

XMM–Newton observations of a gamma-ray pulsar J0633+0632: pulsations, cooling and large-scale emission

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ABSTRACT

We report results of *XMM–Newton* observations of a γ -ray pulsar J0633+0632 and its wind nebula. We reveal, for the first time, pulsations of the pulsar X-ray emission with a single sinusoidal pulse profile and a pulsed fraction of 23 ± 6 percent in the 0.3–2 keV band. We confirm previous *Chandra* findings that the pulsar X-ray spectrum consists of thermal and non-thermal components. However, we do not find the absorption feature that was previously detected at about 0.8 keV. Thanks to the greater sensitivity of *XMM–Newton*, we get stronger constraints on spectral model parameters compared to previous studies. The thermal component can be equally well described by either blackbody or neutron star atmosphere models, implying that this emission is coming from either hot pulsar polar caps with a temperature of about 120 eV or from the colder bulk of the neutron star surface with a temperature of about 50 eV. In the latter case, the pulsar appears to be one of the coolest among other neutron stars of similar ages with estimated surface temperatures. We discuss cooling scenarios relevant to this neutron star. Using an interstellar absorption–distance relation, we also constrain the distance to the pulsar to the range of 0.7–2 kpc. Besides the pulsar and its compact nebula, we detect regions of weak large-scale diffuse non-thermal emission in the pulsar field and discuss their possible nature.

Key words: stars: neutron – pulsars: general – pulsars: individual: PSR J0633+0632.

1 INTRODUCTION

More than 200 pulsars have been detected in γ -rays with the *Fermi* observatory.¹ A significant number of them are radio-quiet, which can be partially explained by unfavourable orientations of pulsar radio beams. Due to the intrinsic faintness of pulsars in the optical band, any additional information on the radio-quiet *Fermi* pulsars, including distances to them, can be obtained only from observations in X-rays. X-ray observations are also crucial for the study of non-thermal and thermal emission components from pulsar magnetospheres and surfaces. In addition, X-ray observations can reveal a parent supernova remnant (SNR) and/or a pulsar wind nebula (PWN), studies of which can help to constrain the age and transverse velocity of the corresponding pulsar as well as the properties of its wind and environment. Furthermore, analysing the morphology of some PWNe, namely torus-like PWNe like Crab and Vela, one can constrain the inclination of the pulsar’s rotational axis to the observer’s line of sight (Ng & Romani 2004, 2008).

A radio-quiet pulsar J0633+0632 (hereafter J0633) was discovered with *Fermi* by Abdo et al. (2009). It has a period $P = 297.4$ ms, a characteristic age $t_c = 59.2$ kyr, a spin-down luminosity $\dot{E} = 1.2 \times 10^{35}$ erg s^{−1} and a dipole surface magnetic field $B = 4.9 \times 10^{12}$ G (Abdo et al. 2013). The first 20-ks *Chandra* observations allowed Ray et al. (2011) to identify J0633 in X-rays and to reveal a faint PWN adjusted to the pulsar. The *Chandra* image obtained with the Advanced CCD Imaging Spectrometer (ACIS) is shown in the left-hand panel of Fig. 1 where J0633, its PWN and an unrelated point-like source ‘A’ are marked (see Danilenko et al. 2015 for a description of the data reduction). The X-ray spectrum of J0633 consists of thermal and non-thermal components (Ray et al. 2011; Danilenko et al. 2015). The latter is fitted by a power law (PL) while the former can be equally well described by either the blackbody model or the model of a neutron star (NS) magnetized atmosphere (Pavlov et al. 1995; Ho, Potekhin & Chabrier 2008).

Danilenko et al. (2015) found a signature of an absorption feature at ≈ 0.8 keV in the *Chandra* spectrum of the pulsar. They suggested that it might be the cyclotron line created in the strong magnetic field of the NS though other origins are also possible. Among known isolated NSs, X-ray absorption lines have been reported only for a few exotic objects, including compact central objects in SNRs, X-ray dim isolated NSs and magnetars (see e.g. Danilenko et al. 2015 for references). Concerning

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¹ <https://confluence.slac.stanford.edu/display/GLAMCOG/Public+List+f+LAT-Detected+Gamma-Ray+Pulsars>

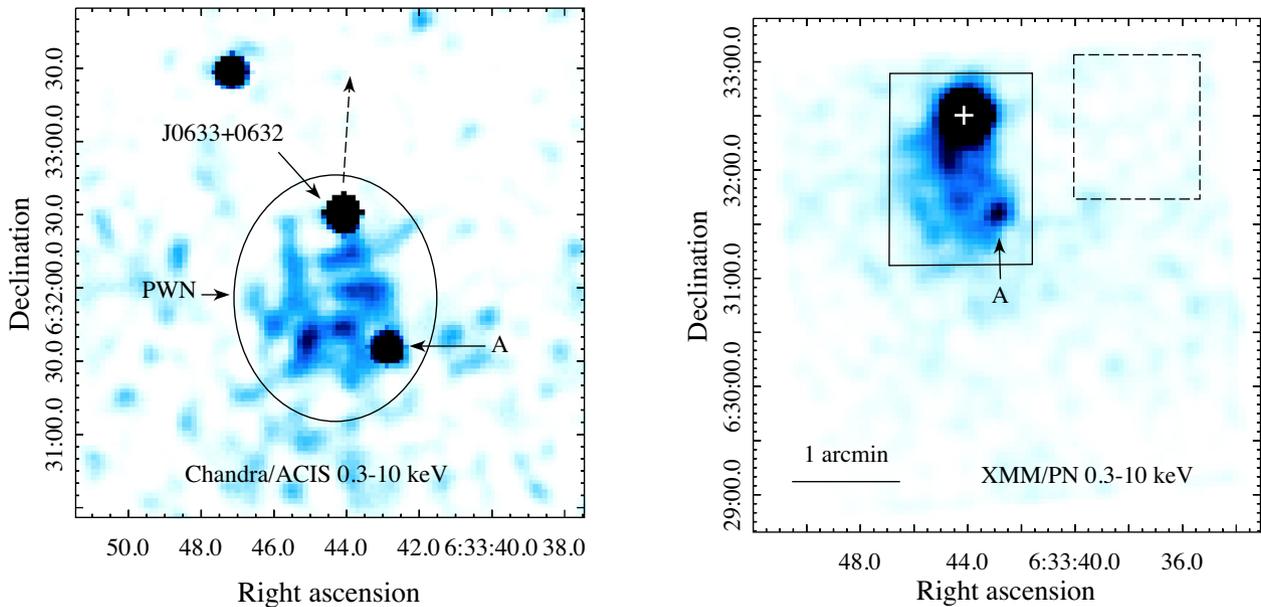


Figure 1. *Left:* 3.5×3.5 arcmin *Chandra* image of the J0633 vicinity in the 0.3–10 keV band. J0633 and an unrelated source ‘A’ are marked. The compact PWN is enclosed by the ellipse. The possible direction of the pulsar proper motion is shown by the dashed arrow. *Right:* FOV of the *XMM–Newton* EPIC-pn camera in the small window mode (0.3–10 keV). The J0633 position is shown by the ‘+’ symbol. Source ‘A’ is also marked. The solid and dashed boxes enclose regions used to extract the PWN and background spectra.

rotation-powered pulsars (RPPs), the most numerous subclass of isolated NSs, there are only PSR J1740+1000 (Kargaltsev et al. 2012) and possibly PSR J0659+1414 (Arumugasamy et al. 2018) whose spectra show absorption features. J0633 could thus be the third such RPP. However, the low count statistics of the *Chandra* data does not allow one to confidently resolve its line profile.

Analysing the interstellar absorption towards J0633, Danilenko et al. (2015) constrained the distance to the pulsar within the range of 1–4 kpc. They also noted that the elongation of the PWN southwards of the pulsar is likely caused by the pulsar proper motion in the opposite direction. The presumed proper motion direction is shown by the dashed arrow in Fig. 1 (left-hand panel). Its expected value was estimated to be $\approx 80 \text{ mas yr}^{-1}$, which corresponds to a transverse velocity of $380 D_{1\text{kpc}} \text{ km s}^{-1}$, where $D_{1\text{kpc}}$ is the distance in units of 1 kpc. Taking this, a possible birthplace of J0633 was suggested to be in the Rosette nebula, which is a 50-Myr-old active star-forming region.

A search for J0633 in the optical has been performed with the Gran Telescopio Canarias (Mignani et al. 2016). No pulsar optical counterpart was detected down to ≈ 27.3 mag in the *g* band. The limit is consistent with the extrapolation of the X-ray PL spectral component to the optical range. The High Altitude Water Cherenkov (HAWC) collaboration recently reported on the possible detection of a TeV halo around J0633, HAWC J0635+070, extending by about $0^\circ.65$ and recalling the TeV halo around the Geminga pulsar (Brisbois et al. 2018).

To further study J0633 in X-rays, we performed deeper observations² with *XMM–Newton*. Here we present a description of the data analysis and results. The paper is organized as follows. The data and imaging analysis are described in Section 2. Timing and spectral analyses of J0633 are presented in Sections 3 and 4, respectively. In Section 5, we analyse the large-scale diffuse

emission revealed around the pulsar by *XMM–Newton*. We discuss the results in Section 6 and give a short summary in Section 7.

2 THE DATA AND IMAGING ANALYSIS

The J0633 field was observed with the European Photon Imaging Camera (EPIC)³ onboard *XMM–Newton* on 2016 March 31 (MJD 57478), with a total exposure time of 93 ks. Two metal oxide semiconductor (MOS) CCD arrays were in the full frame mode with the medium filter setting while the pn-CCD detector (EPIC-pn) was in the small window mode with the thin filter enabling timing data analysis with ≈ 6 ms temporal resolution. We used the XMM-SAS v.16.0.0 software for the data analysis.

We exclude periods of high background activity using the ESPFILT tool. This results in clean exposure times of 51.8, 63.6 and 33.0 ks for the MOS1, MOS2 and pn cameras, respectively.

The EPIC-pn field of view (FOV) is shown in the right-hand panel of Fig. 1. As seen, the pulsar and its PWN, previously revealed with *Chandra*, are firmly detected with *XMM–Newton*. The *Chandra* position of J0633 (see Table 1) is marked by the ‘+’ symbol. The image appears to be blurred, as compared to the *Chandra* image, due to the lower spatial resolution of *XMM–Newton*. Nevertheless, an unrelated point-like background source ‘A’, with coordinates $\text{RA} = 6^{\text{h}}33^{\text{m}}42^{\text{s}}.902$ and $\text{Dec.} = +6^{\circ}31'36''.16$, obtained with a CIAO tool WAVDETECT from the *Chandra* data, is clearly resolved from the PWN in the EPIC-pn image.

Due to the mode selected, the EPIC-pn data allow us to image only the nearest vicinity of the pulsar, constrained by a small FOV of $\approx 4 \times 4$ arcmin. We used MOS1 and MOS2 data and the *XMM–Newton* Extended Source Analysis Software (XMM-ESAS; Snowden & Kuntz 2014) to construct much larger images with a

²ObsID 0764020101, PI Danilenko

³<https://www.cosmos.esa.int/web/xmm-newton/technical-details-epic>

Table 1. The J0633 timing model.[†]

RA (J2000) [‡]	06 ^h 33 ^m 44 ^s .142
Dec. (J2000) [‡]	+06°32′30″.40
Rotation frequency f , Hz	3.362 481 7298(6) [§]
Frequency derivative \dot{f} , Hz s ⁻¹	-8.9983(2) × 10 ⁻¹³
Frequency second derivative \ddot{f} , Hz s ⁻²	7.2 × 10 ⁻²⁵
Epoch of frequency, MJD	55555
Valid MJD range	54686.15–56583.16
Solar system ephemeris model	DE405
Time system	TDB

Notes. [†]Obtained from the LAT Gamma-ray Pulsar Timing Models page (Kerr et al. 2015) available at http://www.slac.stanford.edu/ke/rm/fermi_pulsar_timing/.

[‡]The position is obtained from the *Chandra* data (Ray et al. 2011).

[§]Hereafter, the numbers in parentheses denote errors relating to the last significant digit quoted.

FOV of $\approx 30 \times 30$ arcmin.⁴ We created these images and respective exposure maps using the MOS-SPECTRA tool. The quiescent particle background (QPB) images were generated by the MOS.BACK task and then subtracted. We adaptively smoothed the MOS1+MOS2 QPB-subtracted and exposure-corrected image applying the ADAPT tool and accumulating 50 counts for the smoothing kernel. The resulting image, in the 0.4–7.0 keV energy band, is presented in the top left-hand panel of Fig. 2.

Besides the pulsar and its compact PWN seen with *Chandra* and *XMM-Newton*/EPIC-pn, this image also reveals a fainter extended emission at larger scales. A relatively bright emission clump located west of the compact PWN and a long extended structure in the north-western part of the image, which apparently is not related to the pulsar, are particularly interesting. To better investigate them, we also created images in the 0.4–7, 0.4–2 and 2–7 keV bands where point-like sources were removed and the respective holes were refilled utilizing the CIAO DMFILTH task and pixel values from surrounding background regions. We did not exclude J0633 and the ‘A’ source since their removal leads to some distortion of the compact PWN shape. MOS1+MOS2 images were then adaptively smoothed accumulating 100 counts for the smoothing kernel. They are presented in the top-right and bottom panels of Fig. 2. One can see that morphology of the extended emission is roughly the same in the soft and hard bands, although the emission intensity appears to be higher at lower energies.

3 TIMING ANALYSIS

We used the EPIC-pn data to search for pulsations from J0633. To obtain maximal sensitivity for a pulsing component, we did not filter the event list for flaring background and used events in the 0.3–10 keV range extracted from a 15 arcsec-radius aperture centred at the *Chandra* position of the pulsar. This resulted in a total event number of 1717. We then corrected the event times of arrival (ToA) to the Solar system barycentre using the SAS task BARYCEN, the J0633 *Chandra* coordinates obtained by Ray et al. (2011) (see Table 1) and the Solar system ephemeris DE 405.

As a first step, we examined the Z_1^2 -test periodogram (Buccheri et al. 1983) in the frequency range of 3.35–3.37 Hz, enclosing the pulsar rotation frequency known from *Fermi* data (Table 1). It

shows a pronounced peak at the frequency of $\approx 3.362\,332$ Hz with $Z_1^2 \approx 40$, which corresponds to a pulsation detection significance of $\approx 4.8\sigma$ (Fig. 3).⁵ The X-ray pulsation frequency is consistent with the γ -ray one of 3.362 332 235(3) Hz, which is adjusted to the epoch of the *XMM-Newton* observations (MJD 57478) using the *Fermi* timing results from Table 1.

To crosscheck this result and to compute the frequency uncertainty, we applied the Gregory–Loredo Bayesian method for the analysis of periodic signals (Gregory & Loredo 1992) and used pn data cleaned from the flaring background. The method considers a number of step-wise profiles each consisting of a specific number of steps m , $m = 1 \dots m_{\max}$. During the analysis, we folded ToA with each m -step model for any trial pair of frequency ν and phase ϕ . The method then applies the Bayesian theory to compute a probability p in favour of any periodic model ($m > 1$) over the constant model ($m = 1$):

$$p(m > 1 | \text{ToA}) = \frac{\sum_{m=2}^{m_{\max}} O_{m1}}{1 + \sum_{m=2}^{m_{\max}} O_{m1}}. \quad (1)$$

In equation (1), O_{m1} is the odds ratio in favour of the m -step periodic model. It is inversely proportional to the number of ways a given distribution $\{n_i\}$, $i = 1 \dots m$, of N_{ToA} times of arrival over m period bins could have arisen by chance, or the so-called multiplicity:

$$W_m(\nu, \phi) = \frac{N_{\text{ToA}}!}{\prod_{i=1}^m n_i!}. \quad (2)$$

To sample the probability density $-\ln W_m(\nu, \phi)$, we applied the Metropolis–Hastings (MH) Markov chain Monte Carlo (MCMC) method (Metropolis et al. 1953).

It turns out O_{m1} drops very quickly as m increases. To compute the resulting odds ratio $Q_{\text{per}} = \sum_{m=2}^{m_{\max}} O_{m1}$ in favour of the hypothesis that the signal is periodic, we thereby safely chose $m_{\max} = 6$ since larger m would not significantly contribute to Q_{per} . The resulting $Q_{\text{per}} \approx 2451$ corresponds to the 99.96 per cent probability (equation 1) that the signal is periodic. MCMC simulations yield, for any m , a maximal-probability frequency of 3.362 333(1) Hz, where the number in brackets is the uncertainty computed from the 68 per cent credible interval. Within 1σ uncertainty, it is consistent with the *Fermi* value and with the results of the Z_1^2 test.

To calculate a zero rotational phase for EPIC-pn events, we used the *Fermi* ephemeris and applied the PHOTONS plug-in⁶ for the TEMPO2 package (Hobbs, Edwards & Manchester 2006). Phase-folded *XMM-Newton* light curves of J0633 in soft (0.3–2 keV) and hard (2–10 keV) bands are presented in the two bottom panels of Fig. 4. We also show the γ -ray pulse profile obtained from *Fermi* data using the TEMPO2 FERMI plug-in.⁷ For the latter, we downloaded data from the *Fermi* website⁸ and processed them using the *Fermi* science tools (v10r0p5). We selected events from the 0°.8 radius aperture applying a SOURCE class event (EVCLASS = 128)

⁵The corresponding frequency uncertainty, calculated using the formula from Chang et al. (2012), is 1.3 μ Hz.

⁶<http://www.physics.mcgill.ca/aarchiba/photons.plugin.html>

⁷The J0633 *Fermi* timing model, which was used to create the pulse profiles in Fig. 4, is constructed for the MJD range (see Table 1), which ends before *XMM-Newton* observations. Since the extrapolated frequency is in agreement with that found in the X-ray data, we just folded the pn light curve using this model. However, further refinement of the model potentially may lead to some change in the shift between the peaks of the X-ray and γ -ray profiles.

⁸<https://fermi.gsfc.nasa.gov/cgi-bin/ssc/LAT/LATDataQuery.cgi>

⁴Note that MOS1 CCDs 3 and 6 were damaged due to micrometeorite strikes and thus switched off (Snowden & Kuntz 2014).

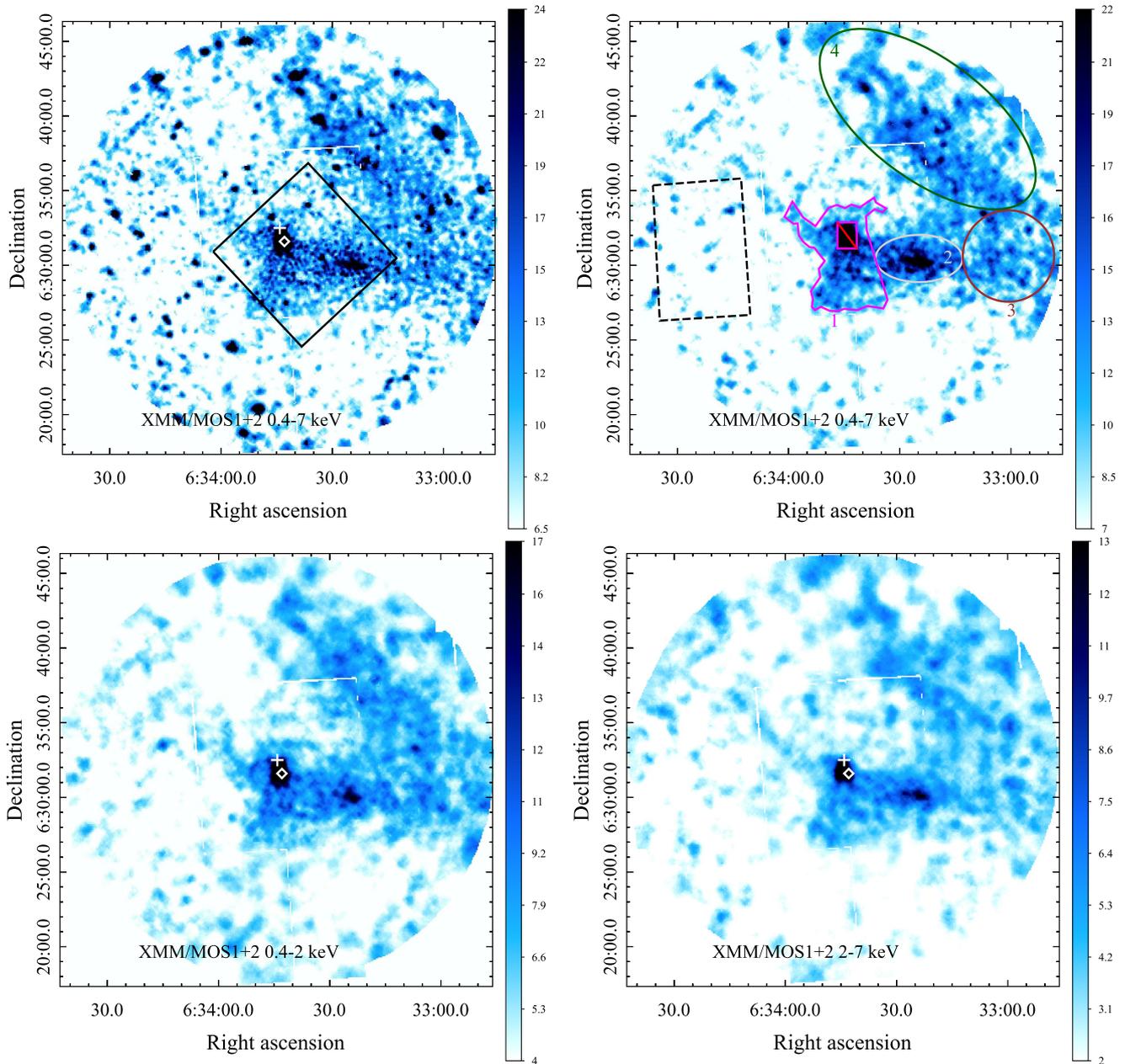


Figure 2. *Top-left:* combined XMM–Newton MOS1 and MOS2 exposure-corrected QPB-subtracted image of the J0633 field in the 0.4–7 keV band. The positions of J0633 and the ‘A’ source are shown by the ‘+’ and ‘◇’ symbols, respectively. The solid box in the *top-left* indicates the Chandra/ACIS-S3 chip FOV. *Top-right:* the same combined image where we have removed all point sources except J0633 and ‘A’. Regions used for spectral analysis of the diffuse emission are shown and numbered. The bright PWN region shown in the right-hand panel of Fig. 1 was excluded from region 1 in the analysis. The dashed box was used for the background. *Bottom:* the same as in the *top-right* but in the soft and hard photon energy bands, as shown in the panels. The intensity is given in counts $\text{s}^{-1} \text{deg}^{-2}$.

and a zenith angle of $<100^\circ$. Good time intervals were generated assuming filtering criteria `DATA_QUAL == 1` and `LAT_CONFIG == 1`.

The J0633 pulsations are clearly seen in the soft X-ray band, while they are only marginally resolved in the hard band. In contrast to the sharp double-peaked γ -ray pulse profile, with about 0.5 phase gap between two peaks, presumably produced by energetic particles accelerated near the equatorial current sheet, which emerges at and/or beyond the light cylinder of the pulsar (see e.g. Kalapotharakos et al. 2019 and references therein), the soft X-ray profile is broad and sinusoidal, as expected for thermal emission from the NS surface modulated by its rotation. A similar

situation is observed, e.g. for the well studied and also radio-quiet pulsar Geminga, where there is a broad single pulse of the thermal emission observed in the soft X-ray band accompanied by two sharp peaks of non-thermal emission seen in hard X-rays and gamma-rays (Mori et al. 2014).

We calculated the X-ray pulsed fraction (PF) as $(I_{\max} - I_{\min}) / (I_{\max} + I_{\min})$, where I_{\max} and I_{\min} are maximum and minimum intensities of the pulse profile. The intrinsic PF in the soft band, corrected for the background contribution, is 23 ± 6 per cent. In the hard band, the data allow us to place only a 3σ (99.7 per cent) upper limit $\text{PF} < 30$ per cent.

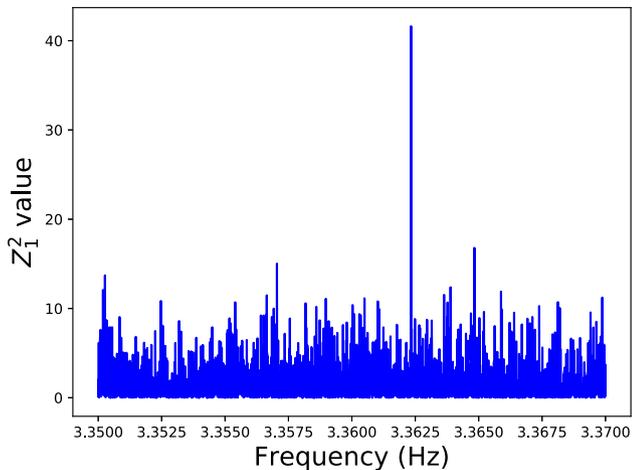


Figure 3. Z_1^2 -test periodogram for *XMM-Newton* observations of J0633 using only events with energies in the range of 0.3–10 keV. The event list was not filtered for flaring background, to obtain maximal sensitivity for the pulsing component.

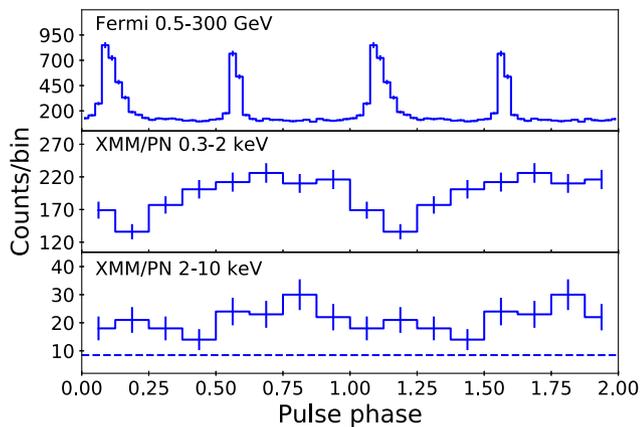


Figure 4. Phase-folded light curves of J0633 in different energy ranges, indicated in the panels. X-ray light curves were obtained from the data cleaned from flaring background. The dashed line indicates the background level in the 2–10 keV band. In the 0.3–2 keV band, the background level (≈ 13 counts phase bin $^{-1}$) is not shown since it is significantly lower than the pulsar count rate.

4 SPECTRA OF J0633 AND ITS PWN

We extracted time-integrated spectra of the J0633 pulsar from the MOS and pn data using a circular aperture with a radius of 15 arcsec centred at the pulsar position, as measured by *Chandra*. The PWN spectra were extracted from a solid region shown in the right-hand panel of Fig. 1, wherein circular regions around J0633 and the source ‘A’, with radii of 20 and 15 arcsec, respectively, were excluded. All background spectra were extracted from a dashed region that is also shown in the right-hand panel of Fig. 1. Redistribution matrix (RMF) and ancillary response (ARF) files were created by the RMFGEN and ARFGEN commands. The total number of counts extracted from the pulsar aperture in the 0.3–10 keV range is 2894, with about 2626 counts left after subtraction of the background. The total number of PWN counts is 4884 with about 2504 counts being from the PWN itself.

To describe the non-thermal emission of the pulsar magnetosphere, we applied a PL model and we used another PL for the

PWN emission. For thermal emission from the NS surface, we tried blackbody (*bb*) and several models of the NS hydrogen atmosphere available in XSPEC. Namely, we considered models *nsa12* and *nsa13*, which provide spectra of NSs with fully ionized atmospheres and uniform radial magnetic fields $B = 10^{12}$ G and $B = 10^{13}$ G (Pavlov et al. 1995). We also considered models describing NSs with partially ionized atmospheres, NSMAX (Ho et al. 2008). Below, these models are referred to by the same number codes as in XSPEC. The model *ns1260* is for the uniform radial field $B = 4 \times 10^{12}$ G, which is close to the dipole field of J0633 estimated from the γ -ray timing. Models *ns123100* and *ns123190* are for the dipole magnetic field with $B = 1.82 \times 10^{12}$ G at the magnetic pole. They differ by the angle between the magnetic dipole axis and the direction to the observer, 0° and 90° , which is encoded by the last two digits of their numerical codes. Models *ns130100* and *ns130190* are the same but for larger $B = 10^{13}$ G. In the dipole models, the NS temperature varies with the magnetic latitude due to the magnetic anisotropy of the heat transfer from the star interiors, making the NS pole significantly hotter than the equator. For all thermal models, the gravitational redshift $1 + z_g = [1 - 2.953M_{\text{NS}}(M_\odot)/R_{\text{NS}}(\text{km})]^{-1/2}$ was fixed at 1.21, which corresponds to a reasonable NS with a mass $M_{\text{NS}} = 1.4 M_\odot$ and a circumferential radius $R_{\text{NS}} = 13$ km.

To describe the interstellar absorption, we applied an XSPEC photoelectric absorption model PHABS with atomic cross-sections from Balucinska-Church & McCammon (1992) and solar abundances from Anders & Grevesse (1989).

We performed spectral analysis in the 0.3–10 keV range simultaneously for J0633 and the PWN, assuming a common value of the absorption column density N_{H} . We grouped spectra of J0633 and the PWN using the FTOOLS GRPPHA command (Blackburn 1995) with the condition that each spectral bin should contain at least one count. As a likelihood, we used the so-called W statistic (Arnaud, Gordon & Dorman 2018), which is the C statistic (Cash 1979) modified to account for Poisson background and which tends to χ^2 , for background-subtracted spectra, as the number of counts in each bin increases.

We analysed spectra following the Bayesian approach and using an MCMC sampler proposed by Goodman & Weare (2010) (GW). It is straightforward in the Bayesian inference to account for some additional information (*prior*), which can help to better constrain the model parameters. In this respect, to constrain the radius of the thermally emitting area on the NS surface R and the distance to the NS D separately, but not only their ratio, we used a relation between distance and the Galactic selective extinction $E(B - V)$ in the pulsar direction as a prior (see e.g. Danilenko et al. 2015). In Fig. 5, we present such a relation obtained by means of a PYTHON package DUSTMAPS (Green 2018). We produced it from a recent 3D map of the dust distribution in the Galaxy based on *Gaia*, Pan-STARRS 1 and 2MASS data (Green et al. 2019). Five samples of the relation, shown in Fig. 5 by black lines, are drawn by means of the MCMC and represent the corresponding posterior distribution (see Green et al. 2019 for details). The thick red line there is the median of the samples. To use the samples in X-ray data fitting, we transformed $E(B - V)$ to the absorption column density N_{H} , the main parameter of the X-ray photoelectric absorption model. For the transformation, we applied an empirical relation $N_{\text{H}} = (0.7 \pm 0.1) \times E(B - V) \times 10^{22}$ cm $^{-2}$ obtained by Watson (2011) for the Galaxy using observations of X-ray afterglows of a large number of gamma-ray bursts.

To use all the samples shown in Fig. 5 in the MCMC, we do as follows. At each step of the MCMC, we randomly chose one of the samples and then, using the chosen sample, compute the distance

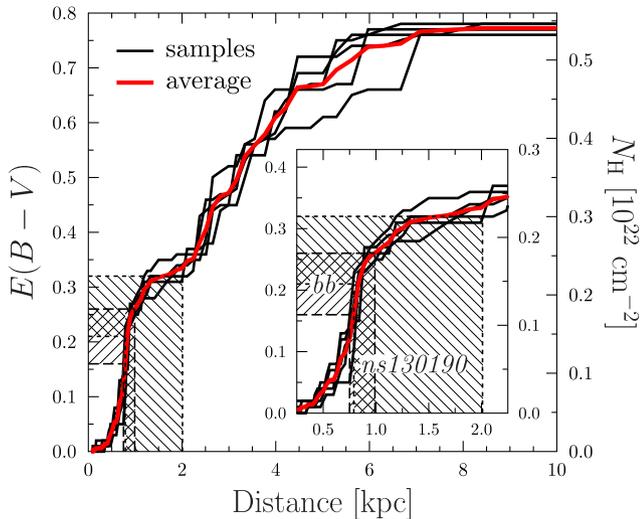


Figure 5. Relation between selective extinction $E(B - V)$ and distance in the direction towards the J0633 pulsar, according to the 3D map of the dust distribution in the Galaxy presented by Green et al. (2019). A distance–extinction domain relevant to J0633 is magnified in the inset. Hatched areas show 90 percent credible intervals for the *bb* and *ns130190* atmosphere models. The right vertical axis represents values of absorption column density N_{H} obtained using an empirical relation between $E(B - V)$ and N_{H} proposed by Watson (2011).

from the current value of N_{H} . In such an approach, only simulations of the distance actually depend on the additional information on the extinction. Other model parameters are simulated irrespective of such information. This approach is quite flexible as it allows one to account, in the same manner, for any number of additional relations, obtained from independent studies, between different model parameters.

In the GW sampler, we set a number of walkers, which is actually the only parameter of the sampler, being $L = 128$. Running L walkers in the GW method can be compared to running L independent *one-sampler* methods, like the MH one, at a time. However, for at least some distributions, basically smooth and unimodal, the former gives much smaller auto-correlation time τ , a parameter that quantifies the simulation errors, than the MH and Gibbs samplers do (Goodman & Weare 2010). Note that we used the MH algorithm instead of the GW one when searching for pulsations (Section 3). Indeed, statistical models of periodic signals quite often have extremely multi-modal distributions. In such cases, the GW sampler, at least as it is, becomes much less efficient.

To estimate τ , we followed a method proposed by Dan Foreman-Mackey, along with a number of useful pieces of advice and instructive examples in PYTHON.⁹ Convincing results are obtained when τ satisfies an empirical condition $\tau < N/50$, where N is the total number of samples. To ensure that the condition was satisfied, we had to run GW walkers for about $T \approx 10^5$ times yielding $N = L \times T \approx 10^7$. We obtained $\tau \approx 10^4 \ll N/50 \approx 2 \times 10^5$. This means that $\approx 10^7$ generated samples are equivalent to $\approx 10^3$ independent ones, which is enough to provide a robust result.

Each of the considered spectral models has eight free parameters. In Table 2, we show their maximal-probability-density values and equal-probability credible intervals computed from the MCMC

simulations, as well as W , χ^2 and the degrees of freedom (d.o.f) values demonstrating the fit qualities. For completeness, in Table 3, we present corresponding thermal bolometric fluxes F_{bol}^{∞} and luminosities L_{bol}^{∞} , as well as non-thermal fluxes ($F_{2-10\text{keV}}^{\text{psr}}$ and $F_{2-10\text{keV}}^{\text{pwn}}$) and luminosities ($L_{2-10\text{keV}}^{\text{psr}}$ and $L_{2-10\text{keV}}^{\text{pwn}}$) of the pulsar and PWN in the 2–10 keV range. The last two columns there also provide efficiencies of the transformation of the pulsar spin-down power to its own non-thermal emission and the emission of the PWN defined as $\eta_{2-10\text{keV}}^{\text{psr,pwn}} = L_{2-10\text{keV}}^{\text{pwn,psr}} / \dot{E}$. We also show the spectra of J0633 and its compact PWN in Fig. 6, and an example of the best-fitting models.

Considering the W and χ^2 values from Table 2, one can see that all the models are consistent with the data. A similar conclusion was drawn by Danilenko et al. (2015) from the analysis of the *Chandra* data, while they tried only *bb* and *ns1260* models for the thermal component. For these two models, our results are generally consistent with the results of that work, while the parameter uncertainties obtained here are much smaller. To our surprise, we found no evidence of the absorption spectral feature at 0.8 keV in the *XMM–Newton* data, whose presence in the *Chandra* data was claimed by Danilenko et al. (2015). This becomes clear from examination of the residuals of the spectral fit by a purely continuum spectral model presented in Fig. 6. The presence of the feature in the *Chandra* data and its absence in the *XMM–Newton* data remains puzzling. It could be either a time-variable feature, a low count fluctuation, or an unknown *Chandra* instrument artefact.

It is remarkable that all the models suggest credible intervals for the distance and N_{H} that are consistent with each other within uncertainties. This is illustrated by the hatched areas in Fig. 5 and implies a conservative range of the distance to J0633 being 0.7–2 kpc. The parameters of the pulsar and PWN non-thermal emission do not seem to depend significantly on the thermal model type either. At the same time, there is a predictably noticeable dependence of the inferred thermally emitting area and temperature of the NS on the chosen thermal model.

The *bb* model implies that the thermal component comes from a hotspot with a temperature of about 120 eV and a radius of about 0.8 km. The latter is about twice as large as ~ 0.4 km, the ‘classical’ size of a pulsar hot polar cap heated by relativistic particles from the pulsar magnetosphere, estimated for J0633 by Danilenko et al. (2015). This discrepancy will be reconciled if we assume that both polar caps are seen simultaneously, due to the gravitational bending of light. However, in that case, we would see a double-peaked pulse profile in X-rays in contrast to what is actually observed (Fig. 4). Alternatively, if the magnetic dipole of the NS is shifted in such a way that both polar caps occupy the same longitude we will still see a single pulse profile. Another alternative is that we see just one hotspot on the surface but of unusually large size, which could be caused, for example, by deviation of the surface magnetic field from the dipole. On the other hand, models *ns123100* and *ns130100*, assuming the NS magnetic axis directed to the observer, yield enormously large emitting area radii of about 50–70 km. Since the expected NS radius is in the range of 10–15 km, as predicted by various theoretical models (e.g. Lattimer & Prakash 2016) and confirmed by both electromagnetic (e.g. Degenaar & Suleimanov 2018) and gravitational-wave (e.g. Abbott et al. 2018) observations, these models can be rejected.

The rest of the spectral fits, that is, those by atmosphere models *nsa12*, *nsa13* and *ns1260*, describing NSs with the radial magnetic field, and models *ns123190* and *ns130190*, which are for NSs with the dipole magnetic field and the magnetic axis being orthogonal to the line of sight, give similar estimates of the effective surface

⁹<https://dfm.io/posts/autocorr/>

Table 2. Best-fitting parameters of the pulsar and PWN spectral models.[†]

Thermal model	N_{H} 10^{21} cm^{-2}	T_s^∞ eV 10^5 K	R km	D kpc	Γ_{psr}	K_{psr} 10^{-5} keV^{-1} $\text{cm}^{-2} \text{ s}^{-1}$	Γ_{pwn}	K_{pwn} 10^{-5} keV^{-1} $\text{cm}^{-2} \text{ s}^{-1}$	W d.o.f. = 769	χ^2
A couple of hot spots on the surface:										
<i>bb</i>	$1.5^{+0.4}_{-0.3}$	120^{+8}_{-8}	$13.7^{+1.0}_{-0.9}$	$0.8^{+0.5}_{-0.3}$	$0.8^{+0.2}_{-0.1}$	$1.9^{+0.3}_{-0.3}$	$1.0^{+0.3}_{-0.3}$	$1.6^{+0.1}_{-0.1}$	$2.4^{+0.3}_{-0.3}$	778 759
The bulk of the NS surface:										
<i>nsa12</i>	$1.8^{+0.4}_{-0.3}$	51^{+5}_{-6}	$5.9^{+0.6}_{-0.7}$	7^{+9}_{-3}	$0.9^{+0.4}_{-0.1}$	$1.6^{+0.3}_{-0.3}$	$0.7^{+0.2}_{-0.2}$	$1.7^{+0.1}_{-0.1}$	$2.6^{+0.3}_{-0.3}$	779 761
<i>nsa13</i>	$1.8^{+0.4}_{-0.3}$	53^{+5}_{-6}	$6.2^{+0.6}_{-0.7}$	6^{+8}_{-2}	$0.9^{+0.4}_{-0.1}$	$1.5^{+0.3}_{-0.3}$	$0.6^{+0.2}_{-0.2}$	$1.7^{+0.1}_{-0.1}$	$2.7^{+0.3}_{-0.3}$	778 762
<i>ns1260</i>	$1.8^{+0.4}_{-0.3}$	53^{+7}_{-5}	$6.2^{+0.8}_{-0.5}$	6^{+9}_{-3}	$0.9^{+0.6}_{-0.1}$	$1.3^{+0.4}_{-0.3}$	$0.5^{+0.3}_{-0.1}$	$1.7^{+0.1}_{-0.1}$	$2.6^{+0.4}_{-0.3}$	781 766
<i>ns123190</i>	$1.8^{+0.4}_{-0.3}$	51^{+5}_{-6}	$5.9^{+0.6}_{-0.8}$	11^{+12}_{-6}	$0.9^{+0.6}_{-0.1}$	$1.4^{+0.3}_{-0.3}$	$0.5^{+0.3}_{-0.1}$	$1.7^{+0.1}_{-0.1}$	$2.7^{+0.3}_{-0.3}$	783 769
<i>ns130190</i>	$2.0^{+0.3}_{-0.5}$	54^{+5}_{-5}	$6.2^{+0.6}_{-0.6}$	10^{+17}_{-5}	$0.9^{+1.1}_{-0.1}$	$1.3^{+0.3}_{-0.3}$	$0.5^{+0.2}_{-0.2}$	$1.7^{+0.1}_{-0.1}$	$2.7^{+0.3}_{-0.4}$	782 772
Unrealistically large radius of the emitting area:										
<i>ns123100</i>	$1.9^{+0.4}_{-0.3}$	28^{+4}_{-3}	$3.3^{+0.5}_{-0.3}$	50^{+96}_{-28}	$1.1^{+1.0}_{-0.3}$	$1.5^{+0.3}_{-0.4}$	$0.6^{+0.3}_{-0.2}$	$1.7^{+0.1}_{-0.1}$	$2.7^{+0.4}_{-0.3}$	781 757
<i>ns130100</i>	$2.2^{+0.4}_{-0.3}$	32^{+3}_{-3}	$3.7^{+0.4}_{-0.4}$	71^{+162}_{-31}	$1.2^{+1.4}_{-0.2}$	$1.4^{+0.3}_{-0.4}$	$0.5^{+0.3}_{-0.2}$	$1.8^{+0.1}_{-0.1}$	$2.8^{+0.4}_{-0.3}$	796 775

Note. [†]The parameters of each thermal model are the effective temperature $T_s^\infty = T_s/(1+z_g)$, as measured by a distant observer, and the circumferential radius R of the NS thermally emitting area. The gravitational redshift $1+z_g$ is fixed at 1.21, when it matters. To distinguish between the two PLs, describing non-thermal emission of the pulsar and the PWN, their photon indices Γ and normalizations K are marked by respective subscripts. A common equivalent hydrogen column density N_{H} is shared between the pulsar and the PWN spectra. Best-fitting values are maximal-probability estimates with errors corresponding to 90 per cent credible intervals; all values are derived via the MCMC.

Table 3. X-ray fluxes, luminosities and efficiencies of the pulsar and the PWN.[†]

Thermal model	Bol. flux $\log F_{\text{bol}}^\infty$	Bol. lum. $\log L_{\text{bol}}^\infty$	PSR flux $\log F_{2-10\text{keV}}^{\text{psr}}$	PWN flux $\log F_{2-10\text{keV}}^{\text{pwn}}$	PSR lum. $\log L_{2-10\text{keV}}^{\text{psr}}$	PWN lum. $\log L_{2-10\text{keV}}^{\text{pwn}}$	PSR eff. $\log \eta_{2-10\text{keV}}^{\text{psr}}$	PWN eff. $\log \eta_{2-10\text{keV}}^{\text{pwn}}$
A couple of hot spots on the surface:								
<i>bb</i>	$-12.5^{+0.2}_{-0.1}$	$31.4^{+0.3}_{-0.2}$	$-13.48^{+0.07}_{-0.09}$	$-12.93^{+0.04}_{-0.05}$	$30.4^{+0.2}_{-0.1}$	$31.0^{+0.1}_{-0.1}$	$-4.6^{+0.2}_{-0.1}$	$-4.1^{+0.1}_{-0.1}$
The bulk of the NS surface:								
<i>nsa12</i>	$-12.2^{+0.2}_{-0.2}$	$31.8^{+0.5}_{-0.3}$	$-13.44^{+0.07}_{-0.09}$	$-12.94^{+0.04}_{-0.06}$	$30.5^{+0.3}_{-0.2}$	$31.0^{+0.3}_{-0.1}$	$-4.5^{+0.3}_{-0.2}$	$-4.0^{+0.3}_{-0.1}$
<i>nsa13</i>	$-12.2^{+0.2}_{-0.2}$	$31.8^{+0.6}_{-0.3}$	$-13.44^{+0.08}_{-0.09}$	$-12.94^{+0.04}_{-0.06}$	$30.5^{+0.5}_{-0.2}$	$31.0^{+0.4}_{-0.1}$	$-4.5^{+0.5}_{-0.2}$	$-4.0^{+0.4}_{-0.1}$
<i>ns1260</i>	$-12.1^{+0.2}_{-0.2}$	$31.8^{+0.6}_{-0.3}$	$-13.42^{+0.06}_{-0.10}$	$-12.95^{+0.04}_{-0.05}$	$30.6^{+0.4}_{-0.2}$	$31.1^{+0.5}_{-0.1}$	$-4.5^{+0.4}_{-0.2}$	$-4.0^{+0.5}_{-0.1}$
<i>ns123190</i>	$-12.0^{+0.1}_{-0.2}$	$32.2^{+0.5}_{-0.5}$	$-13.44^{+0.09}_{-0.08}$	$-12.95^{+0.04}_{-0.06}$	$30.6^{+0.4}_{-0.1}$	$31.0^{+0.4}_{-0.1}$	$-4.5^{+0.4}_{-0.1}$	$-4.1^{+0.4}_{-0.1}$
<i>ns130190</i>	$-12.0^{+0.2}_{-0.2}$	$32.2^{+0.7}_{-0.5}$	$-13.43^{+0.08}_{-0.09}$	$-12.94^{+0.04}_{-0.06}$	$30.6^{+0.4}_{-0.2}$	$31.1^{+0.7}_{-0.1}$	$-4.5^{+0.4}_{-0.2}$	$-4.0^{+0.7}_{-0.1}$
Unrealistically large radius of the emitting area:								
<i>ns123100</i>	$-11.7^{+0.3}_{-0.2}$	$32.5^{+0.8}_{-0.5}$	$-13.44^{+0.08}_{-0.09}$	$-12.96^{+0.05}_{-0.04}$	$30.7^{+0.6}_{-0.3}$	$31.2^{+0.5}_{-0.3}$	$-4.4^{+0.6}_{-0.3}$	$-3.9^{+0.5}_{-0.3}$
<i>ns130100</i>	$-11.2^{+0.3}_{-0.2}$	$33.1^{+0.8}_{-0.4}$	$-13.44^{+0.09}_{-0.08}$	$-12.97^{+0.05}_{-0.05}$	$30.8^{+0.6}_{-0.2}$	$31.3^{+0.6}_{-0.2}$	$-4.3^{+0.6}_{-0.2}$	$-3.8^{+0.6}_{-0.2}$

Note. [†]These are intrinsic, or unabsorbed, fluxes F and luminosities L of the pulsar and the PWN emission, derived using the same MCMC simulations as used to produce Table 2. For the thermal component, the bolometric fluxes and luminosities are given as seen by a distant observer. For non-thermal PL components, we chose a range of 2–10 keV. The efficiencies η of the pulsar and the PWN are ratios of the corresponding non-thermal luminosities to the total spin-down luminosity of the pulsar. Fluxes and luminosities are given in units of $\text{erg s}^{-1} \text{ cm}^{-2}$ and erg s^{-1} .

temperature $T_s^\infty \sim (5-7) \times 10^5 \text{ K}$ and circumferential radii $R \sim 3-27 \text{ km}$ (see Table 2). The credible intervals derived for radii are consistent with the expected radii of NSs. These models thus imply that the thermal spectral component of J0633 comes from the bulk of the NS surface.

It is worth discussing why the models considered in the above paragraph give similar parameters. Ho et al. (2008) show that the spectra of these models are very similar in the considered photon energy range (see their figs 12 and 14). This is partially due to the fact that X-ray emission of an NS with the dipole field is dominated by warmer regions around magnetic poles, where the magnetic field is almost radial. The rest of the surface is colder and virtually cannot be seen in X-rays. At the same time, variation of the magnetic field strength within a reasonable range of $10^{12}-10^{13} \text{ G}$ does not affect the fitting results significantly.

To conclude this part, the thermal emission of J0633 comes from either hot polar caps or the entire NS surface. In the latter case, the spectral analysis suggests that the magnetic axis should stay almost orthogonal to the line of sight during the NS rotation. Consequently, the angle between the magnetic and rotational axes can be close to either 0° (nearly aligned rotator) or 90° (nearly orthogonal rotator): the exact alignment or orthogonality is excluded by the detection of X-ray pulsations. This can naturally explain the absence of the radio emission. The latter is believed to be strongly beamed along the magnetic axis and its narrow beam just misses the observer when this axis remains nearly orthogonal during the rotation of J0633. The models of pulsar evolution predict both the alignment and counter-alignment of the magnetic and rotational axes but neither of these two possibilities has been convincingly justified by observations (see e.g. Arzamasskiy, Beskin & Pirov

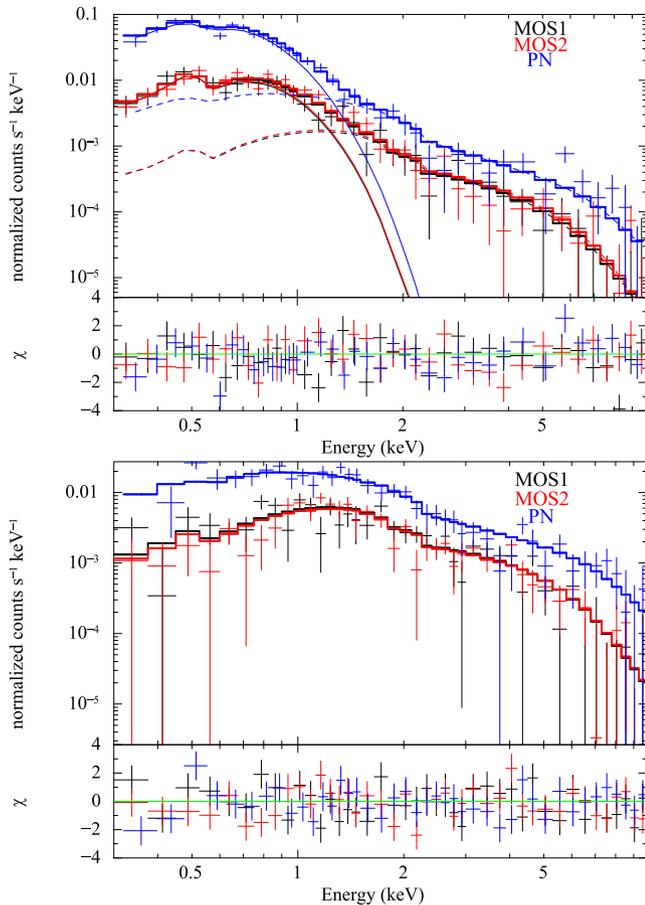


Figure 6. *Top:* XMM–Newton spectra of the J0633 pulsar. The best-fitting $bb+PL$ model (see text for details) is shown by the bold solid lines while the contributions of the bb and PL components are shown by thin solid and dashed lines, respectively. *Bottom:* XMM–Newton spectra of the J0633 PWN and the best-fitting PL model. The data from different instruments are shown by different colours. Spectra are grouped for illustrative purposes.

2017 and references therein). We cannot distinguish between the two cases either. Phase-resolved spectral analysis would be useful to distinguish between the blackbody and atmospheric models. However, the number of obtained EPIC-pn counts is not large enough to produce high signal-to-noise ratio spectra for these purposes.

5 DIFFUSE EMISSION

For the spectral analysis of the large-scale diffuse emission, we used the MOS data and the regions that are shown and numbered in the top right-hand panel of Fig. 2; the area inside the dashed box was used for the cosmic background. To extract the spectra and generate RMFs and ARFs, we applied an XMM-ESAS task MOS-SPECTRA. The spectrum of region 4 was obtained only from the MOS2 data since in the case of MOS1 it is partially projected on to the switched-off CCD. The MOS_BACK tool was used to create model QPB spectra that were then subtracted from the data. All spectra were binned to ensure at least 50 counts per energy bin.

We fitted the spectra from the background region and regions 1–4 together in XSPEC in the 0.3–10 keV energy range excluding 1.2–2 keV interval, which contains emission from the instrumental Al K α and Si K α lines. To account for the residual soft proton (SP)

Table 4. Best-fitting spectral model[†] of the cosmic background.

Temperature T_1 , keV	0.1 (fixed)
Normalization [‡] N_1 , cm ⁻⁵ arcmin ⁻²	$3.4^{+0.8}_{-0.9} \times 10^{-6}$
Temperature T_2 , keV	$0.14^{+0.02}_{-0.02}$
Normalization [‡] N_2 , cm ⁻⁵ arcmin ⁻²	$1.6^{+2.2}_{-0.7} \times 10^{-4}$
Temperature T_3 , keV	$0.61^{+0.17}_{-0.10}$
Normalization [‡] N_3 , cm ⁻⁵ arcmin ⁻²	$2.0^{+0.8}_{-0.8} \times 10^{-6}$
Photon index Γ	1.46 (fixed)
PL normalization K , ph s ⁻¹ cm ⁻² keV ⁻¹ arcmin ⁻²	$6.4^{+3.0}_{-3.0} \times 10^{-7}$
Column density N_H , cm ⁻²	6.5×10^{21} (fixed)
χ^2/N_{bins}	190/187

Notes. [†]MEKAL+(MEKAL+MEKAL+PL)×PHABS. Temperature T_1 and normalization N_1 are for LHB emission, T_2 and N_2 are for the Galactic halo, photon index Γ and normalization K are for cosmological sources and T_3 and N_3 are for the additional thermal component (see text). All errors are at 90 per cent confidence. N_{bins} is the number of spectral bins.

[‡]Normalization of the MEKAL model $N = \frac{10^{-14}}{4\pi D_{\text{cm}}^2} \int n_e n_H dV$, where n_e and n_H are the electron and hydrogen number densities, V is the volume of the emitting region and D_{cm} is the distance in centimeters.

contamination, we utilized PL components convolved with diagonal response matrices. The photon indices of these components were assumed to lie in the range of 0.1–1.4 (see Snowden & Kuntz 2014 for details) and linked for the MOS1 and MOS2 data; for each detector, we tied together normalizations for different regions taking into account appropriate scale factors generated by the PROTON_SCALE task.

The spectra of diffuse emission were fitted with PL models. The cosmic background parameters were linked for all spectra assuming solid angle scale factors provided by the PROTON_SCALE tool for each region. A model of the cosmic background usually includes several components: the unabsorbed thermal component with a temperature of about 0.1 keV from the Local Hot Bubble (LHB), the absorbed thermal component from the Galactic halo and the absorbed PL with $\Gamma = 1.46$ from unresolved cosmological sources (Snowden & Kuntz 2014). For the thermal components, we chose the optically thin plasma model MEKAL (Mewe, Gronenschild & van den Oord 1985). The LHB temperature was fixed at 0.1 keV, and we take the value of the column density of 6.5×10^{21} cm⁻² based on the Dickey & Lockman (1990) HI maps, obtained using the HEASARC N_H tool.¹⁰ Additional components may be necessary since J0633 has a low Galactic latitude ($b = -0^\circ.93$) (see e.g. Ogrea et al. 2013 and references therein). We found that inclusion of one more thermal component in the model improves the fit. In this case $\chi^2/\text{d.o.f.} = 936/858$ and the FTEST routine resulted in a probability of chance improvement of $\approx 7 \times 10^{-5}$; for the spectra of the cosmic background itself this value is $\approx 2 \times 10^{-3}$.

Best-fitting parameters for the astrophysical background are presented in Table 4, while parameters for the diffuse emission from regions 1–4 are given in Table 5. Each of the spectra of regions 1–4 is well fitted by a single PL model, thus demonstrating the pure non-thermal nature of the extended emission with almost similar photon indices. Examples of the observed spectra for regions 1 and 2 together with best-fitting models are presented in Fig. 7. As

¹⁰<https://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3nh/w3nh.pl>

Table 5. Best-fitting parameters for diffuse emission from regions 1–4.

Region	1	2	3	4
Column density N_{H} , 10^{21} cm^{-2}	$1.6^{+0.5}_{-0.4}$	$2.3^{+0.7}_{-0.7}$	$0.8^{+0.8}_{-0.6}$	$2.1^{+1.2}_{-0.9}$
Photon index Γ	$1.54^{+0.13}_{-0.12}$	$1.50^{+0.15}_{-0.15}$	$1.41^{+0.23}_{-0.21}$	$1.56^{+0.26}_{-0.23}$
PL normalization K , $10^{-5} \text{ ph s}^{-1} \text{ cm}^{-2} \text{ keV}^{-1} \text{ arcmin}^{-2}$	$4.7^{+0.7}_{-0.6}$	$6.8^{+1.4}_{-1.2}$	$2.5^{+0.7}_{-0.6}$	$2.8^{+1.0}_{-0.7}$
Area, arcmin ²	25	14	28	95
χ^2/N_{bins}	211/194	114/114	157/145	264/239

Note. Errors are at 90 per cent confidence. N_{bins} is the number of spectral bins.

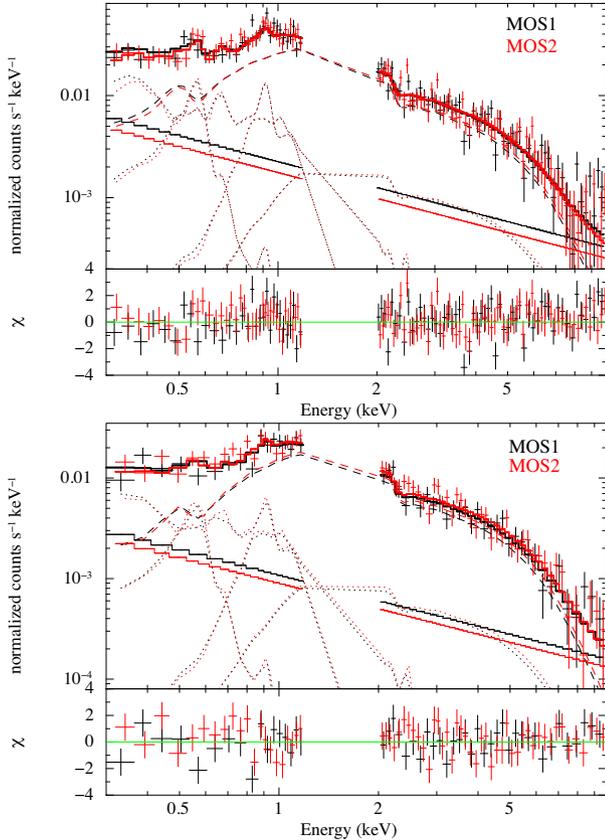


Figure 7. Observed spectra, best-fitting models and fit residuals for regions 1 (top) and 2 (bottom). The data from different instruments are shown by different colours. Solid bold lines show the best-fitting model (background + source); dotted lines show various components of the astrophysical background model; dashed lines are for PL components of the diffuse emission; finally, solid inclined lines show residual SP contamination.

seen, the fit residuals do not show any evidence of spectral features, confirming the above statement.

6 DISCUSSION

6.1 J0633 as a cooling NS

Assuming that the thermal emission of J0633 comes from the bulk of its surface, here we analyse the pulsar as a cooling NS. The respective analysis was done by Danilenko et al. (2015) based on the *Chandra* data obtained with a short exposure but it is worth a revision bearing in mind the better data quality obtained with *XMM-Newton*. We take the pulsar characteristic age, $t_c = 59.2 \text{ kyr}$, as a rough estimate of its true age t , and estimates of its surface

temperature obtained from the X-ray spectral fits. We adopt errors of ± 0.3 , in log scale, to represent a realistic uncertainty of the true age.

As discussed in Section 4, the surface temperature estimate depends on the thermal model used in the spectral fit. We explore here the results for T_s^∞ obtained utilizing models *ns123190* and *ns130190*, which assume the magnetic dipole axis to be perpendicular to the line of sight, since they provide reasonable values of the circumferential radius.

In Fig. 8, we compare J0633 with a sample of other cooling NSs, T_s^∞ and t of which are estimated from observations. The data are taken from table 1 of Beznogov & Yakovlev (2015). While the sample does not include all the relevant observational data on cooling NSs obtained to date, it is quite representative for stars with magnetic fields not large enough to significantly affect cooling. The upper blue point shows the J0633 temperature obtained with the *ns130190* model, which assumes a magnetic field at the pole of 10^{13} G . The lower one corresponds to the *ns123190* model, which describes an NS with a field of $1.82 \times 10^{12} \text{ G}$ at the pole. Both cases are relevant to J0633, since the spin-down dipole field estimate at the equator is $4.9 \times 10^{12} \text{ G}$. One can see that changing the magnetic field strength in reasonable limits does not significantly affect the position of J0633 in the plot. It appears to be rather cold but not exceptional among other cooling NSs of a similar age.

For a general overview of the cooling theory, we refer to Yakovlev & Pethick (2004) and Potekhin, Pons & Page (2015). Briefly speaking, at $t \gtrsim 100 \text{ yr}$, the NS interiors become almost isothermal (redshifted internal temperature is spatially constant), except for a thin outer layer, the heat blanketing envelope, whose properties define the relation between the surface and internal temperatures. The main cooling agents are the neutrino flow from the NS interiors (mainly from the core) and the photon flow from the surface, described by luminosities L_ν and L_γ , respectively. At $t \lesssim 10^5 \text{ yr}$, L_ν is much greater than L_γ (neutrino-cooling stage), while for older NSs photon cooling is the most effective (photon-cooling stage). If C is the total heat capacity of the star, its cooling rate depends on two ratios, L_ν/C and L_γ/C . L_ν and C mainly depend on the equation of state of the core matter and pairing properties of baryons in the core. L_γ depends on the heat-conducting properties of the outer envelope (heat blanket).¹¹ The physics of the heat blanket is well developed (e.g. Potekhin et al. 2003) and generally parametrized by the surface magnetic field at the pole, B_{pole} , and the mass of matter accreted on the envelope, ΔM . In the case of J0633, $B_{\text{pole}} = 9.8 \times 10^{12} \text{ G}$ (twice the equatorial field inferred from the spin-down), while ΔM is generally unknown and can vary from $\lesssim 10^{-17} M_\odot$ (iron envelope with lack of accreted material) to $\lesssim 10^{-7} M_\odot$ (fully accreted envelope). There are a lot

¹¹We do not discuss here the effects of strong internal magnetic field on cooling (e.g. Potekhin et al. 2015), since J0633 is not a magnetar.

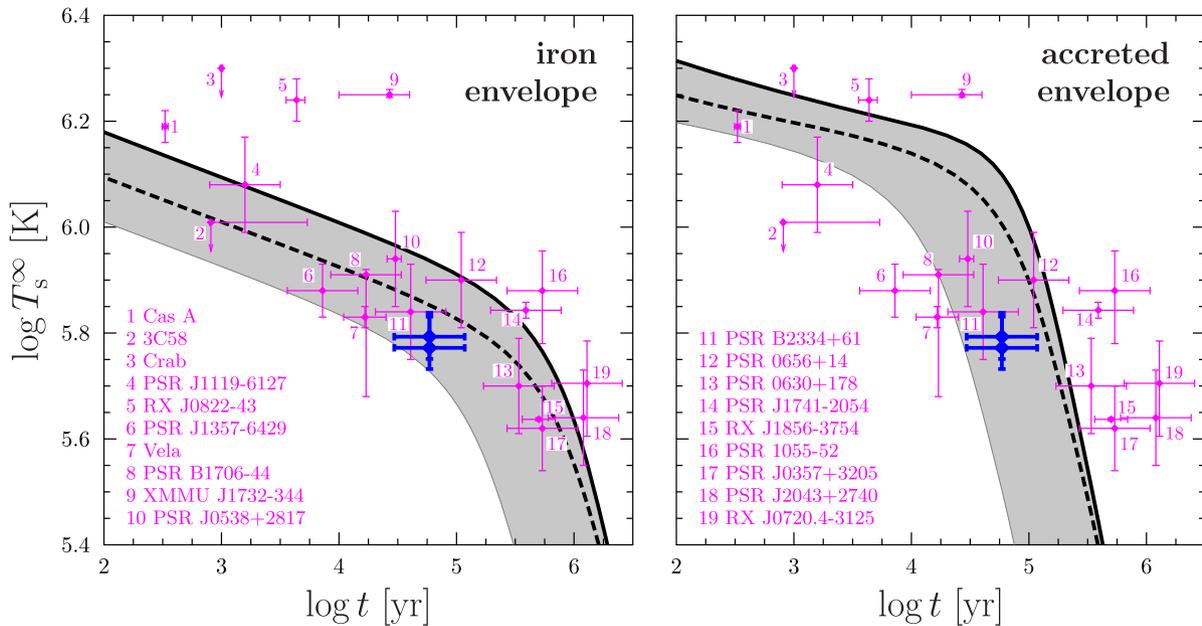


Figure 8. J0633 versus other cooling neutron stars and theoretical cooling scenarios for NSs with the iron (*left*) and accreted (*right*) heat blanket. The blue data points are the *ns123190* and *ns130190* atmospheric fits. Thick black curves show the standard cooling case (solid) and the cases with the neutrino luminosity 10 times (dashed). The grey area approximately shows the domain that superfluid cooling NSs can occupy below the standard cooling curve. See the text for details.

of controversial models of the equation of state and pairing. Instead of specifying one, we adopt the model-independent approach (e.g. Yakovlev et al. 2011), which accounts for these phenomena.

The so-called standard cooling scenario (Yakovlev et al. 2011) is plotted in both panels of Fig. 8 by solid black lines. In this scenario, the core is assumed to be nucleonic, with no baryon pairing and the direct Urca process being prohibited. The main process responsible for neutrino emission is therefore the modified Urca (MURca). The rapid increase of the cooling curve slope (‘the knee’) at $t \sim 10^5$ – 10^6 yr corresponds to transition from the neutrino-cooling to the photon-cooling stage. The luminosity L_ν and heat capacity C are calculated according to Ofengeim et al. (2017) for an NS with $M = 1.4 M_\odot$ and $R = 13$ km, which is consistent with the redshift $1 + z_g = 1.21$ adopted in the spectral analysis. The left-hand panel corresponds to an NS with the iron envelope, $\Delta M = 10^{-17} M_\odot$, while the right one is for $\Delta M = 10^{-7} M_\odot$, i.e. a fully accreted heat blanket. Note that MURca is treated here according to Friman & Maxwell (1979) whose approach has a lot of deficiencies (see e.g. Schmitt & Shternin 2018 for a comprehensive review). The most important lack in their work is that it does not account for in-medium effects. The first effect to account for is the momentum dependence of the in-medium nucleon propagator (Shternin, Baldo & Haensel 2018). Ultimately this makes L_ν up to ~ 10 times larger than that of Friman & Maxwell (1979). This case is shown by dashed lines in Fig. 8. There are several other in-medium effects (e.g. dressing of the virtual pion, see Voskresensky 2001), but we do not account for them here.

Nucleon pairing of different types (see Page et al. 2015 for a review) affects NS cooling in a complex way. Pairing of any type ultimately reduces the heat capacity with a realistic lower limit of $0.2 \times$ non-paired C . The neutron triplet pairing enhances the cooling rate L_ν/C up to a factor of 100 with respect to the standard cooling, due to the Cooper pairing neutrino emission. These pairing

effects are included in the minimal cooling paradigm (Gusakov et al. 2004; Page et al. 2004). In Fig. 8, the grey-shaded strip is a schematic representation of a domain occupied by the minimal cooling curves.

Notice that this paradigm also suggests that there are cooling scenarios with L_ν/C less than the standard value. The corresponding cooling curves are located above the solid black lines in Fig. 8. These cases are not relevant to J0633, and we do not consider them here.

One sees that the realistic fits of J0633 spectra are consistent with various cooling scenarios for both accreted and iron heat blanket models. J0633 can be either at the neutrino-cooling stage, with an iron heat blanket and the cooling rate L_ν/C significantly enhanced due to superfluidity or in-medium effects, or at the photon-cooling stage, with an accreted envelope and the heat capacity C essentially suppressed by neutron pairing.

Several notes have to be made after this. First, remember that the magnetic field inferred from pulsar timing is just an estimate accurate up to a factor of a few (e.g. Biryukov, Astashenok & Beskin 2017). Variation of the magnetic field within this uncertainty does not affect the surface temperature derived from the spectral fits. For instance, the two points marking the J0633 position in Fig. 8 correspond to atmosphere models whose magnetic fields differ by a factor of five, but their temperatures are consistent. We have also studied how such field variations can affect J0633 cooling, and found that this effect is insignificant. Secondly, we have not considered the direct Urca processes in the core (the so-called ‘rapid cooling’; e.g. Yakovlev & Pethick 2004), nor have we allowed any hyperons. In the case of the iron heat blanket, a treatment of the fits of J0633 in terms of hyperon or ‘rapid’ cooling can be relevant but quite tricky (e.g. Raduta, Sedrakian & Weber 2018; Negreiros et al. 2018), and these scenarios are beyond the scope of this paper. Finally, it is not enough to just explain a given NS by some specific

cooling scenario. The real challenge is to find a model that explains simultaneously all the set of cooling NSs shown in Fig. 8, but this is a much more complex task.

6.2 Diffuse emission

The J0633 position is projected on to a large shell-type SNR Monoceros loop (G205.5+0.5). It was estimated to be 30–150 kyr old (Welsh et al. 2001), which is in agreement with the J0633 characteristic age. The distance to the SNR is uncertain. Most estimates are about 1.6 kpc (e.g. Borka Jovanović & Urošević 2009), which is compatible with the distance to the Rosette nebula. It was assumed that these objects are interacting (see Xiao & Zhu 2012 and references therein). However, two new estimates of the distance to the SNR appeared recently: Zhao et al. (2018) obtained 1.98 kpc (and 1.55 kpc to the Rosette nebula) while Yu et al. (2019) derived 0.94 or 1.26 kpc. These new estimates are apparently not consistent with the idea of any interaction between the remnant and the nebula.

We checked whether the large-scale diffuse emission seen by *XMM-Newton* has a thermal origin, i.e. whether it may be attributed to the Monoceros loop SNR. Using the MEKAL model instead of the PL resulted in temperatures of $\gtrsim 10$ keV for all the regions. They are too large for the thermal emission of an evolved SNR such as the Monoceros loop. Therefore, the non-thermal origin of the emission seems to be more favourable.

Using various sky surveys, we found that the X-ray diffuse emission is projected on the edge of an extended clump detected in different bands: Effelsberg 11 and 21 cm radio continuum surveys of the Galactic plane (Furst et al. 1990; Reich, Reich & Furst 1997), the Sino-German $\lambda 6$ cm polarization survey of the Galactic plane¹² (Gao et al. 2010), the 4.85 GHz Sky Survey¹³ (Condon et al. 1994), the IRAS Galaxy Atlas¹⁴ (IGA; 60 and 100 μm , Cao et al. 1997), the Southern H-Alpha Sky Survey Atlas¹⁵ (SHASSA, Gaustad et al. 2001), the INT Photometric H α Survey of the Northern Galactic Plane¹⁶ (IPHAS; filters *r* and H α , Drew et al. 2005), the Second Palomar Observatory Sky Survey¹⁷ (POSS-II; red and blue plates, Lasker et al. 1996), *Spitzer* Galactic Legacy Infrared Midplane Survey Extraordinaire 360 (GLIMPSE360; 4.5 μm)¹⁸ (Whitney et al. 2011). In the case of the IPHAS data, stacked images were created using the CASUTOOLS¹⁹ MOSAIC command. The H α image of the Monoceros loop SNR is shown in the top left-hand panel of Fig. 9. The enlarged H α image of better spatial resolution, as well as 60- μm and 4.85-GHz images overlaid with contours of the extended emission revealed by *XMM-Newton*, are shown in the top right-hand and bottom panels of Fig. 9.

Optical emission of the clump can be produced by recombination lines of hydrogen, helium and carbon. The clump therefore may be a small dense cloud of interstellar matter. Thus, a likely origin of the

emission from regions 3–4 is the interaction of particles accelerated in the shocks of the Monoceros loop with this cloud. The distance to the X-ray diffuse emission estimated using an $N_{\text{H}}-D$ relation is compatible with the lower estimate of the distance to the SNR. The situation may be similar to that of SNR RX J1713.7–3946, where the hard non-thermal X-ray features were assumed to be the result of interaction between dense molecular clumps and SNR shock waves (Sano et al. 2013). SNR shock–cloud interactions can amplify magnetic field around clumps, which enhances X-ray emission around them (Inoue et al. 2012; Sano et al. 2013).

Extended emission in region 1 can be attributed to the fainter part of the PWN, i.e. shocked pulsar wind and shocked interstellar medium (ISM). PWNe spectra usually steepen with distance from a pulsar due to radiative losses of electrons. However, the J0633 PWN photon indices are in agreement, within uncertainties, with indices obtained for regions 1–4 (see Tables 2 and 5). The derived values are also in agreement with those obtained from *Chandra* data by Danilenko et al. (2015), though their best-fitting indices are lower, that is, $\Gamma = 1.2\text{--}1.3$, depending on the spectral model of the PSR+PWN system. *XMM-Newton* has broad point spread function (PSF) wings, so the spectrum of the PWN in the pulsar vicinity may be somewhat softened by the pulsar emission contamination. Thus some steepening cannot be excluded though it is not enough to obtain typical values of photon indices in the case of synchrotron cooling ($\Gamma > 2$).

There are some other PWNe where the same situation occurs. For instance, the photon indices of the tails of PSRs J1509–5850 and J0357+3205 do not show a significant dependence on distance from the pulsars, and the photon indices of the tails of PSRs B0355+54 and J1741–2054 show only a hint of synchrotron cooling (see e.g. Reynolds et al. 2017 and references therein). This may indicate an additional acceleration of particles within a tail. An alternative explanation is a high velocity of the outflowing matter and/or a low magnetic field (Reynolds et al. 2017).

The elongated X-ray feature (region 2) may have various origins. Its orientation, almost transverse to the presumed pulsar proper motion, allows us to suggest that the feature may be an outflow misaligned from the pulsar as seen, for example, in the Lighthouse nebula (see e.g. Pavan et al. 2016). Alternatively, it can be explained in the same way as emission in regions 3–4, and that seems like a more favourable explanation because of a remarkable spatial coincidence between the X-ray emission seen in region 2 and the clump material revealed in various spectral bands, as can be guessed from Fig. 9.

In Fig. 9, we also indicate HAWC J0635+070, which was proposed as a TeV halo of J0633 (Brisbois et al. 2018). However, its centre is shifted significantly from the pulsar position and thus its nature is still in question. It is interesting that in the *XMM-Newton* images (Fig. 2) there is some weak north-east protrusion, better seen in the hard 2–7 keV band, which directs to the TeV source and might indicate the association with it.

It was mentioned above that the characteristic age of J0633 and the Monoceros loop age are compatible. Nothing, therefore, would stop us from wondering if they are associated. If the pulsar was actually born somewhere near the centre of the Monoceros loop it would move approximately in the direction shown by the solid black arrow (2) in Fig. 10, which does not follow the PWN extension at all. However, there are many examples of similar misalignment, e.g. the Lighthouse nebula mentioned above, and this would not therefore contradict the association. Meanwhile, we have repeated *Chandra* observations of J0633 to measure its proper motion (Danilenko, Karpova & Shibano 2019). The pulsar’s proper motion direction

¹²11, 21 and 6 cm images are available at <https://www3.mpifr-bonn.mpg.de/survey.html>.

¹³4.85 GHz images are available at <https://skyview.gsfc.nasa.gov/current/cgi/query.pl>.

¹⁴<https://irsa.ipac.caltech.edu/applications/IRAS/IGA/>

¹⁵<http://amundsen.swarthmore.edu/SHASSA/>

¹⁶<http://www.iphas.org/>

¹⁷POSS-II data in digitized form are available at http://stdatu.stsci.edu/cgi-bin/dss_form.

¹⁸GLIMPSE data are available at <https://irsa.ipac.caltech.edu/data/SPITZER/GLIMPSE/>.

¹⁹<http://casu.ast.cam.ac.uk/surveys-projects/software-release> CASUTOOLS

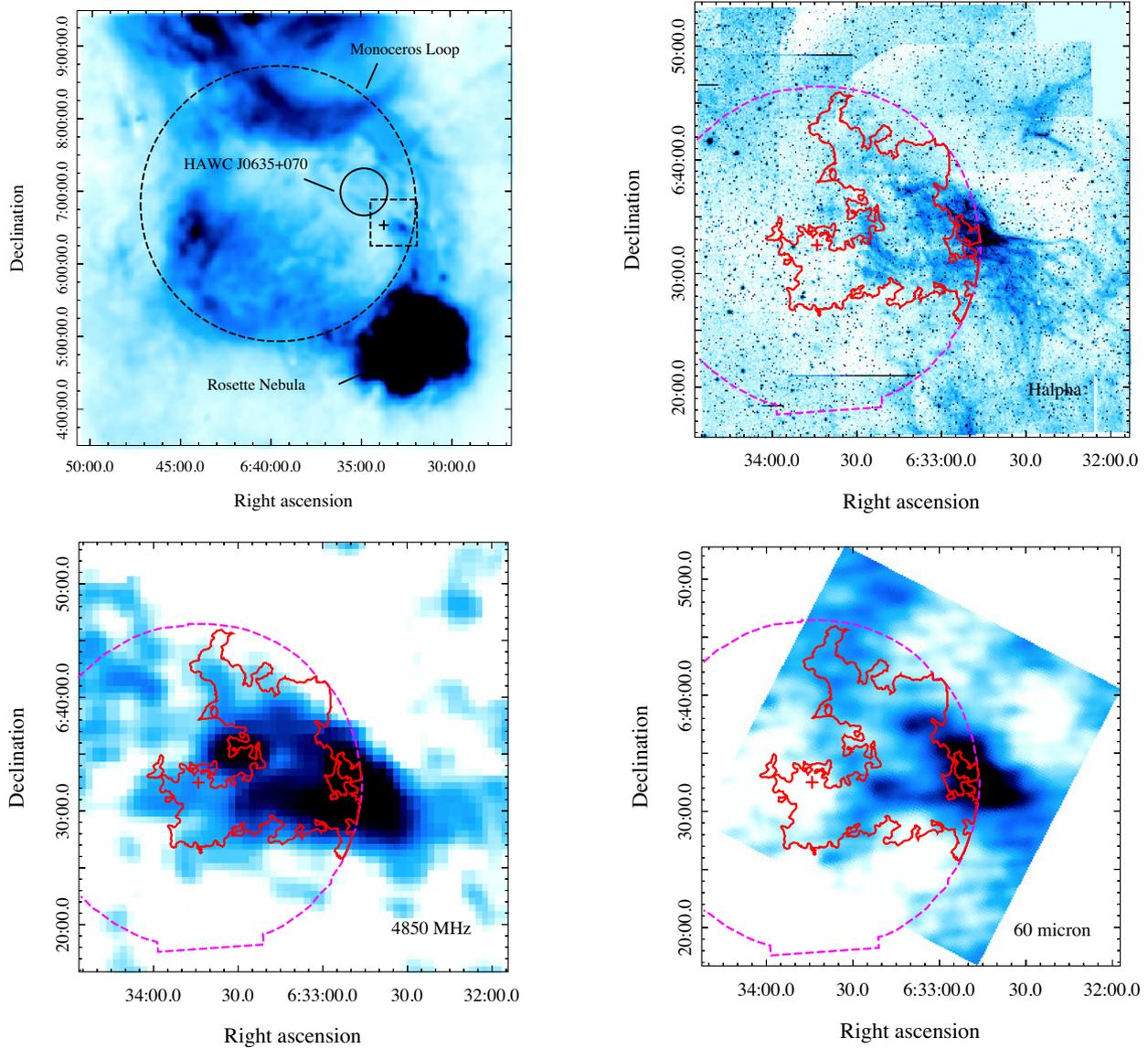


Figure 9. *Top left:* $H\alpha$ image of the Monoceros loop region taken from SHASSA. The Monoceros loop SNR is marked by the dashed circle with a diameter of $\approx 4^\circ$. The solid circle indicates the position (RA = $98^\circ.71$, Dec. = $+7^\circ.00$) and a Gaussian 1σ extent ($0^\circ.65$) (Brisbois et al. 2018) of HAWC J0635+070. The Rosette nebula is also labelled. The dashed box with sizes of $\approx 38 \times 38$ arcmin marks the region, enlarged in other panels, in which images obtained from different surveys are shown: IPHAS (*top right*), 4.85 GHz Sky Survey (*bottom left*) and the IRAS Galaxy Atlas (*bottom right*). XMM–Newton contours of diffuse emission are overlaid (contours correspond to intensity of $9 \text{ counts s}^{-1} \text{ deg}^{-2}$ in the 0.4–7 keV band). The J0633 position is shown by the ‘+’ symbol. The XMM–Newton combined MOS1+MOS2 FOV is indicated by the dashed line.

and uncertainties are shown by solid and dashed grey arrows in Fig. 10. It follows from these still-preliminary results that the pulsar is hardly associated with either the Monoceros loop or the Rosette nebula. Fortunately, we found another possible birth site, an open stellar cluster Collinder 106 (Danilenko et al. 2019).

7 SUMMARY

We analysed the XMM–Newton observations of the J0633 γ -ray pulsar. We confirmed previous investigations (Ray et al. 2011; Danilenko et al. 2015) that the pulsar spectrum contains thermal and non-thermal components. The former can be equally well fitted by either the blackbody or magnetized neutron star atmosphere models. In the first case, the emission comes from hotspot(s), presumably

pulsar polar caps, and, in the second case, it may originate from the entire NS surface. The derived spectral parameters of the pulsar and its PWN are in general agreement, within uncertainties, with those obtained from the *Chandra* data (Danilenko et al. 2015), uncertainties here being significantly smaller. However, new data do not confirm the absorption feature in the J0633 spectrum. Its apparent presence in the *Chandra* data remains puzzling. It could be either a time-variable feature or an unknown instrument artefact. Using the interstellar extinction–distance relation, we better, compared to previous studies, constrained the distance to the pulsar, 0.7–2 kpc.

We discovered X-ray pulsations from the pulsar. The pulse profile is broad and sinusoidal as expected for thermal emission modulated by NS rotation. The pulsed fraction in the 0.3–2 keV band is

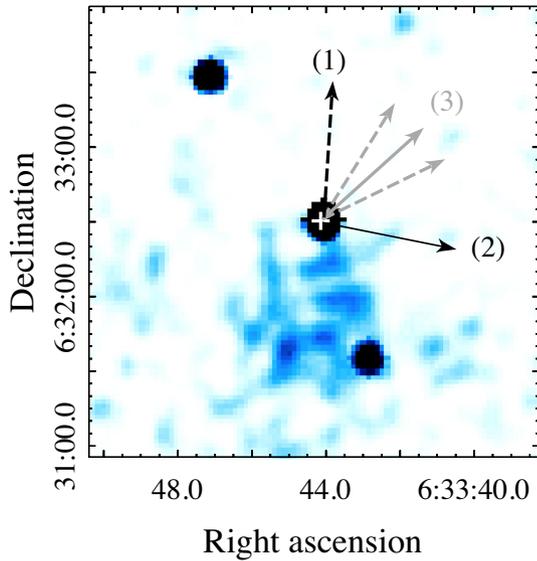


Figure 10. *Chandra* image of the J0633 vicinity. The pulsar position is marked by the cross. The dashed black arrow (1), the same as the one shown in the left-hand panel of Fig. 1, is the proper motion direction presumed from the PWN extension. The solid black arrow (2) shows the approximate direction in which the pulsar would be moving if it had been born near the centre of the Monoceros loop. Solid and dashed grey arrows (3) represent preliminary measurements of the pulsar proper motion and its uncertainties, done by means of repeated *Chandra* observations of J0633 (Danilenko et al. 2019).

23 ± 6 percent and its upper limit in the 2–10 keV range is <30 percent.

We analysed the cooling stage of the NS, accepting that the thermal emission is coming from the bulk of its surface with the effective temperature $T_s^\infty \approx 6 \times 10^5$ K, as shown by spectral fits. This result is quite insensitive to possible variations of the J0633 magnetic field (within a reasonable range near the spin-down value). Depending on the cooling scenario, J0633 could be either at the neutrino-cooling stage, with the cooling rate significantly enhanced by nucleon superfluidity or in-medium effects, or at the photon-cooling stage, if it has an accreted envelope and the heat capacity in its core essentially suppressed by neutron pairing.

Beside J0633 and its PWN, the *XMM-Newton* observations revealed weak large-scale diffuse emission south, west and north-west of the pulsar. The part of this emission adjacent to the PWN may be attributed to the fainter emission of the shocked pulsar wind and shocked ISM. The brighter feature, elongated almost transverse to both the PWN extent and the preliminary direction of the pulsar proper motion measured recently by Danilenko et al. (2019), may be a misaligned outflow from the pulsar. The most favourable explanation for other parts of the diffuse emission located at larger angular distances from the pulsar is the interaction of particles accelerated in the shocks of the Monoceros loop SNR with the dense cloud of ISM detected in the radio, IR and optical bands.

Deep X-ray observations with better spatial resolution are needed to carry out the detailed spatial and spatially resolved spectral analysis of the large-scale diffuse emission. This may allow separation of the PWN emission from that caused by the interaction of the SNR shocks with a dense ISM. Time-resolved spectral analysis of different phases of the pulsar light curve obtained with better signal-to-noise ratio would allow one to establish whether its thermal

emission component comes from hot pulsar polar caps or from the cooler bulk of the NS surface.

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