

Electron and Exciton Spin Dynamics in Quantum Dots

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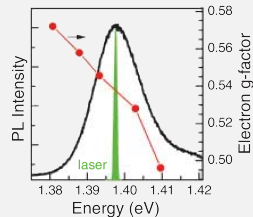
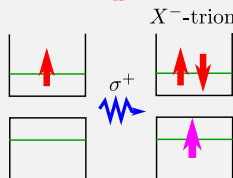
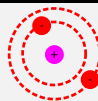
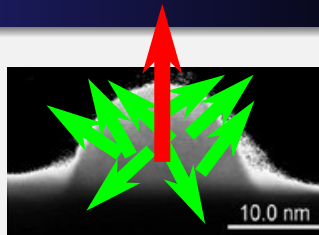
2nd International School on SpinOptronics, 13 July 2012

Why quantum dots?



n-type **single quantum dots** and quantum dot arrays

- Carrier localization leads to the spin relaxation **slowdown**
- Strong Coulomb interaction allows the **trion** formation
- Hyperfine** interaction of electron and nuclear spins is effective



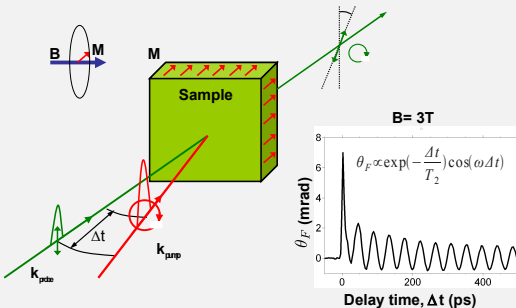
Element	^{27}Al	$^{69(71)}\text{Ga}$	^{75}As	^{115}In
Z	13	31	33	49
I	$5/2$	$3/2$	$3/2$	$9/2$

DICHROISM AND OPTICAL ANISOTROPY OF MEDIA WITH ORIENTED SPINS OF FREE ELECTRONS

A. G. Aronov and E. L. Ivchenko

Sov. Phys. Solid State
(1973)

A. F. Ioffe Physicotechnical Institute,
Academy of Sciences of the USSR, Leningrad



Faraday
rotation



Ellipticity



Pump: circularly
polarized pulse
orients carrier spins

$$S_z \neq 0 \Rightarrow \begin{cases} n_+ \neq n_- \\ \alpha_+ \neq \alpha_- \end{cases}$$

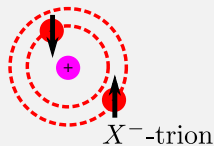
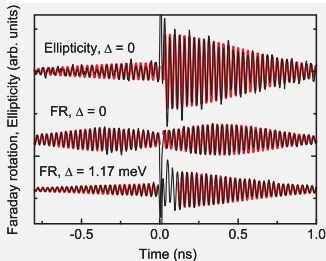
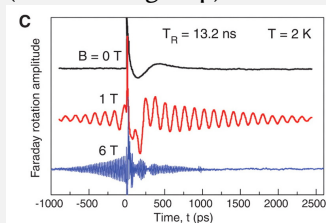
Faraday rotation

$$\Theta \propto S_z$$

- **Faraday Effect** (polarization plane rotation)
- **Ellipticity Effect** (appearance of the circular polarization)
- **Kerr Effect** (polarization plane rotation of reflected light)

InAs *n*-type quantum dots array

Experiment (Dortmund group):



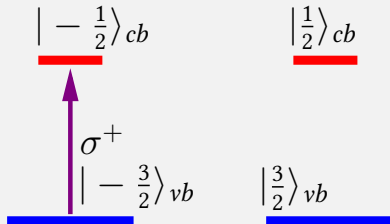
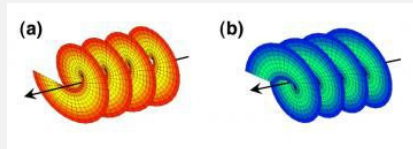
- 1 Origin of the Long-living signal at **singlet ($S = 0$)** trion excitation?
- 2 Signals at negative delays, i.e. **before the next pump pulse?**
- 3 Growth of Faraday rotation with time?



- 1 Introduction. Questions to theory
- 2 Interaction of light with spins
 - Optical orientation via trions
 - State-of-the-art in electron spin control
 - Supersensitive detection of spin polarization
- 3 Spin mode-locking effect
 - Phase synchronization condition & passive mode-locking
 - Nuclei-induced active mode-locking
- 4 Spin dynamics in equilibrium
- 5 Conclusions



Optical orientation is a transformation of the photon angular momentum to **the system of electron spins**



(normal light incidence)

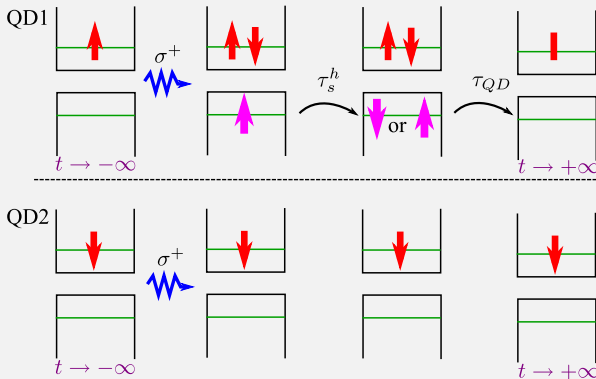
Semiconductor quantum well or self-organized quantum dot:

- at σ^+ pump $-\frac{3}{2} + 1 = -\frac{1}{2}$
i.e. $(e, hh) = (-1/2, 3/2)$
- at σ^- pump $\frac{3}{2} + (-1) = \frac{1}{2}$
i.e. $(e, hh) = (1/2, -3/2)$

Absorption of circularly polarized light

generates spin-polarized electrons and holes

Long-living electron spin polarization



σ^+ pump $\Rightarrow (-1/2e, 3/2h)$

The carriers with the spins opposite to those of photocreated electrons are picked out

Hole spin relaxation/fast spin precession (@ $B \neq 0$) $\Rightarrow$ spin of returning electron is negligible

Resident electrons become spin polarized after recombination

Spin pumping in quantum dots



Only QDs with a **certain spin projection** interact with the **circularly polarized light**

Technical details:

- Short pump pulse: $\tau_p \ll \tau_{QD}, 2\pi/\Omega_L$
- Four level model: two ground states $\psi_{\pm 1/2}$, two excited states $\psi_{\pm 3/2}$

$$i\hbar\dot{\psi}_{1/2} = V_+^*(t)\psi_{3/2},$$

$$i\hbar\dot{\psi}_{3/2} = \hbar\omega_0\psi_{3/2} + V_+(t)\psi_{1/2},$$

$$V_{\pm}(t) = - \int d(\mathbf{r}) E_{\sigma\pm}(\mathbf{r}, t) d^3r$$

- Returning electron is depolarized

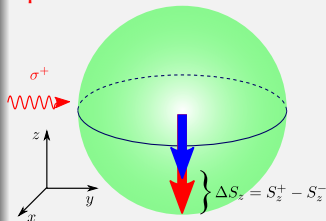
Under σ^+ pump the wave function transforms as

$$\psi_{1/2}(t \rightarrow +\infty) = Q e^{i\Phi} \psi_{1/2}(t \rightarrow -\infty)$$

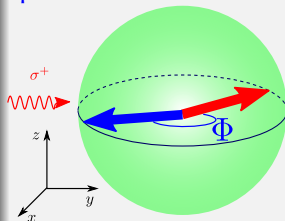
$$\psi_{-1/2}(t \rightarrow +\infty) = \psi_{-1/2}(t \rightarrow -\infty)$$

Similar to N. Rosen & C. Zener (1932)

Spin orientation



Spin rotation



Spin pumping in quantum dots



Only QDs with a **certain spin projection** interact with the circularly polarized light

$$\text{Electron spin } S = \frac{1}{2} \langle \psi | \boldsymbol{\sigma} | \psi \rangle$$

$$S_z^+ = \frac{Q^2 + 1}{2} S_z^- + \frac{Q^2 - 1}{4}$$

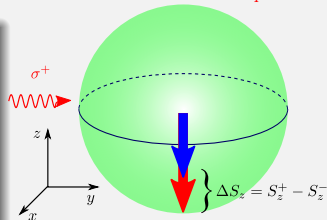
$$S_y^+ = Q \cos \Phi S_y^- - Q \sin \Phi S_x^-$$

$$S_x^+ = Q \cos \Phi S_x^- + Q \sin \Phi S_y^-$$

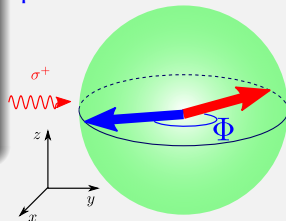
- Before pump pulse S^- , after S^+
- An increase of spin z-component
- In-plane components rotation

Yugova, MMG, Ivchenko, Efros (2009)

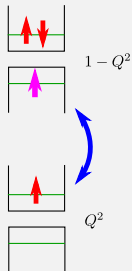
Spin orientation $\sim \frac{Q^2 - 1}{4}$



Spin rotation $\sim \Phi$



Spin rotation by the optical pulse



Circular pulse

- generates spin coherence (optical orientation)
- rotates spin (inverse Faraday effect)

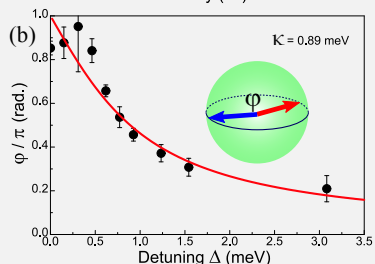
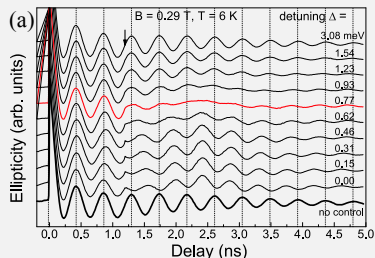
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$$S_y^+ = Q \cos \Phi S_y^- - Q \sin \Phi S_x^-$$

$$S_x^+ = Q \cos \Phi S_x^- + Q \sin \Phi S_y^-$$

Phys. Rev. B **80**, 104436 (2009)

Parameters Q and Φ are determined by the pump pulse intensity, duration and **detuning** from the resonance (Φ)



A. Grelich et al. (2009): InGaAs QDs
C. Phelps et al. (2009): CdTe QWs

Details in next talk by A. Ramsay



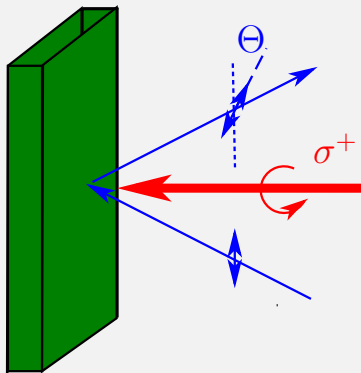
Circularly polarized pulses being resonant with the singlet trion transition orient electron spins in quantum dots

Slightly off-resonant pulse rotates spins

Effects of the probe



QW or ensemble of QDs or QWRs



Ellipticity and Faraday rotation

$$\mathcal{E} + i\mathcal{F} \propto r_+ - r_-$$

Probe: transmission/reflection of weak linearly-polarized pulse
weak=does not affect spin coherence

$$\updownarrow = \curvearrowright + \curvearrowleft$$

$r_+ \neq r_- \Rightarrow$ **rotation** of the linear polarization plane of the probe pulse and **appearance** of its ellipticity

Resonance (trion, exciton, ...)

$$r_{\pm}(\omega) = \frac{i\Gamma_{0,\pm}}{\omega_{0,\pm} - \omega - i(\Gamma_{0,\pm} + \Gamma_{\pm})}$$

$$t_{\pm} = 1 + r_{\pm}$$

Zhukov, Yakovlev, Bayer, MMG, Ivchenko, et al. (2007)

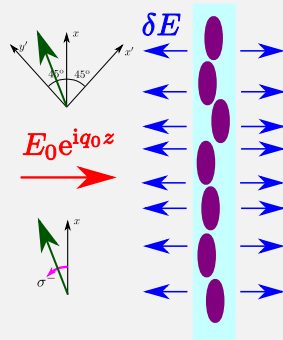


- **Faraday Effect** (polarization plane rotation)

$$\mathcal{F} = \lim_{z \rightarrow +\infty} \int_{-\infty}^{\infty} \left[|E_{x'}^{(t)}(z, t)|^2 - |E_{y'}^{(t)}(z, t)|^2 \right] dt$$

- **Ellipticity Effect** (appearance of the circular polarization)

$$\mathcal{E} = \lim_{z \rightarrow +\infty} \int_{-\infty}^{\infty} \left[|E_{\sigma^-}^{(t)}(z, t)|^2 - |E_{\sigma^+}^{(t)}(z, t)|^2 \right] dt$$



Probe induced field

$$\delta \mathbf{E}(t) = -4\pi \left(\frac{\omega_{\text{pr}}}{c} \right)^2 \frac{i e^{iq|z|}}{2q} N_{\text{QD}}^{2d} \mathbf{\Pi}(t)$$

$$\Pi_x \propto (n_e - n_{tr}) E_x^{\text{probe}}$$

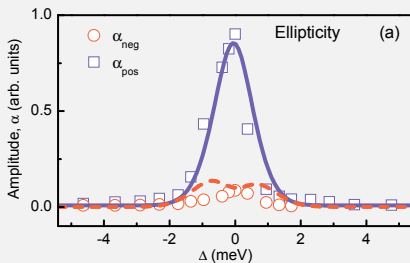
$$\Pi_y \propto (S_z - J_z) E_x^{\text{probe}}$$

Spectral function

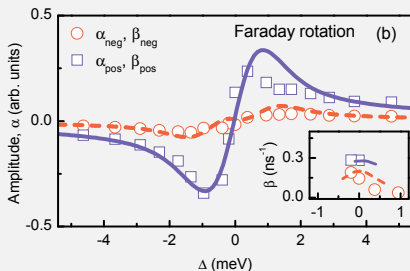
$$\mathcal{E} + i\mathcal{F} \propto$$

$$\int_{-\infty}^{\infty} dt \int_{-\infty}^t dt' f(t) f(t') e^{i\Delta(t-t')}$$

$$\Delta = \omega_{\text{pr}} - \omega_0; E_{\text{pr}} \propto f(t) e^{-i\omega t}$$



Linearly polarized pulse can readout spin polarization



Correct description is based on reflection/transmission rather than on dielectric constant

MMG, Yugova + Dortmund group (2010)



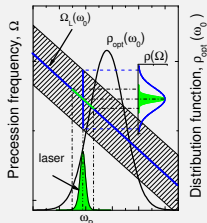
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Electron spin precession mode-locking



Train of pump and probe pulses, T_R is the repetition period

- Large spread of electron g -factors $\Rightarrow$ fast dephasing
- Signal reappears before the next pump pulse arrival

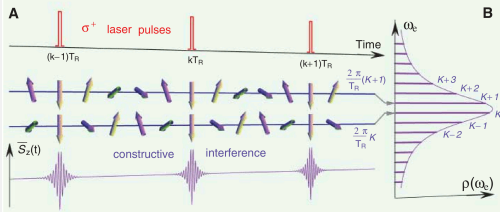
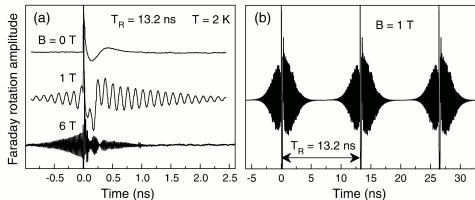


Resonant optical frequency, ω_0

$$\hbar/\tau_p \sim 1 \text{ meV}$$

$$\Omega T_R = 2\pi N$$

Constructive
interference
exp.: $N \sim 10^2$

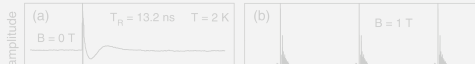
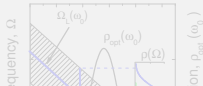


Electron spin precession mode-locking



Train of pump and probe pulses, T_R is the repetition period

- Large spread of electron g -factors $\Rightarrow$ fast dephasing
- Signal reappears before the next pump pulse arrival



“Passive” mode-locking:

all synchronized modes have same initial phases owing to the pump

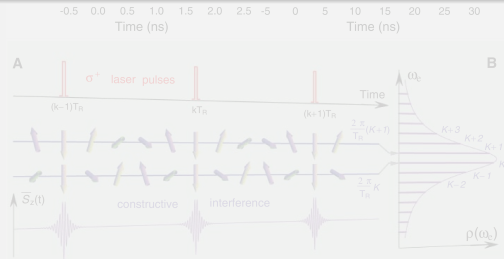


Resonant optical frequency, ω_0

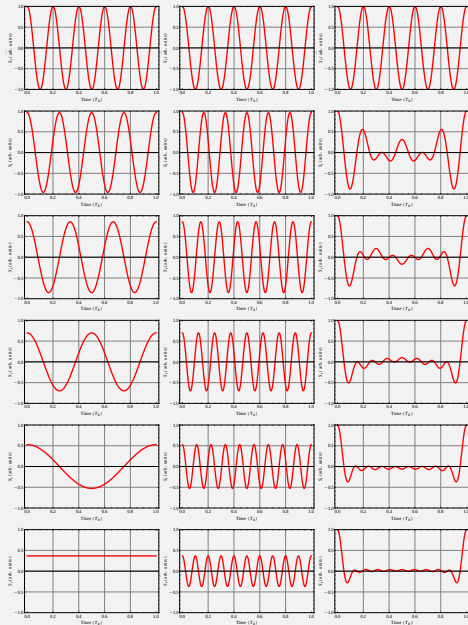
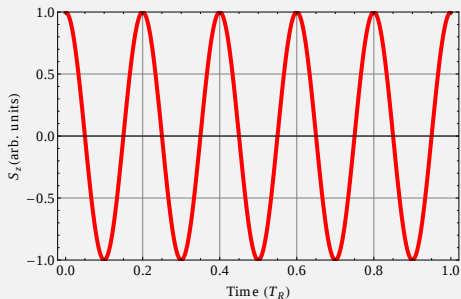
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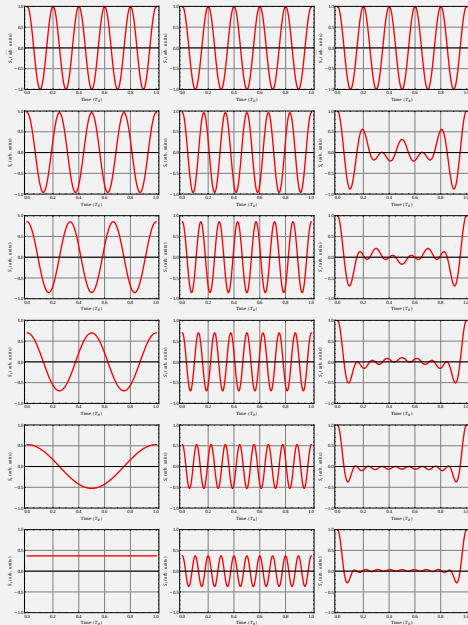
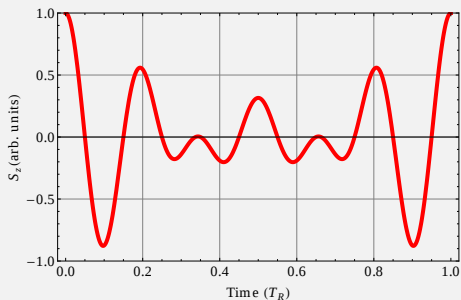
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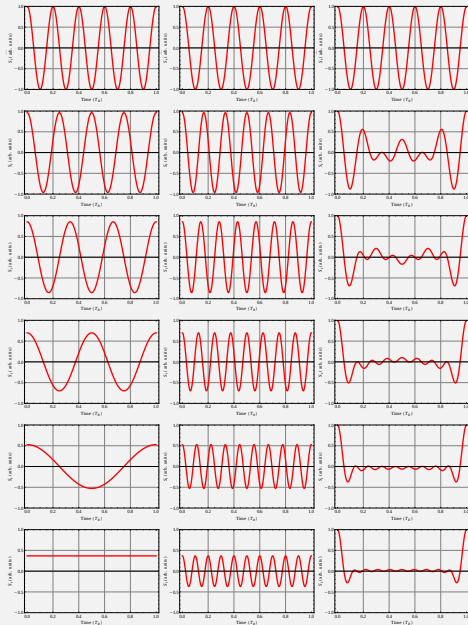
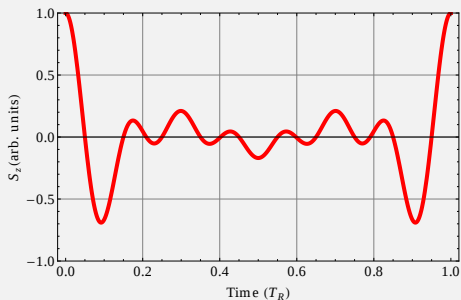
Electron spin precession modelocking – III



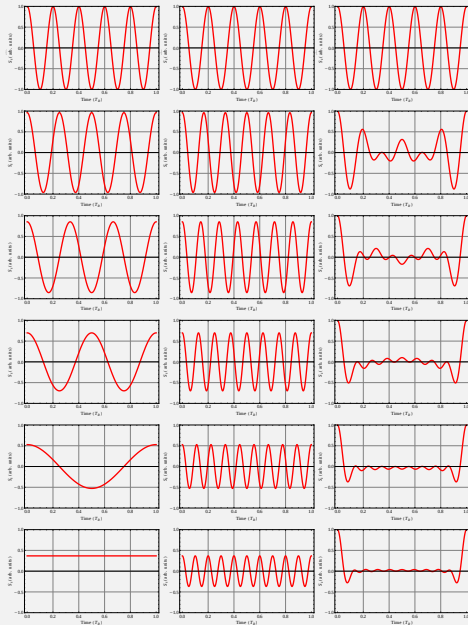
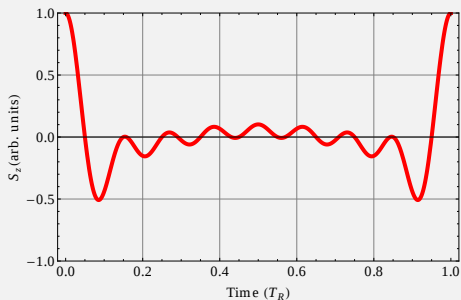
Electron spin precession modelocking – III



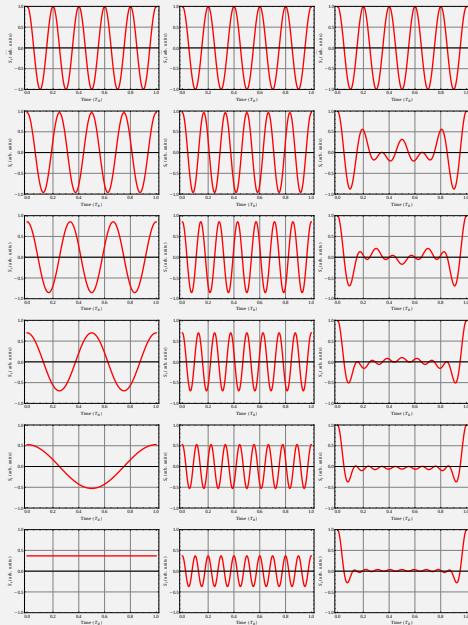
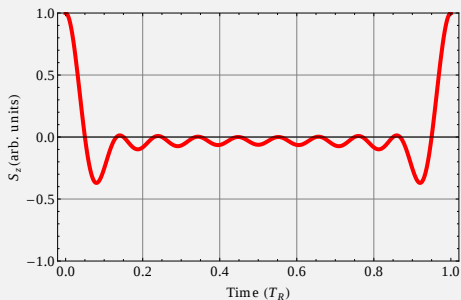
Electron spin precession modelocking – III



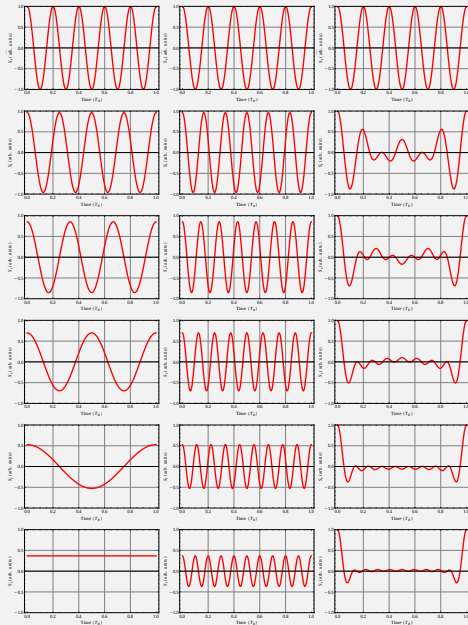
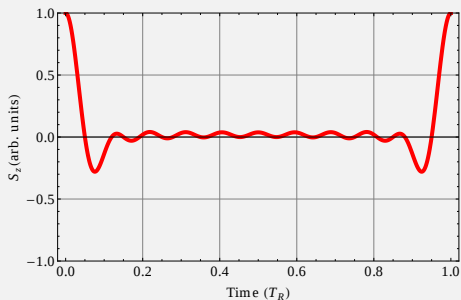
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Electron spin precession modelocking – III

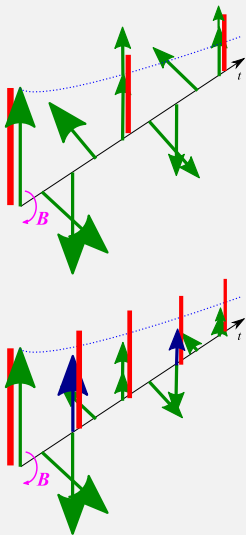




Where are **other spins** with frequencies $\Omega \neq \frac{2\pi N}{T_R}$?



Very high amplitude at negative delays

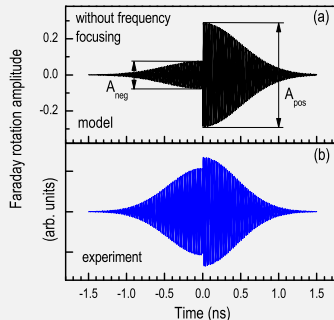


$$\Omega_{\text{eff}} T_R = 2\pi$$

↑
Nuclei-
induced
frequency
focusing



$$\Omega_{\text{eff}} T_R = \pi$$

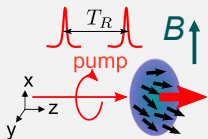


$$\Omega_{\text{eff}} = \Omega_L + \Omega_{\text{nucl}}$$

Feedback of nuclei is necessary

Nuclei-induced frequency focusing takes place

Greulich, Shabaev, Yakovlev, Efros, Yugova, Reuter, Wieck, Bayer (2007)



Nuclear spin polarization

$$\mathbf{m} = \sum_i \mathbf{I}_i$$

Spin precession between the pulses

$$\frac{d\mathbf{m}}{dt} = [\alpha \mathbf{S}(t) \times \mathbf{m}(t)] + [\boldsymbol{\omega} \times \mathbf{m}(t)],$$

$$\frac{d\mathbf{S}}{dt} = [\alpha \mathbf{m}(t) \times \mathbf{S}(t)] + [\boldsymbol{\Omega} \times \mathbf{S}(t)],$$

$$(n-1)T_R < t < nT_R$$

Pump pulse action: $\mathbf{m}^+ = \mathbf{m}^-$

$$S_z^+ = \frac{Q^2 + 1}{2} S_z^- + \frac{Q^2 - 1}{4}$$

$$S_y^+ = QS_y^-, \quad S_x^+ = QS_x^-$$

Time scales @ $B = 1$ T

- 1 Electron spin precession

$$\frac{2\pi}{\Omega} \lesssim 0.1 \text{ ns}$$

- 2 Precession in nuclear field

$$\frac{2\pi}{\alpha m} \sim 10 \text{ ns}$$

- 3 Pulse repetition period

$$T_R \sim 10 \text{ ns}$$

- 4 Nuclear spin precession

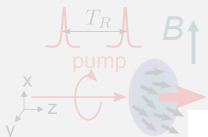
$$\frac{2\pi}{\omega} \lesssim 100 \text{ ns}$$

- 5 Precession in electron field

$$\frac{2\pi}{\alpha S} \gtrsim 10^3 \text{ ns}$$

MMG, Yugova, Efros (2012)

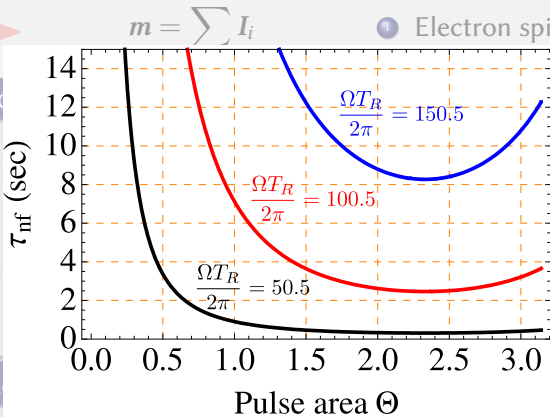
Classical origin of the focusing



Nuclear spin polarization

Time scales @ $B = 1 \text{ T}$

① Electron spin precession



$\lesssim 0.1 \text{ ns}$

in nuclear field

$\sim 10 \text{ ns}$

ation period

$\sim 10 \text{ ns}$

in precession

$\lesssim 100 \text{ ns}$

in electron field

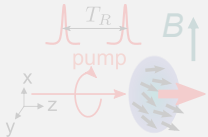
$$\frac{2\pi}{\alpha S} \gtrsim 10^3 \text{ ns}$$

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MMG, Yugova, Efros (2012)

Classical origin of the focusing



Nuclear spin polarization

$$m = \sum_i I_i$$

Spin precession between the pulses

$$dm = [\alpha S(t) \times m(t)] + [\gamma \times m(t)]$$

“Active” mode-locking:

spin precession frequencies are synchronized in all dots **thanks to nuclei**

$$dt$$

$$(n-1)T_R < t < nT_R$$

Pump pulse action: $m^+ = m^-$

$$S_z^+ = \frac{Q^2 + 1}{2} S_z^- + \frac{Q^2 - 1}{4}$$

$$S_y^+ = QS_y^-, \quad S_x^+ = QS_x^-$$

Time scales @ $B = 1$ T

- 1 Electron spin precession

$$\frac{2\pi}{\Omega} \lesssim 0.1 \text{ ns}$$

- 2 Precession in nuclear field

$$2\pi \gtrsim 10 \text{ ns}$$

- 4 Nuclear spin precession

$$\frac{2\pi}{\omega} \lesssim 100 \text{ ns}$$

- 5 Precession in electron field

$$\frac{2\pi}{\alpha S} \gtrsim 10^3 \text{ ns}$$

MMG, Yugova, Efros (2012)



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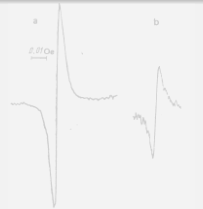
Magnetic resonance in the Faraday-rotation noise spectrum

E. B. Aleksandrov and V. S. Zapasskii

(Submitted 23 January 1981)

Zh. Eksp. Teor. Fiz. 81, 132–138 (July 1981)

A maximum at the magnetic resonance frequency of sodium atoms in the ground state is observed near the 5896 Å absorption line in the fluctuation spectrum of the azimuth of the polarization plane of light crossing a magnetic field in sodium vapor. The experiment is a demonstration of a new EPR method which does not require in principle magnetic polarization of the investigated medium, nor the use of high-frequency or microwave fields to induce the resonance.



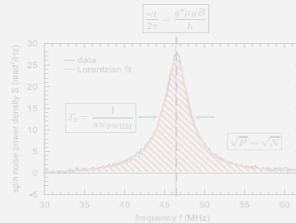
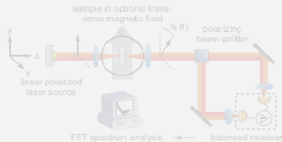
$$\langle \vartheta_{\mathcal{F}}(t) \vartheta_{\mathcal{F}}(t') \rangle,$$

Can spin dynamics be studied **without** any pump?

Semiconductor spin noise spectroscopy: Fundamentals, accomplishments, and challenges

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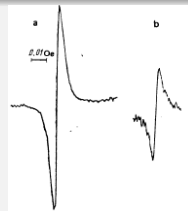
Magnetic resonance in the Faraday-rotation noise spectrum

E. B. Aleksandrov and V. S. Zapasskii

(Submitted 23 January 1981)

Zh. Eksp. Teor. Fiz. **81**, 132–138 (July 1981)

A maximum at the magnetic resonance frequency of sodium atoms in the ground state is observed near the 5896 Å absorption line in the fluctuation spectrum of the azimuth of the polarization plane of light crossing a magnetic field in sodium vapor. The experiment is a demonstration of a new EPR method which does not require in principle magnetic polarization of the investigated medium, nor the use of high-frequency or microwave fields to induce the resonance.

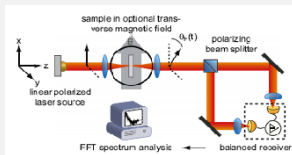


Invited review

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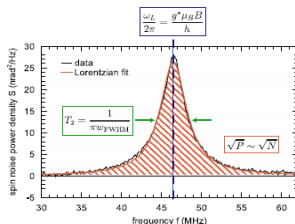
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$$\langle \vartheta_{\mathcal{F}}(t) \vartheta_{\mathcal{F}}(t') \rangle,$$

$$\langle \vartheta_{\mathcal{K}}(t) \vartheta_{\mathcal{K}}(t') \rangle \propto \langle S_z(t) S_z(t') \rangle$$



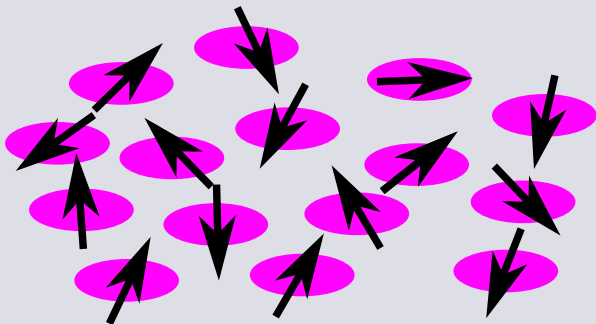


Single spin

$$\langle s_x \rangle = \langle s_y \rangle = \langle s_z \rangle = 0 \quad \text{but} \quad \langle s_x^2 \rangle = \langle s_y^2 \rangle = \langle s_z^2 \rangle = \frac{1}{3} \times \frac{1}{2} \left(1 + \frac{1}{2} \right)$$

Spin ensemble

$$\sqrt{\langle S_i^2 \rangle} = \sqrt{N} \sqrt{\langle s_i^2 \rangle} = \frac{\sqrt{N}}{2}$$

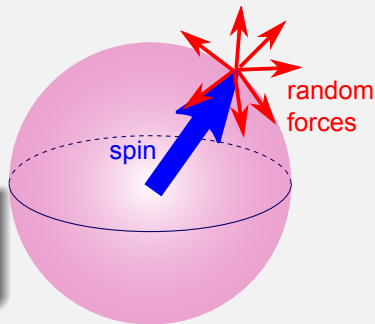




$$\frac{\partial \delta \mathbf{s}(t)}{\partial t} + \frac{\delta \mathbf{s}(t)}{\tau_s} + \delta \mathbf{s}(t) \times (\boldsymbol{\Omega}_B + \boldsymbol{\Omega}_N) = \boldsymbol{\xi}(t)$$

Random (Langevin) forces

$$\langle \xi_\alpha(t') \xi_\beta(t) \rangle = \frac{1}{2\tau_s} \delta_{\alpha\beta} \delta(t' - t)$$



Our task is to calculate

$$\langle s_\alpha(t) s_\beta(t') \rangle \quad \text{or} \quad (\delta s_\alpha \delta s_\beta)_\omega = \int_{-\infty}^{+\infty} \langle s_\alpha(t + \tau) s_\beta(t) \rangle e^{-i\omega\tau} d\tau$$

MMG, Ivchenko (2012)



Without field: $\dot{s}_j + \frac{s_j}{\tau_s} = \xi_j$

$$\langle \delta s_j^2 \rangle_\omega = \frac{2\tau_s \langle \delta s_j^2 \rangle}{1 + (\omega\tau_s)^2} = \frac{1}{2} \frac{\tau_s}{1 + (\omega\tau_s)^2}, \quad \langle \xi_j^2 \rangle_\omega = \frac{2\langle \delta s_j^2 \rangle}{\tau_s} = \frac{1}{2\tau_s},$$

since $\langle \delta s_j^2 \rangle = \langle s_j^2 \rangle - \langle s_j \rangle^2 = 1/4$.

In the presence of the field: $\left(-i\omega + \frac{1}{\tau_s}\right) \mathbf{s} + \mathbf{s} \times \boldsymbol{\Omega} = \boldsymbol{\xi}.$

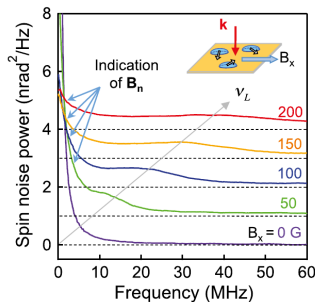
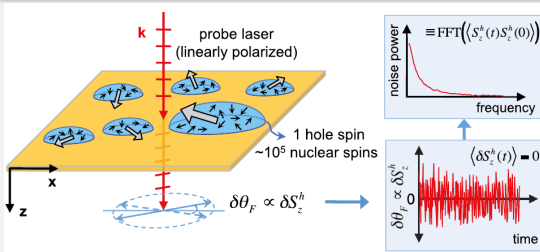
$\boldsymbol{\Omega} \parallel 3$ (axes: $1 \perp 2 \perp 3$):

$$\langle \delta s_1^2 \rangle_\omega = \langle \delta s_2^2 \rangle_\omega = \frac{\pi}{4} [\Delta(\omega - \Omega) + \Delta(\omega + \Omega)], \quad \langle \delta s_3^2 \rangle_\omega = \frac{\pi}{2} \Delta(\omega),$$

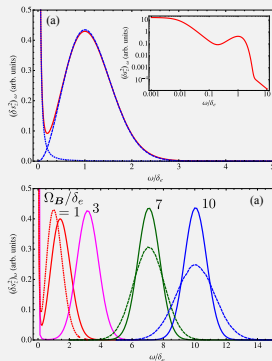
Lorentian form in strong enough magnetic fields ($\Omega\tau_s \gg 1$)

$$\Delta(\eta) = \frac{1}{\pi} \frac{\tau_s}{1 + (\eta\tau_s)^2}$$

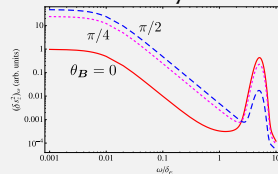
Singly charged quantum dot ensemble



Yan Li, Sinitsyn, Smith, Reuter, Wieck,
Yakovlev, Bayer, Crooker



Theory



MMG, Ivchenko (2012)



Coherent spin dynamics of electrons and excitons in nanostructures (a review),
Phys. Solid State 54, 1 (2012)

Spin noise in quantum dot ensembles, arXiv:1206.3479

Spin coherence generation and detection in spherical nanocrystals, arXiv:1205.2764

Plan

- 1 Introduction. Questions to theory
- 2 Interaction of light with spins
- 3 Spin mode-locking effect
- 4 Spin dynamics in equilibrium
- 5 Conclusions

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Dynamics and fluctuations of electron and nuclear spins can be most conveniently studied by optical means

Thank you for attention!