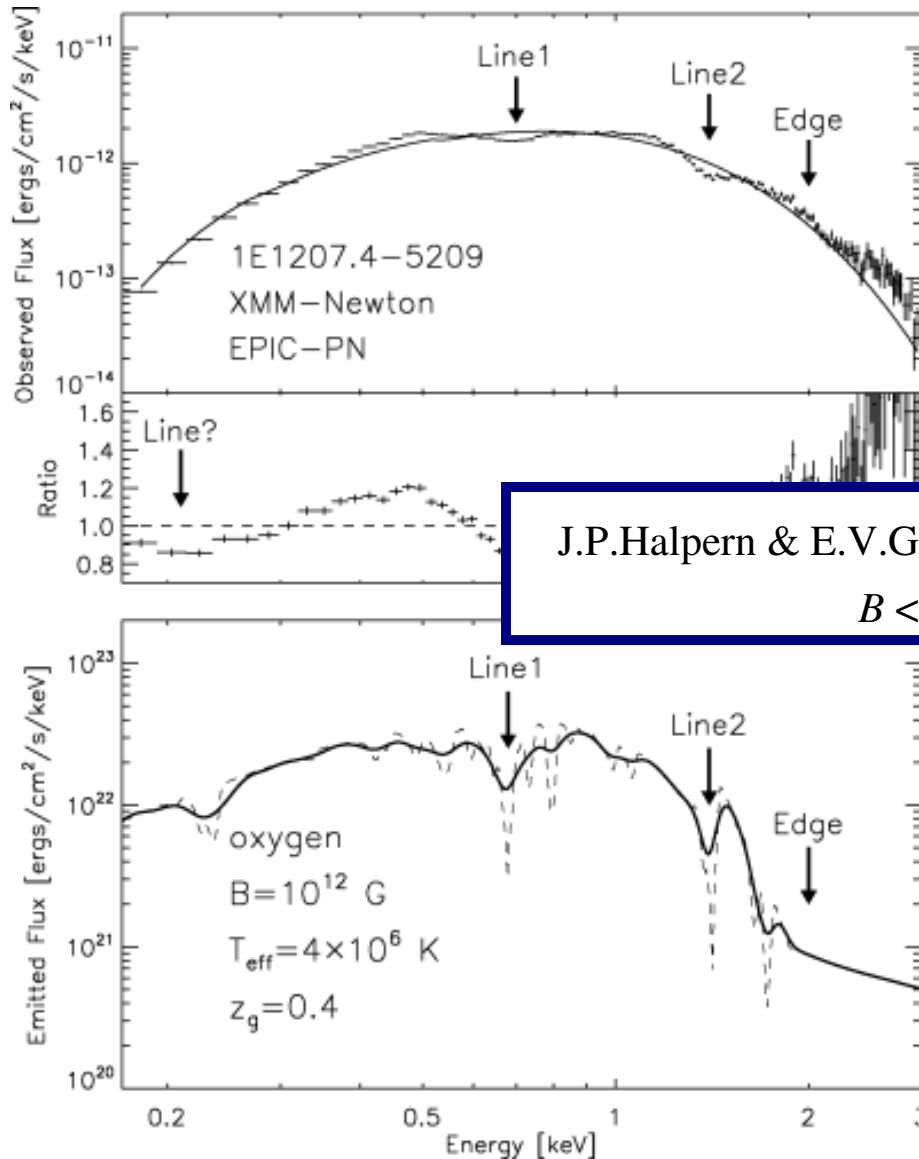


# Link of the theory with observations

## Case of 1E 1207.4–5209

### Atmosphere models for heavier elements

K.Mori & W.C.G.Ho (2007) *MNRAS* 377, 905

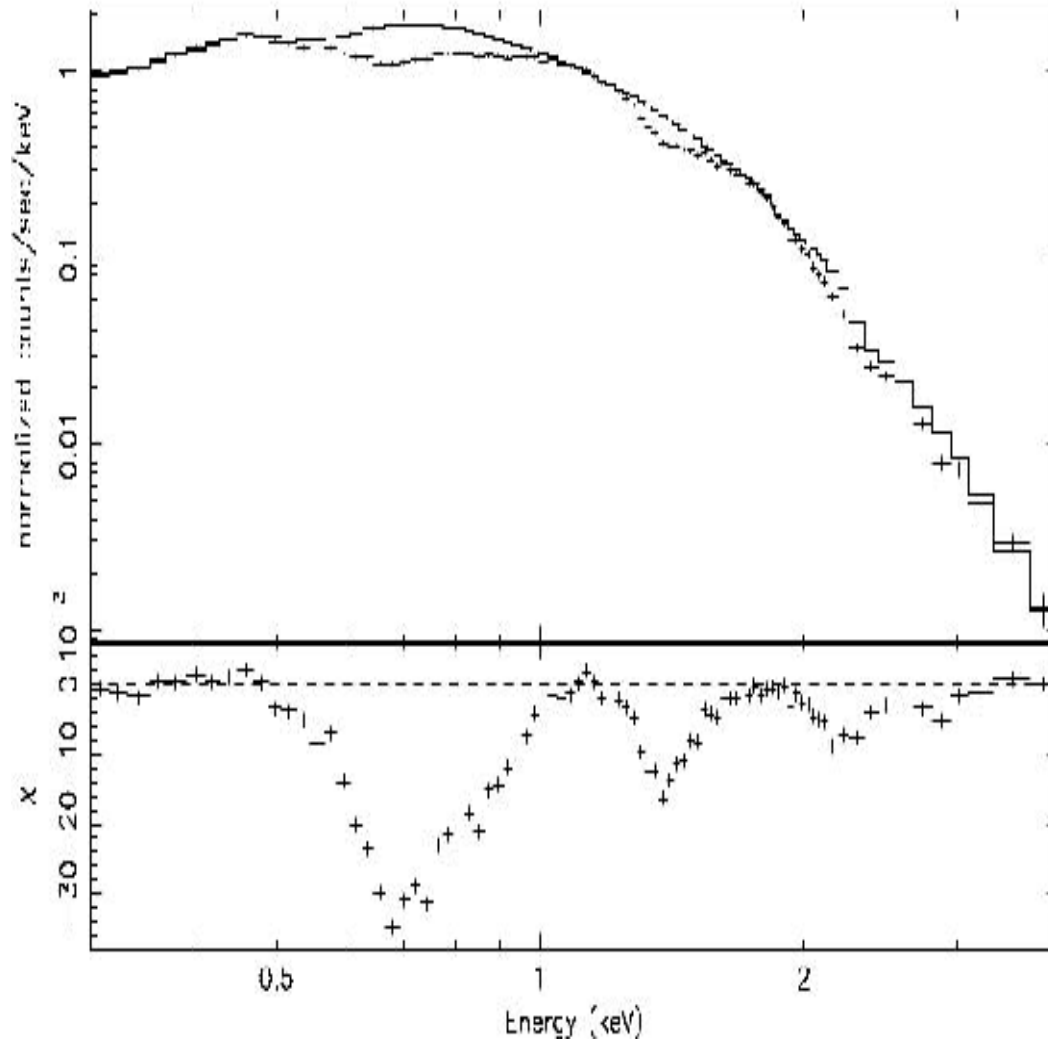


J.P.Halpern & E.V.Gottelf (2010) *ApJ* 709, 436:

$$B < 3.3 \times 10^{11} \text{ G}$$

## Case of 1E 1207.4–5209

Data and best fit continuum model



[Figure: Bignami *et al.* (2004) *Mem.S.A.It.* **75**, 448]

$$\hbar\omega_c = \hbar e B / mc = 11.577 B_{12} \text{ keV}$$

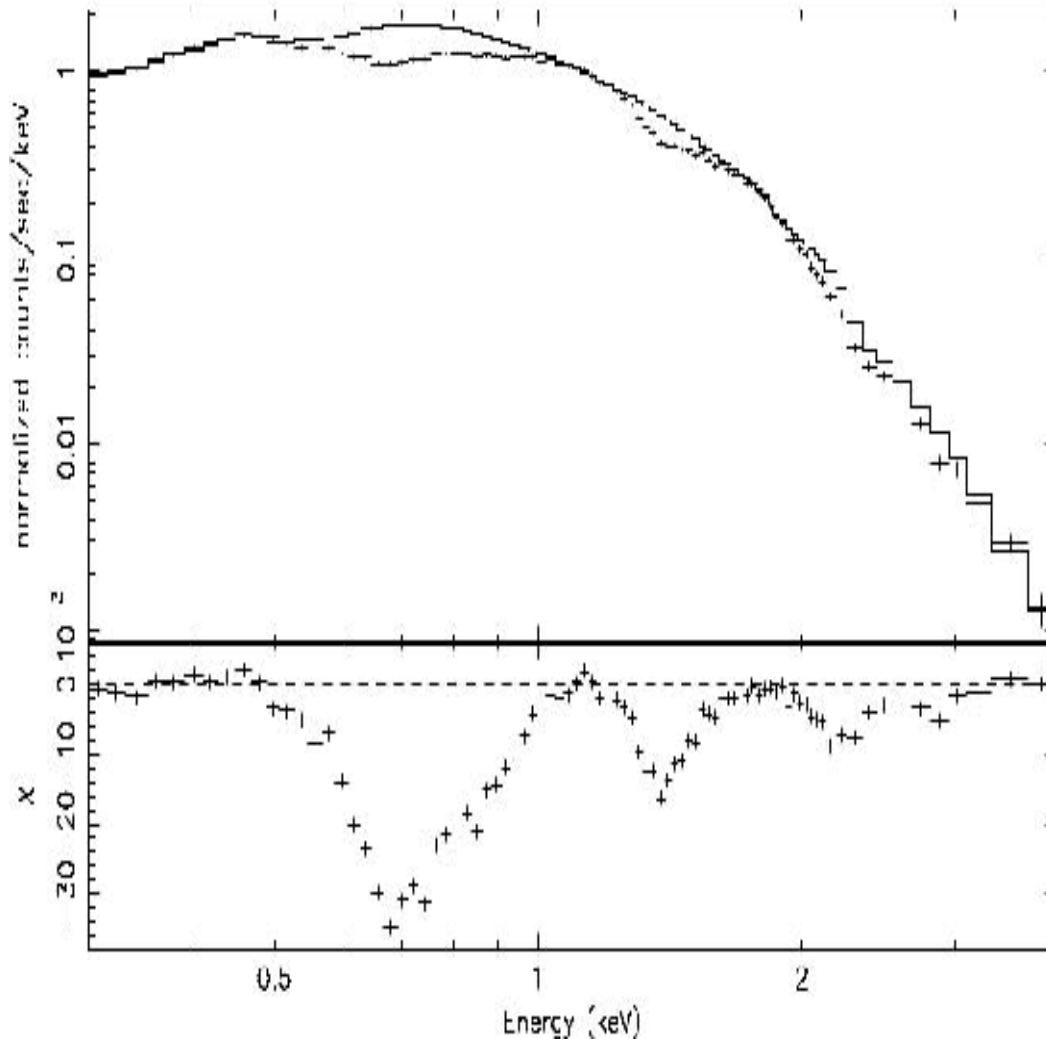
$$\hbar\omega_{ci} = \hbar Z e B / m_i c = 6.35 (Z/A) B_{12} \text{ eV}$$

$$\max(T_{\text{eff}}, E_a) / mc^2 \sim 10^{-3}$$

K.Mori, J.C.Chonko, C.J.Hailey  
(2005): only 2 features are real.

## Case of 1E 1207.4–5209

Data and best fit continuum model



$$\hbar\omega_c = \hbar e B / mc = 11.577 B_{12} \text{ keV}$$

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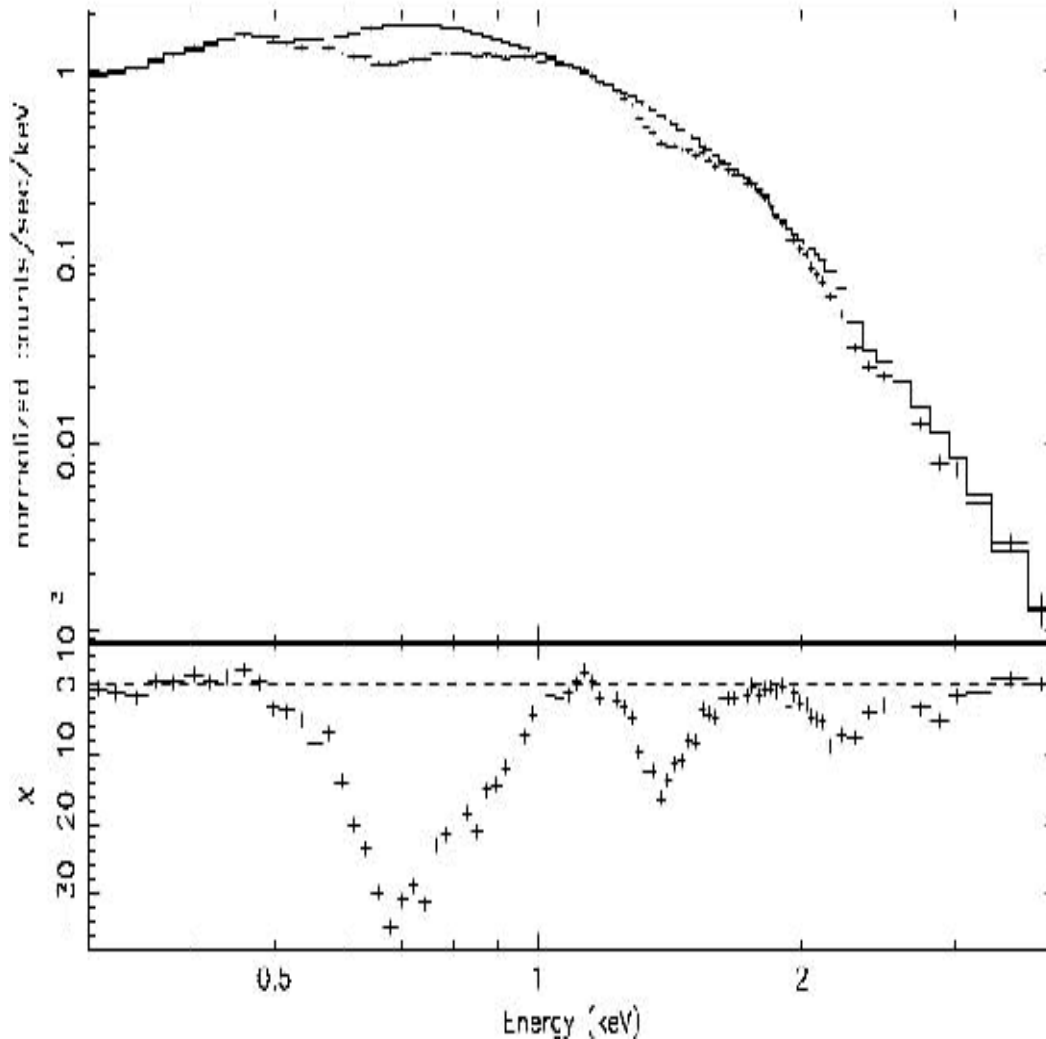
G.G.Pavlov & Yu.A.Shibanov (1978);  
S.Zane, R.Turolla, A.Treves (2001):  
electron or proton (ion) **free-free** cyclotron  
harmonics?

**Electron** cyclotron  $\rightarrow B \approx 8 \times 10^{10} \text{ G}$ .

V.F.Suleimanov, G.G.Pavlov, K.Werner  
(2010) *ApJ* **714**, 630 (“**quantum**” cyclotron  
harmonics)

## Case of 1E 1207.4–5209

Data and best fit continuum model



$$\hbar\omega_c = \hbar e B / mc = 11.577 B_{12} \text{ keV}$$

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$$\max(T_{\text{eff}}, E_a) / mc^2 \sim 10^{-3}$$

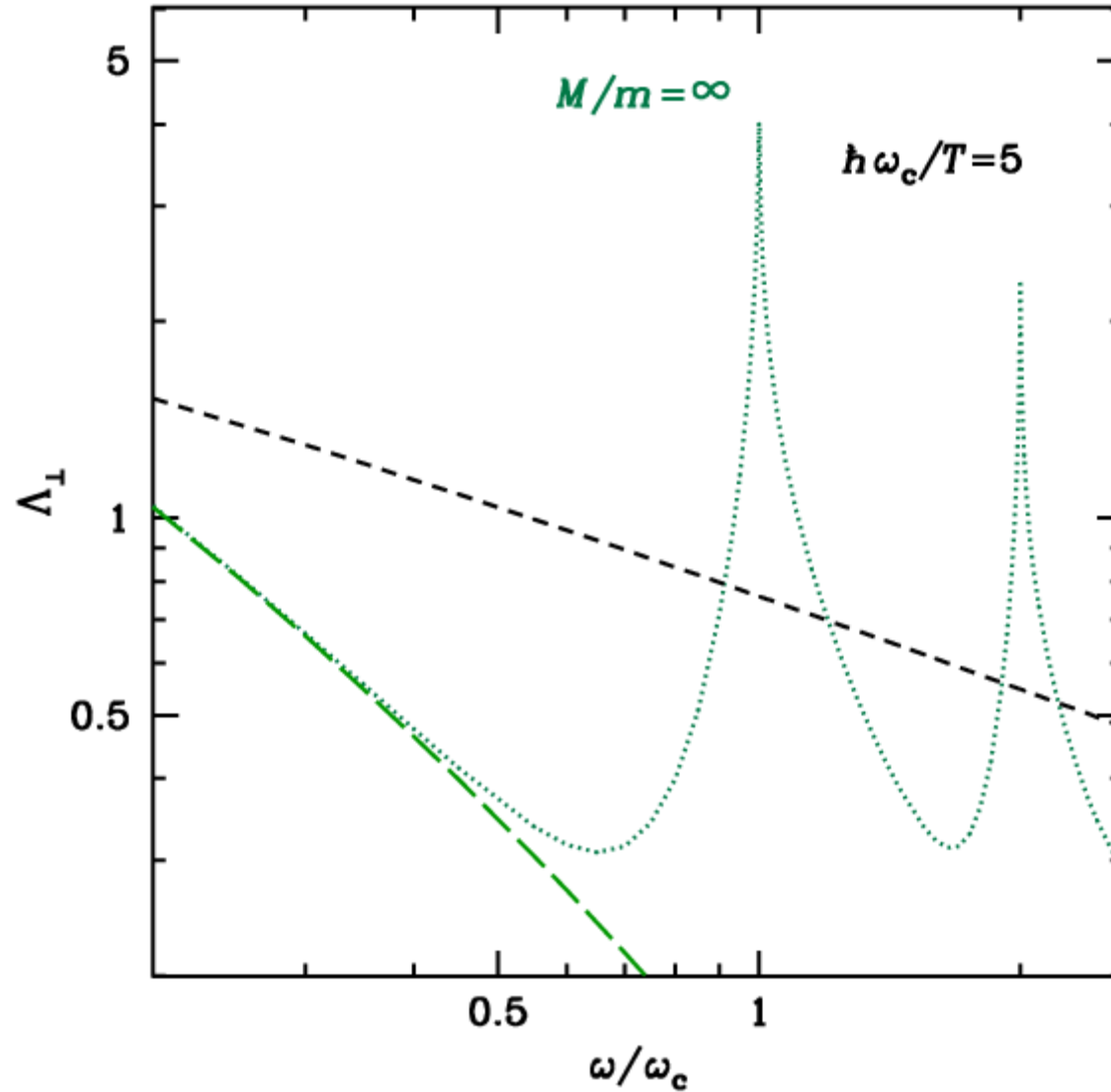
G.G.Pavlov & Yu.A.Shibanov (1978);  
S.Zane, R.Turolla, A.Treves (2001):  
electron or proton (ion) **free-free** cyclotron  
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V.F.Suleimanov, G.G.Pavlov, K.Werner  
(2010) *ApJ* **714**, 630 (**free-free** cyclotron  
harmonics)

J.P.Halpern & E.V.Gottelf (2011)  
*ApJ* **733**, L28:  $B \approx 2.4 \times 10^{11} \text{ G}$  or  
 **$9.9 \times 10^{10} \text{ G}$  (!)**

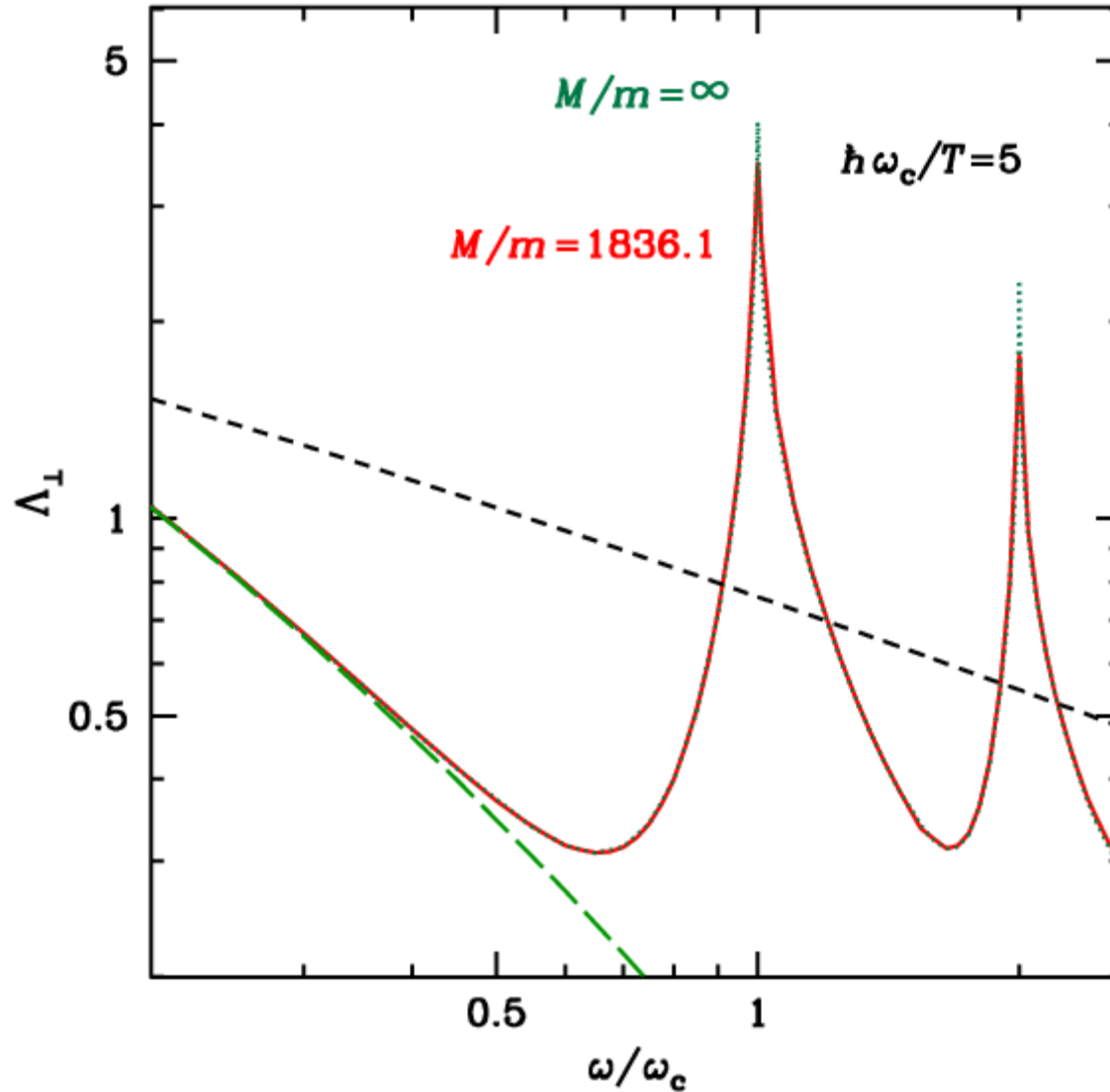
## Cyclotron harmonics in spectra of isolated neutron stars



$$\sigma_{\alpha}(\omega) = \frac{4\pi e^2}{mc} \frac{\nu_{\alpha}^{\text{ff}}(\omega)}{(\omega + \alpha\omega_c)^2 - (\nu_e + \nu_{\alpha}^{\text{ff}})^2}$$

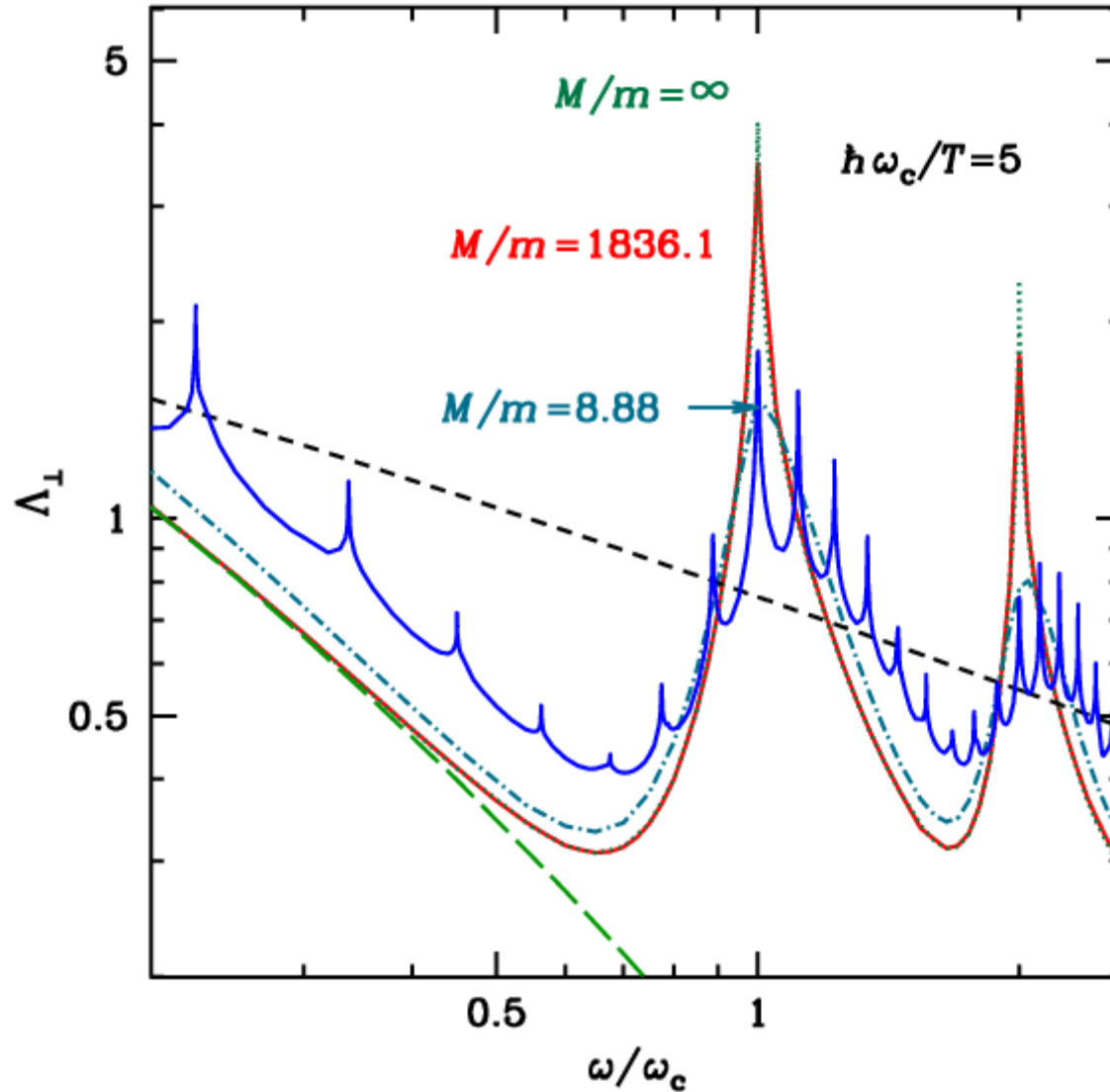
$$\nu_{\alpha}^{\text{ff}} = \frac{4}{3} \sqrt{\frac{2\pi}{mT}} \frac{n_0 e^4}{\hbar\omega} \Lambda_{\alpha}^{\text{ff}}(\beta_0, \omega/\omega_c)$$

## Cyclotron harmonics in spectra of isolated neutron stars



V.F.Suleimanov, G.G.Pavlov, K.Werner (2010) *ApJ* **714**, 630:  
approximate treatment of proton recoil  
(following G.G.Pavlov & A.N.Panov, 1976, *Sov. Phys. JETP* **44**, 300)

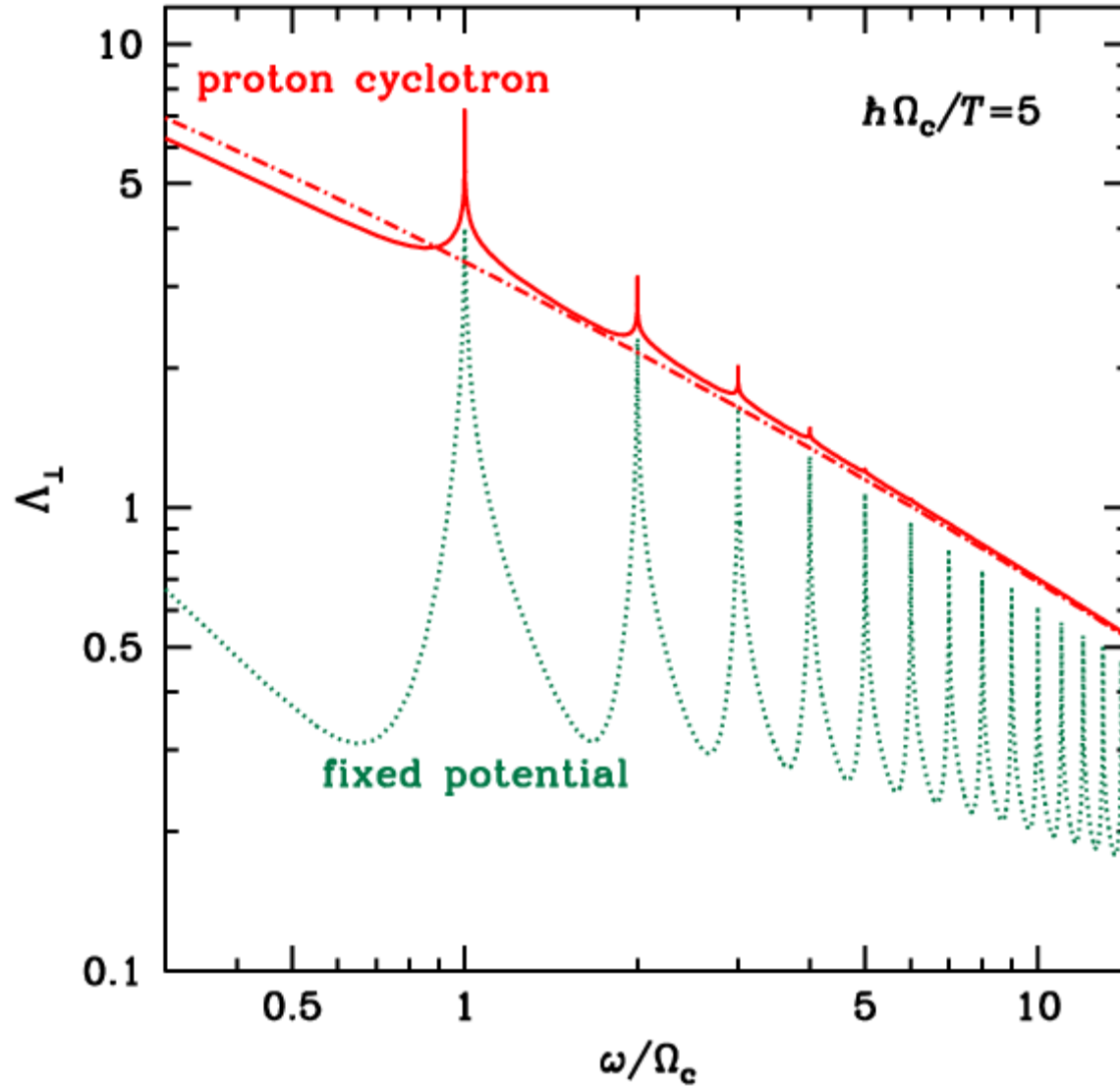
## Cyclotron harmonics in spectra of isolated neutron stars



Accurate treatment of the proton-lepton-photon system in quantizing magnetic fields  
[Potekhin & Chabrier (2003) *ApJ* **585**, 955; Potekhin (2010) *A&A* **518**, A24]



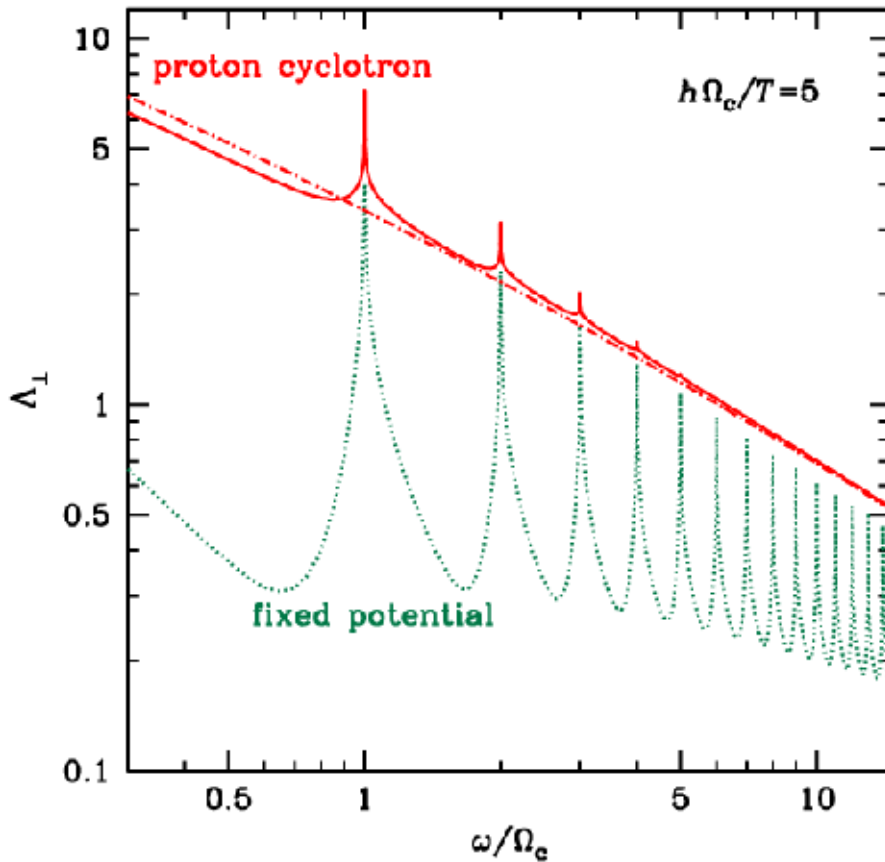
## Cyclotron harmonics in spectra of isolated neutron stars



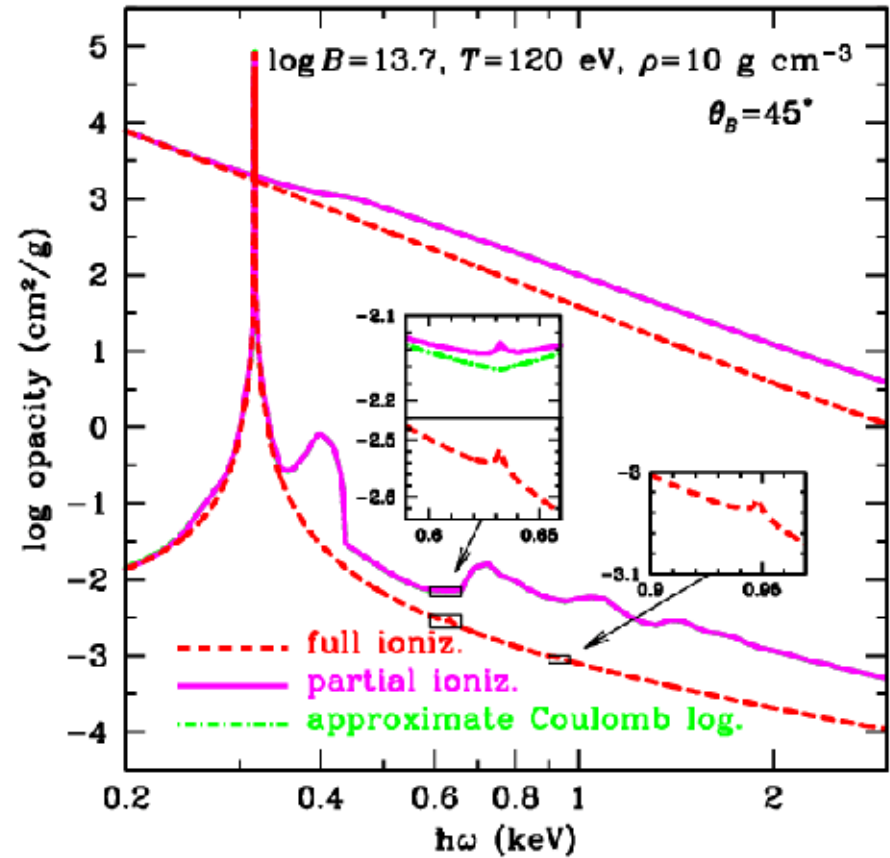
Accurate treatment of the proton-lepton-photon system in quantizing magnetic fields  
[Potekhin & Chabrier (2003) *ApJ* **585**, 955; Potekhin (2010) *A&A* **518**, A24]

# Absence of ion cyclotron harmonics in spectra of isolated neutron stars

A.Y.Potekhin "Cyclotron harmonics in opacities of isolated neutron star atmospheres" *Aston. Astrophys.* 518, A24 (2010)



Coulomb logarithm in the cross section of the free-free photoabsorption in a H plasma with a strong magnetic field as a function of the ratio of photon frequency  $\omega$  to the cyclotron frequency  $\Omega_c$ . Dotted line – approximation of a fixed scattering potential (suitable for electron cyclotron harmonics). Solid line – an accurate calculation. Dash-dotted line – neglecting Landau quantization for protons.

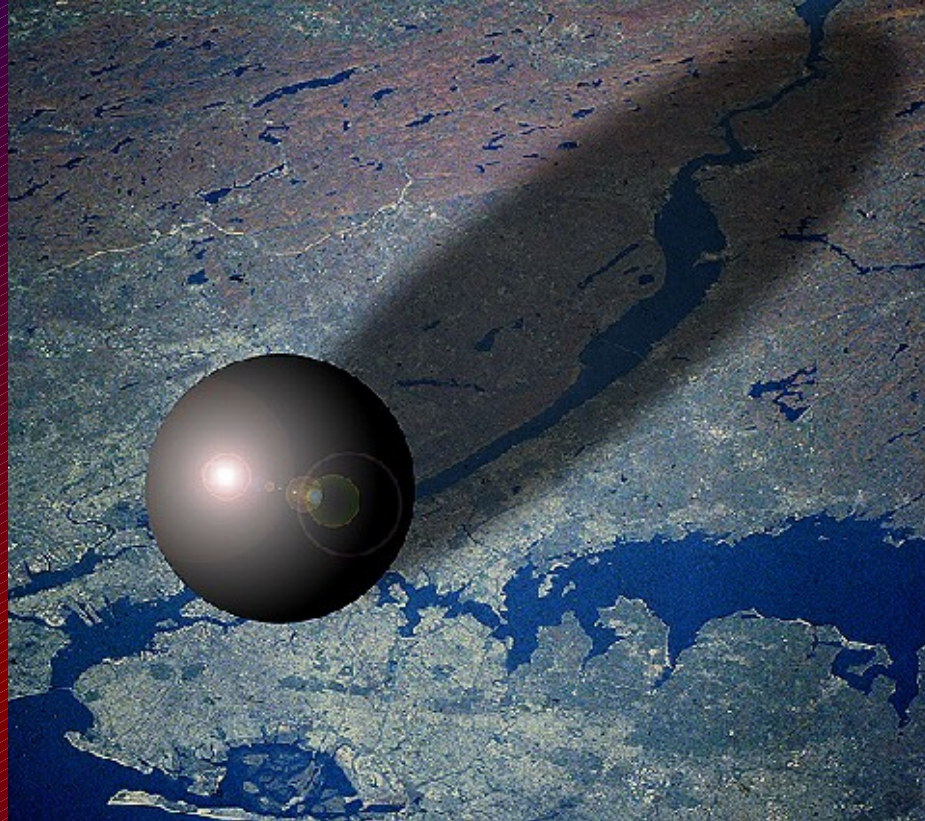


Opacities for O- (upper curves of each type) and X-modes of radiation in the H atmosphere of a NS with  $B=5 \times 10^{13}$  G. Dashes – fully ionized plasma model, solid lines – partially ionized, dot-dashed – partially ionized without free-free cyclotron harmonics. The features caused by incomplete ionization (atomic resonances) are much stronger than proton cyclotron harmonics.

# Conclusions

- Practical models of the *EOS* and *opacities* of strongly magnetized plasmas, applicable to neutron stars, are developed and applied to modeling thermal structure of neutron-star envelopes and spectra of neutron star thermal radiation.
- Models of neutron-star thermal spectra with account of *strong magnetic fields*, *partial ionization*, and *magnetic condensation* are becoming practical for interpretation of observations.
- *For chemical elements other than H*, magnetic atmosphere opacities are known at crude approximations and require further study.
- *Superstrong* magnetic fields (1) induce new effects which can reveal themselves in the spectra and (2) lead to theoretical uncertainties, which require further studies.

***THANK YOU FOR YOUR ATTENTION !***



[Image credit: NASA/Marshall Space Flight Center]