

Indirect Excitons

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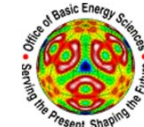
University of California Santa Barbara

Introduction:

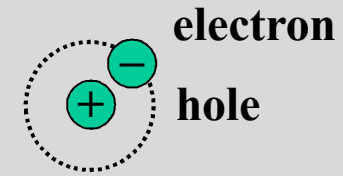
- **Cold exciton gas**
- **Indirect excitons**

Data:

- **Spatial ordering**
- **Spontaneous coherence**
- **Spin textures**
- **Phase singularities**
- **Condensation in a trap**



exciton – bound pair of electron and hole
light bosonic particle in semiconductor



$$\lambda_{dB} = \left(\frac{2\pi\hbar^2}{mk_B T} \right)^{1/2}$$

cold excitons



thermal de Broglie wavelength is comparable to separation between excitons

$$T_{dB} = \frac{2\pi\hbar^2}{mk_B} n$$

excitons in GaAs QW

$$n = 10^{10} \text{ cm}^{-2}, m_{exciton} = 0.2 m_e \rightarrow T_{dB} \sim 3 \text{ K}$$

how to realize cold exciton gas ?

$T_{lattice} \ll 1 \text{ K}$ in He refrigerators

finite lifetime of excitons can result to high exciton temperature: $T_{exciton} > T_{lattice}$

find excitons with lifetime \gg cooling time $\longrightarrow T_{exciton} \sim T_{lattice}$

estimates for characteristic temperatures for cold 2D Bose gases

for $n = 10^{10} \text{ cm}^{-2}$ per spin state ($< n_{Mott} \sim 1/a_B^2 \sim 10^{11} \text{ cm}^{-2}$), $M = 0.22 m_0$

λ_{dB} is comparable to interexcitonic separation

$$T_{dB} = \frac{2\pi\hbar^2 n}{Mk_B} \approx 3K \quad \lambda_{dB}^2 n = 1$$

thermal de Broglie wavelength

$$\lambda_{dB} = \left(\frac{2\pi\hbar^2}{Mk_B T} \right)^{1/2} \approx 160nm \quad \text{at } T = 1K$$

temperature of quantum degeneracy

$$T_0 = T_{dB} \approx 3K \quad N_{E=0} = \exp(T_{dB}/T) - 1$$

BEC in finite 2D system

$$T_{cS} = T_{dB} \frac{1}{\ln(nS)} \approx 0.3K \quad \text{for } N=nS \sim 10^5$$

temperature of onset of local superfluidity

$$T_c = T_{dB} \frac{1}{\ln \ln(1/na^2)} \approx 1.7K$$

Bogoliubov temperature
onset of nonzero order
parameter

$\ln \ln(1/na^2) = 1-3$ for $1/na^2 = 10-10^8$ for $\ln \ln(1/na^2) = 1.5$

Kosterlitz-Thouless temperature

$$T_{KT} \approx T_{dB} \frac{\ln \ln(1/na^2)}{1 + \ln \ln(1/na^2)} \approx 1K$$

pairing of vortices =
onset of macroscopic
superfluidity which
is not destroyed by
vortices

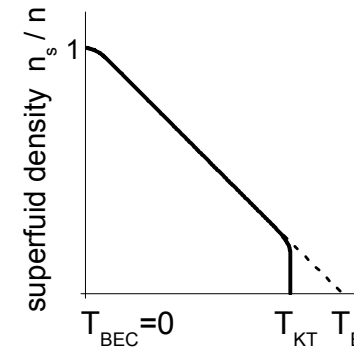
for not so dilute gas

$$T_c \approx T_{dB} \frac{1}{\ln(\xi/4\pi) + \ln \ln(1/na^2)} \approx 0.6K \quad \xi \approx 380$$

A.L. Ivanov, P.B. Littlewood, H. Haug,
PRB 59, 5032 (1999)

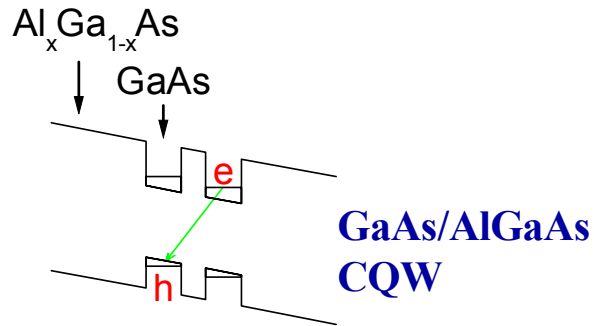
Y.M. Kagan, lectures
W. Ketterle, N.J. van Druten, PRA 54, 656 (1996)

V.N. Popov, Theor. Math. Phys. 11, 565 (1972)
D.S. Fisher, P.C. Hohenberg, PRB 37, 4936 (1988)



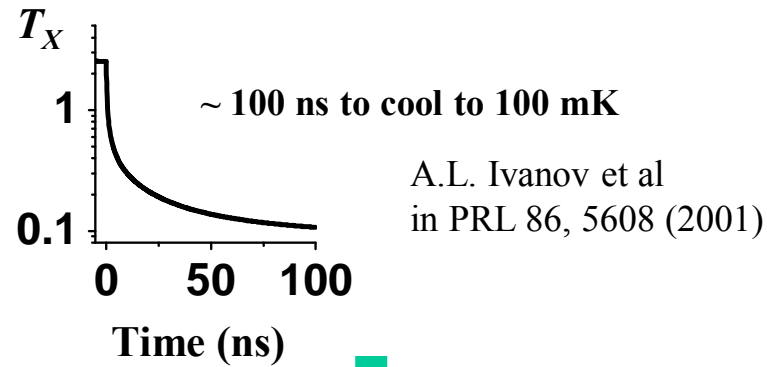
N. Prokof'ev, O. Ruebenacker, B. Svistunov,
PRL 87, 270402 (2001)

Indirect excitons in CQW



10³ – 10⁶ times longer exciton lifetime due to separation between electron and hole layers

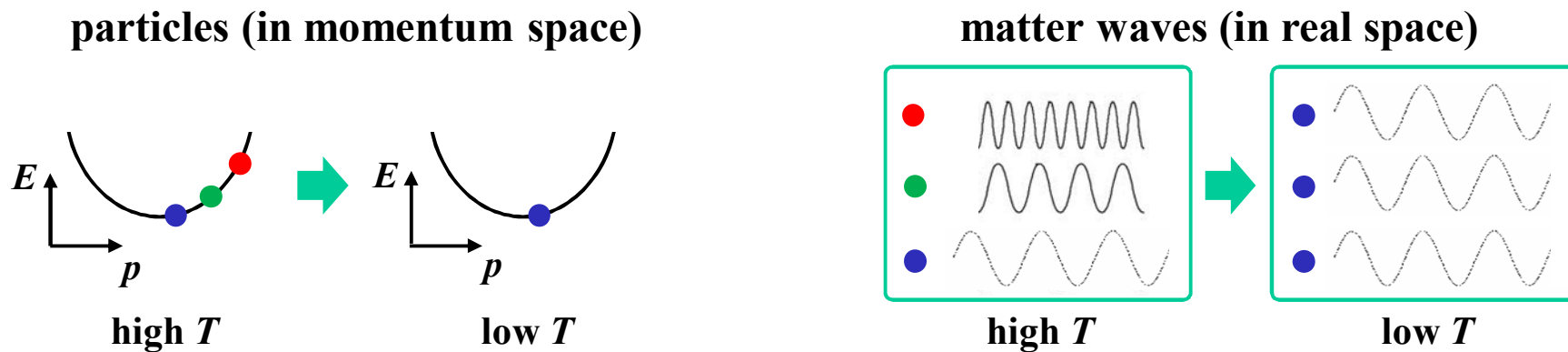
realization of cold exciton gas in separated layers was proposed by Yu.E. Lozovik, V.I. Yudson (1975); S. I. Shevchenko (1976); T. Fukuzawa, S.S. Kano, T.K. Gustafson, T. Ogawa (1990)



**$T_X \sim 100$ mK
is realized in experiments
30 times below T_{dB}**

Louis de Broglie, 1923: all forms of matter have wave as well as particle properties.
The wavelength of a matter wave associated with any moving object $\lambda = h/p$

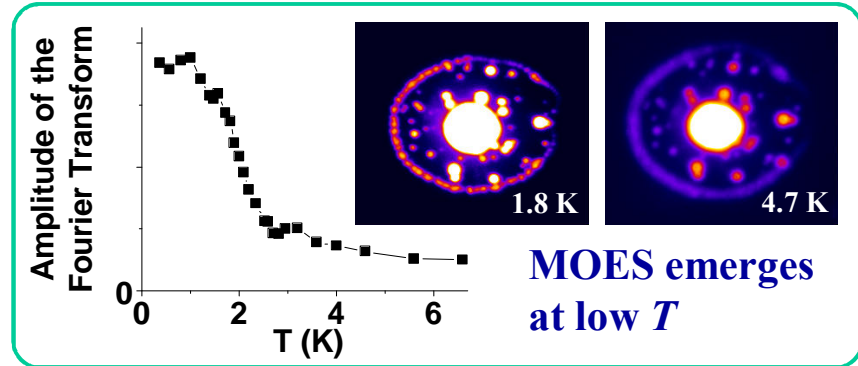
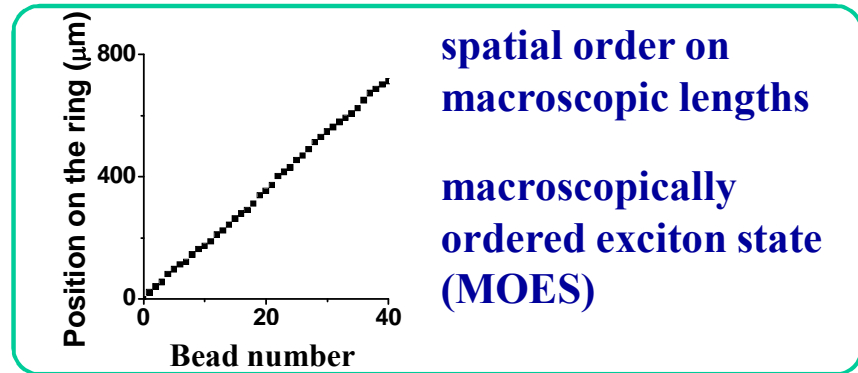
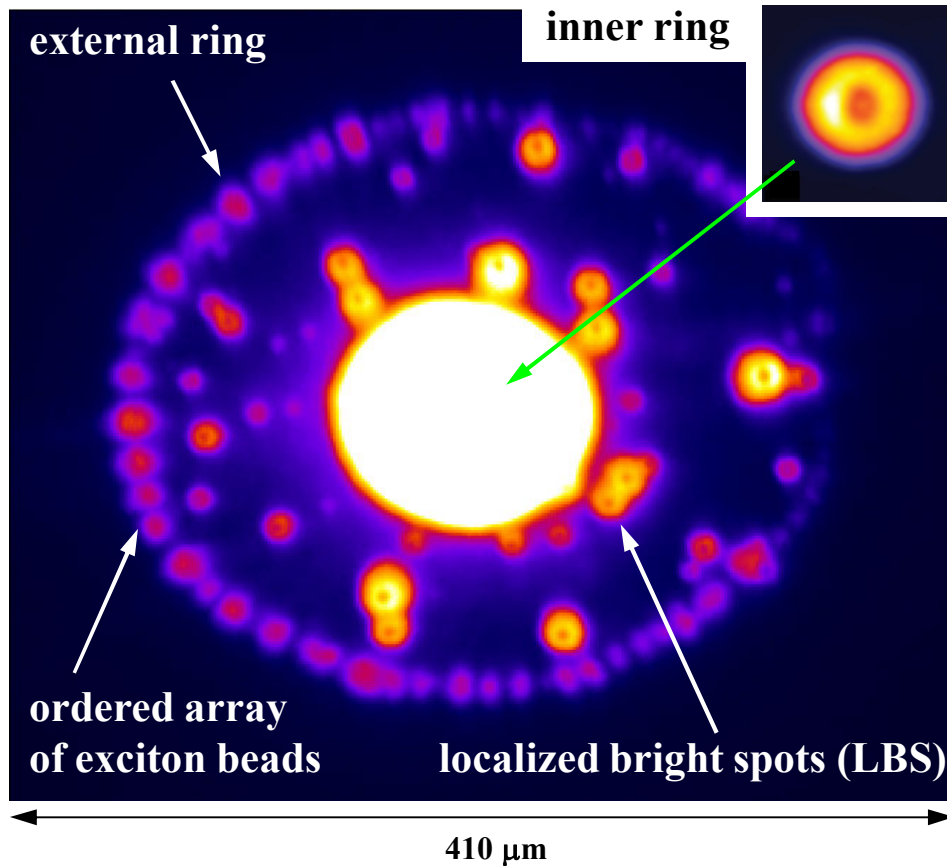
below the temperature of quantum degeneracy bosonic particles can form a **coherent state**
condensation in momentum space \leftrightarrow **spontaneous coherence of matter waves**



theoretical predictions for **coherent states in cold exciton systems:**

- **BEC** L.V. Keldysh, A.N. Kozlov, JETP 27, 521 (1968)
- **BCS-like condensate** L.V. Keldysh, Yu.V. Kopaev, Phys. Solid State 6, 2219 (1965)
- **charge-density-wave** X.M. Chen, J.J. Quinn, PRL 67, 895 (1991)
- **condensate with SO coupling** Congjun Wu, Ian Mondragon-Shem, arXiv:0809.3532

Exciton rings and macroscopically ordered exciton state

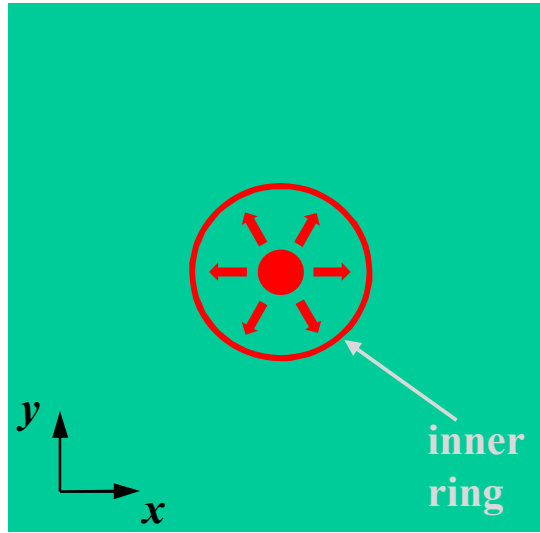
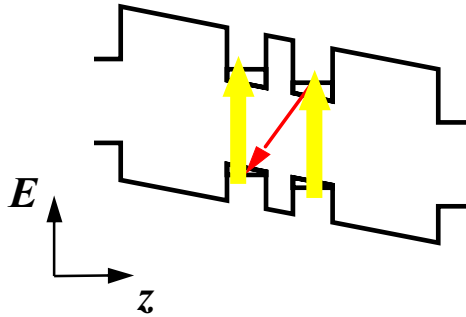


L.V. Butov, A.C. Gossard, D.S. Chemla,
Nature 418, 751 (2002)

model of

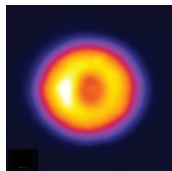
- **inner ring:** A.L. Ivanov, L. Smallwood, A. Hammack, Sen Yang, L.V. Butov, A.C. Gossard, EPL 73, 920 (2006)
- **external ring:** L.V. Butov, L.S. Levitov, B.D. Simons, A.V. Mintsev, A.C. Gossard, D.S. Chemla, PRL 92, 117404 (2004)
R. Rapaport, G. Chen, D. Snoke, S.H. Simon, L. Pfeiffer, K. West, Y. Liu, S. Denev, PRL 92, 117405 (2004)
- **MOES:** L.S. Levitov, B.D. Simons, L.V. Butov, PRL 94, 176404 (2005)

laser excitation
creates **excitons**
in CQW



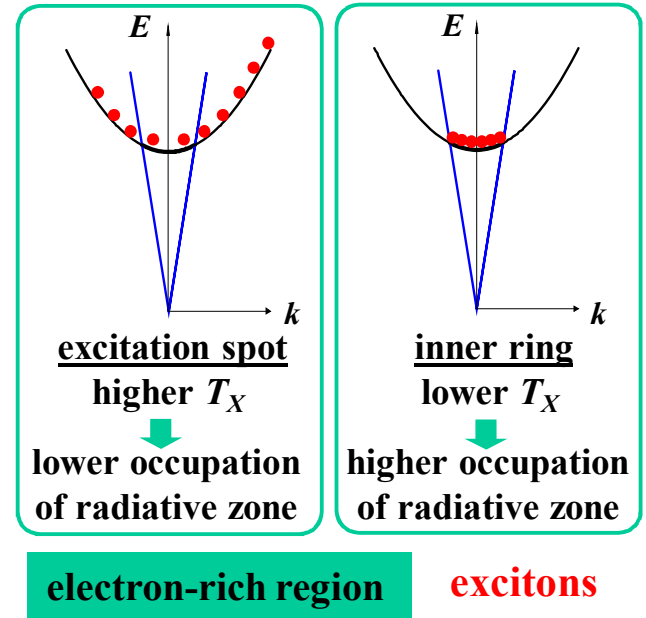
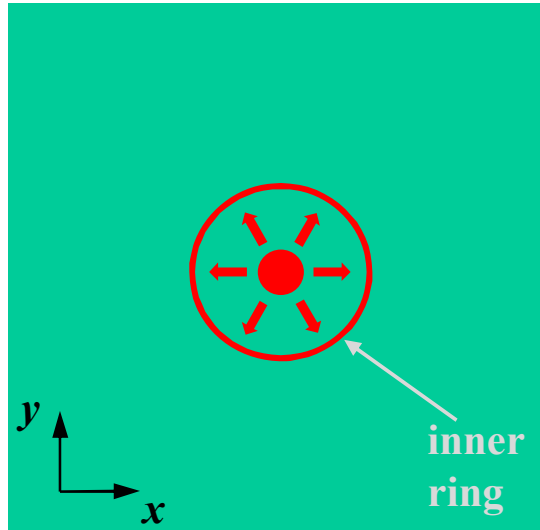
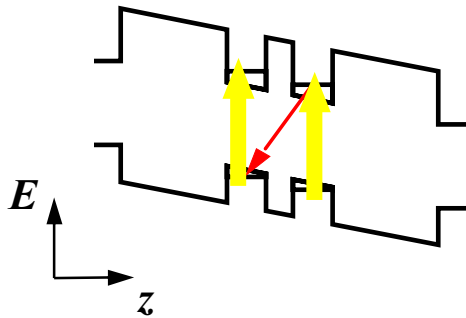
electron-rich region **excitons**

inner ring forms due to transport and cooling of optically generated excitons

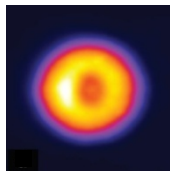


emission of indirect excitons

laser excitation
creates **excitons**
in CQW

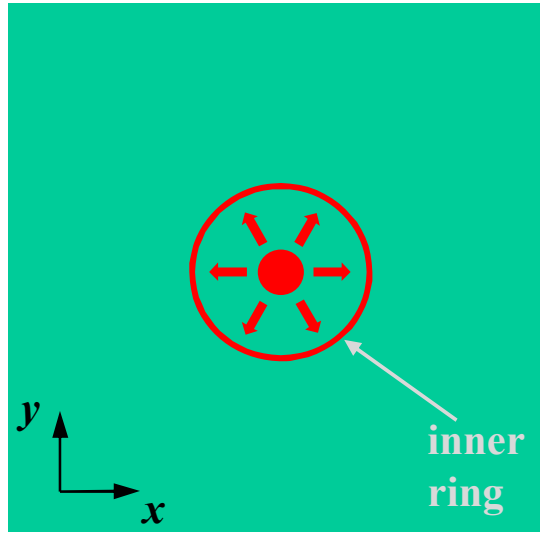
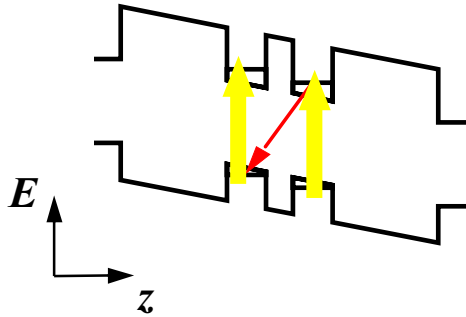


inner ring forms due to transport and cooling of optically generated excitons



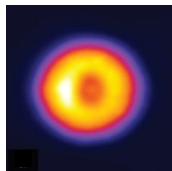
emission of indirect excitons

laser excitation
creates **excitons**
in CQW



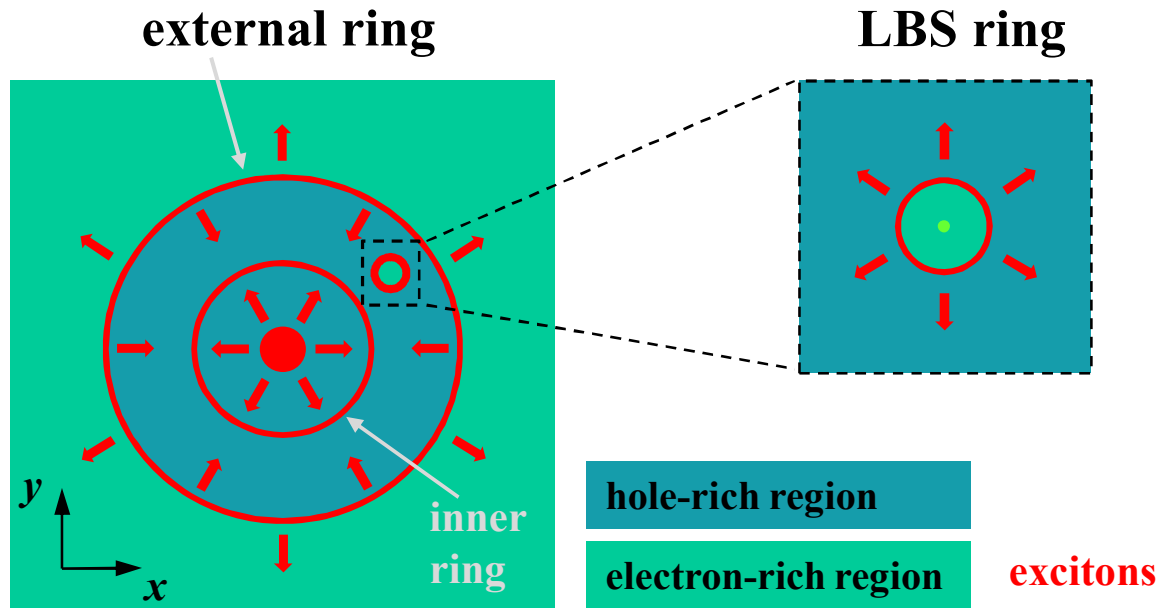
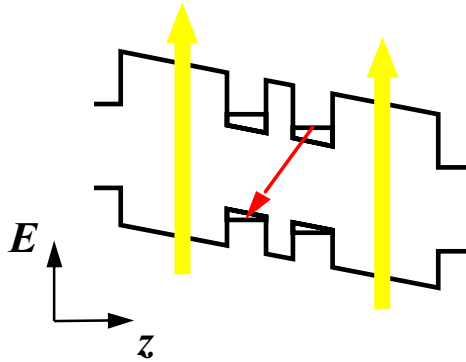
electron-rich region **excitons**

inner ring forms due to transport and cooling of optically generated excitons

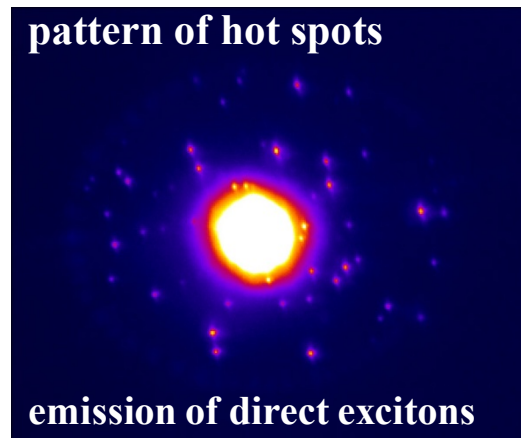
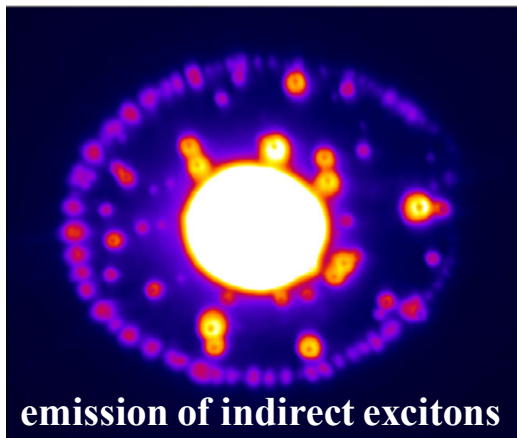


emission of indirect excitons

above barrier laser excitation
creates **excitons** + **holes**
in CQW



excitons are generated in external ring and LBS rings
at ring shaped interface between **electron**-rich and **hole**-rich regions



external rings and LBS rings
form sources of cold excitons

exciton gas
is hot in LBS centers
is cold in external ring and LBS rings

measured by
shift-interferometry

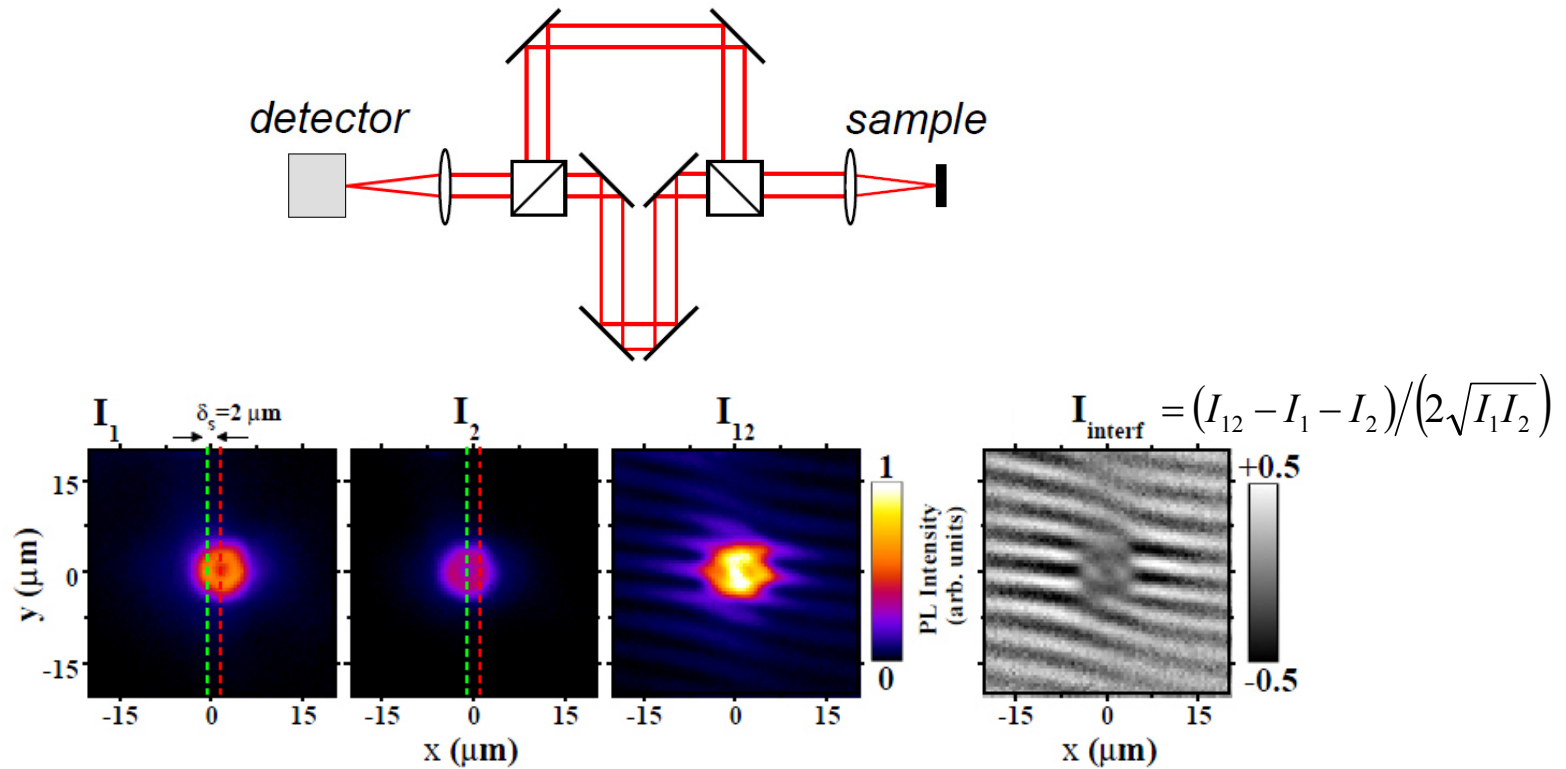


**spontaneous coherence
and
spin polarization textures**



measured by
polarization resolved imaging

First order coherence function $g_1(\delta x)$

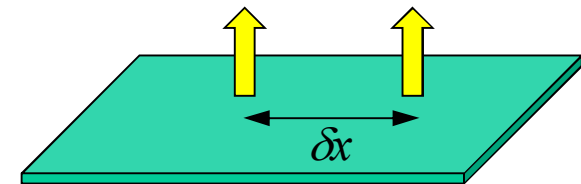


Pattern of $g_1(\delta x)$ is measured by shift-interferometry

$$g(t, \mathbf{r}) = \langle E(t' + t, \mathbf{r}' + \mathbf{r}) E(t', \mathbf{r}') \rangle / \langle E^2(t', \mathbf{r}') \rangle$$

Images produced by arm 1 and 2 of MZ interferometer are shifted to measure interference between emission of excitons separated by δx

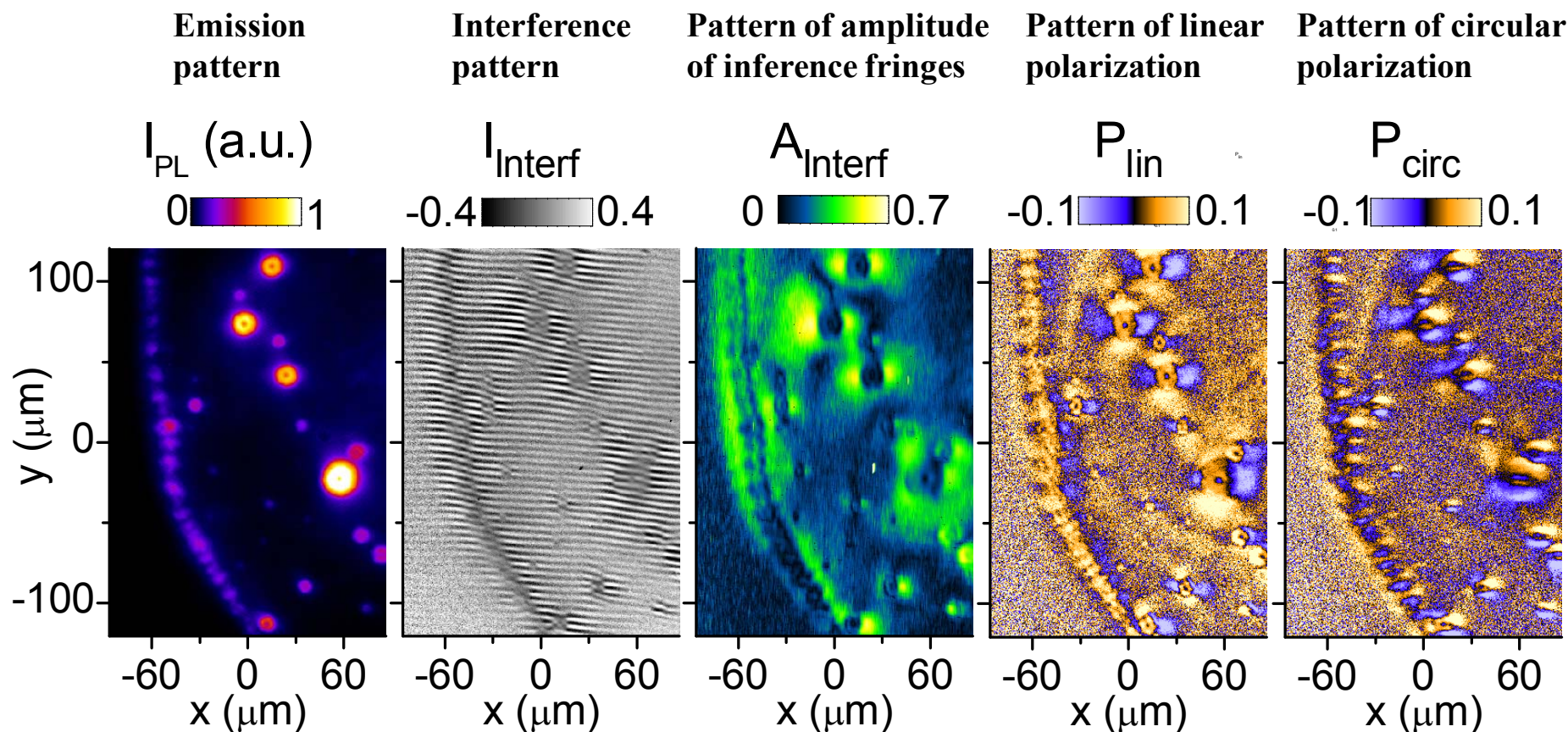
Contrast of interference fringes $A_{\text{interf}}(\delta x) \rightarrow g_1(\delta x)$



exciton coherence is imprinted on coherence of their light emission

Pattern of spin polarization is measured by polarization resolved imaging

Emission, interference, coherence degree, and polarization patterns

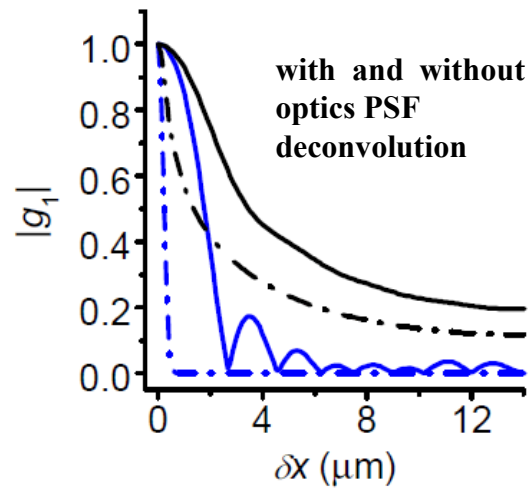
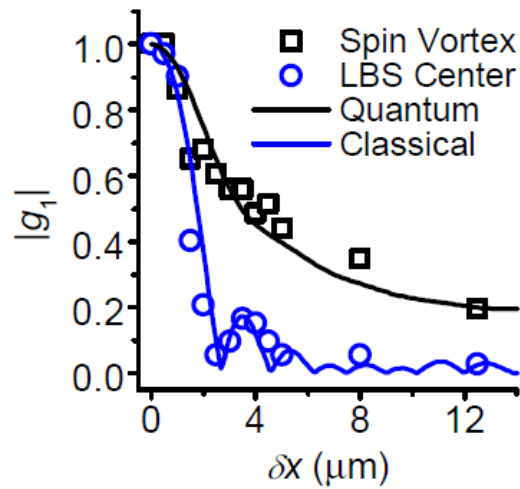


A.A. High, J.R. Leonard, A.T. Hammack, M.M. Fogler, L.V. Butov, A.V. Kavokin, K.L. Campman, A.C. Gossard, Nature 483, 584 (2012)

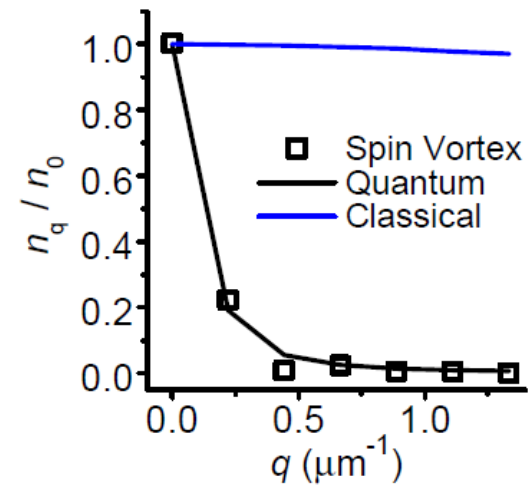
map of coherence degree
green: regions of spontaneous coherence of excitons

A.A. High, A.T. Hammack, J.R. Leonard, Sen Yang, L.V. Butov, T. Ostatnický, A.V. Kavokin, A.C. Gossard, arXiv:1103.0321

First order coherence function $g_1(\delta x)$



Distribution in q -space n_q



$g_1(r) \xleftrightarrow{\text{Fourier transform}} n_q$ $\delta q \cdot \xi \sim 1$
 coherence length

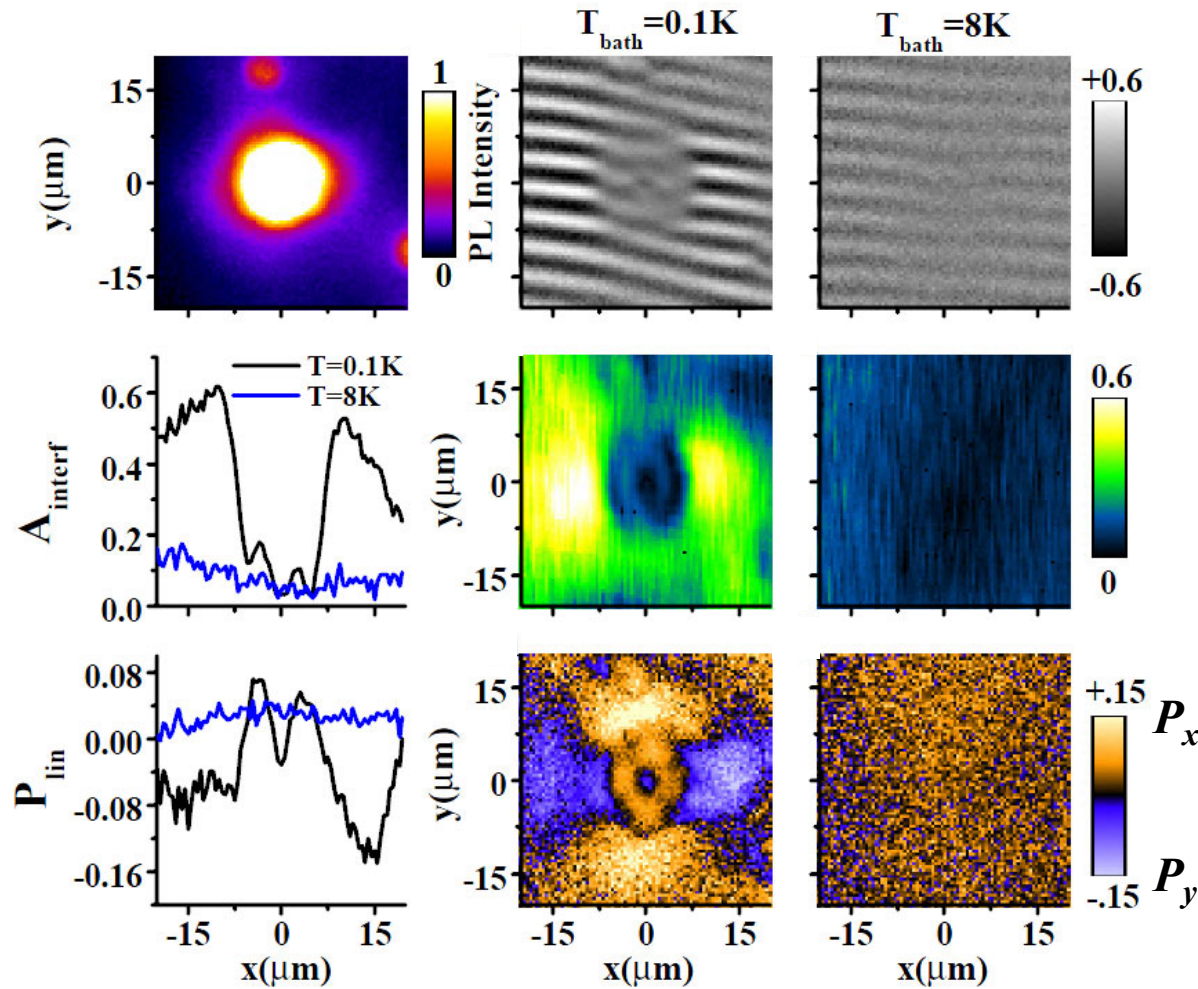
Classical gas: narrow $g_1(r)$ and broad n_q
 $\xi_{\text{classical}} \sim \lambda_{\text{dB}} / \pi^{1/2} \sim 0.3 \mu\text{m}$ at 0.1 K

Quantum gas: extended $g_1(r)$ and narrow n_q
 $\xi \gg \xi_{\text{classical}}$
 $\delta q \ll \delta q_{\text{classical}}$
characteristic of a condensate

$\xi \sim \xi_0 = \sqrt{\frac{n_0}{4\pi}} \lambda_{\text{dB}} \longleftarrow g_1(r) \sim \int d^2 q e^{iqr} n_q$

A_{interf} is given by convolution of g_1 with point-spread function (PSF) of optics

Exciton coherence and spin texture around LBS-ring



Emergence of

- Spontaneous coherence
- Spin polarization vortex at low T at $r > r_0$

at $r = r_0$

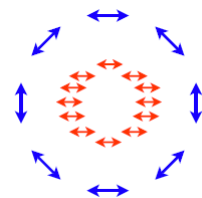
- average momentum drops
- coherence degree rises

enhancement of amplitude of interference fringes

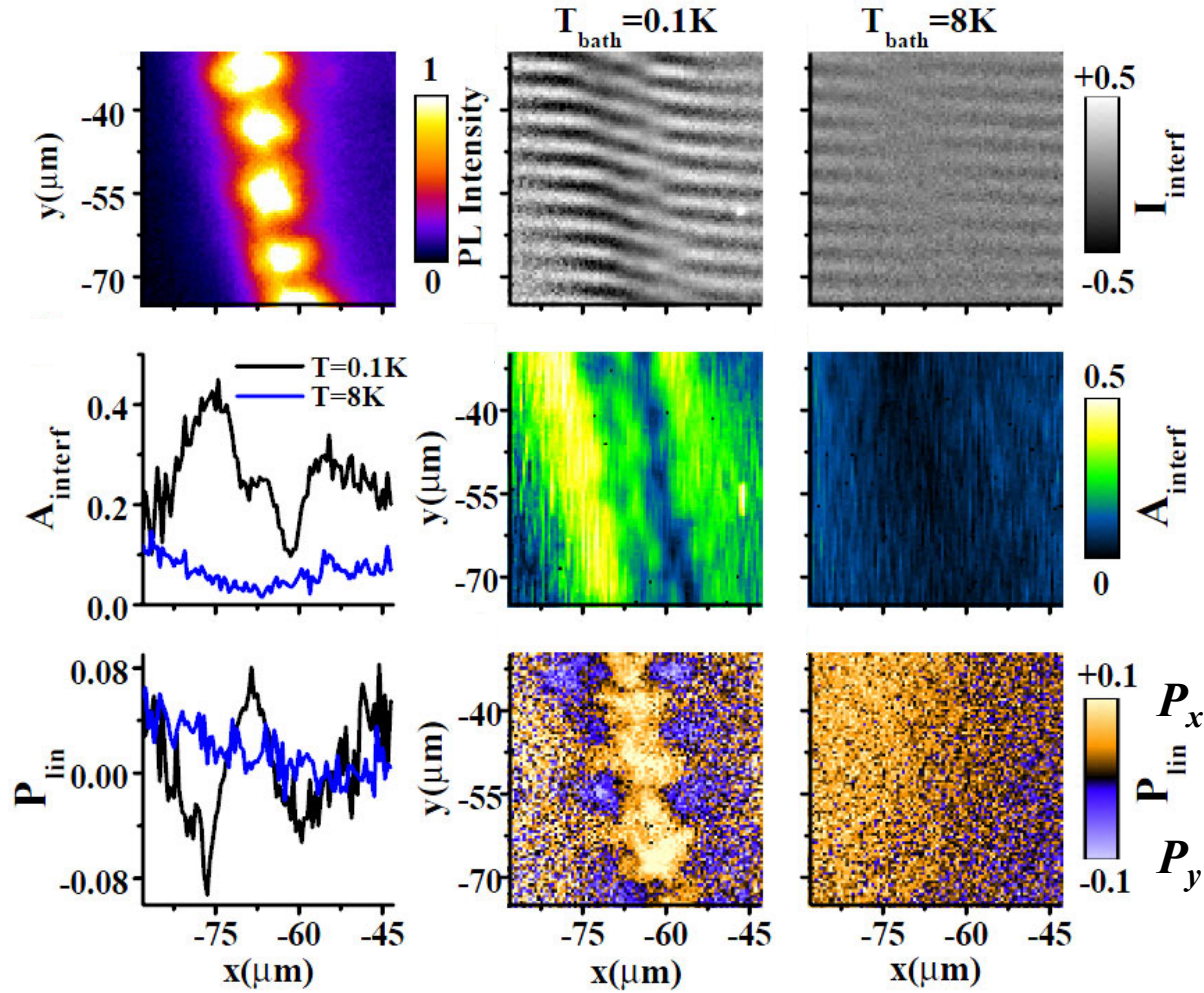
shift in phase of interference fringes

vortex of linear polarization

ring of linear polarization



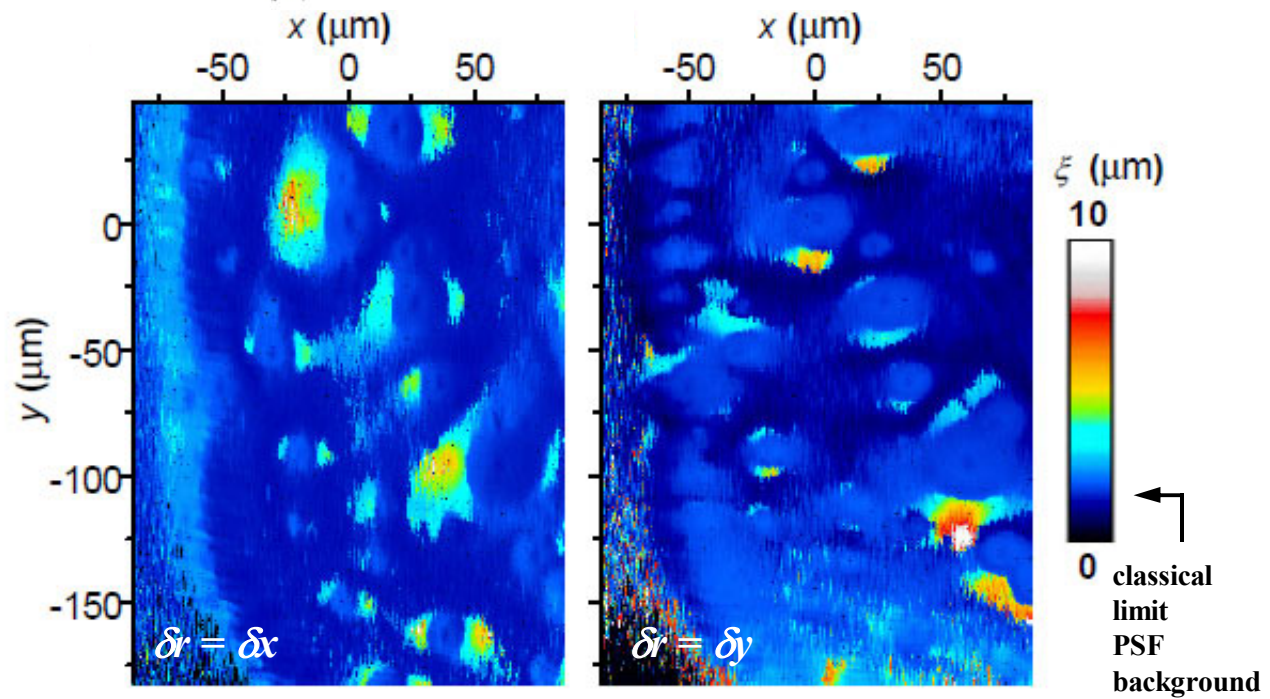
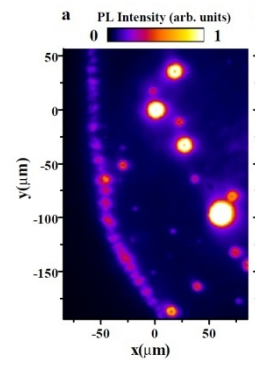
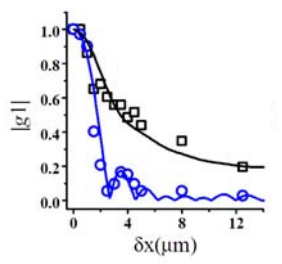
Exciton coherence and spin texture around external ring



Emergence of

- Spontaneous coherence
 - Periodic spin texture
- at low T at $r > r_0^*$

Pattern of coherence length $\xi(x, y)$



spontaneous coherence of excitons emerges

- in region of MOES
- in region of vortices of linear polarization

$\xi \gg \xi_{\text{classical}}$
 $\delta q \ll \delta q_{\text{classical}}$

directional property of exciton coherence:
 extension of $g_1(r)$ is higher when exciton propagation direction is along vector r

phase singularities

**in singly quantized vortex
phase of wavefunction winds by 2π around singularity point**



fork-like defect in phase pattern can be signature of quantized vortex

vortices in atom BEC

S. Inouye, S. Gupta, T. Rosenband, A.P. Chikkatur, A. Görlitz, T.L. Gustavson, A.E. Leanhardt, D.E. Pritchard, W. Ketterle, PRL 87, 080402 (2001)

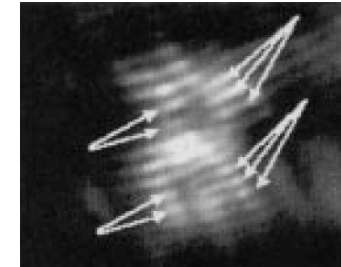
F. Chevy, K.W. Madison, V. Bretin, J. Dalibard, PRA 64, 031601(R) (2001)

Z. Hadzibabic, P. Krüger, M. Cheneau, B. Battelier, J. Dalibard, Nature 441, 1118 (2006)



optical vortices

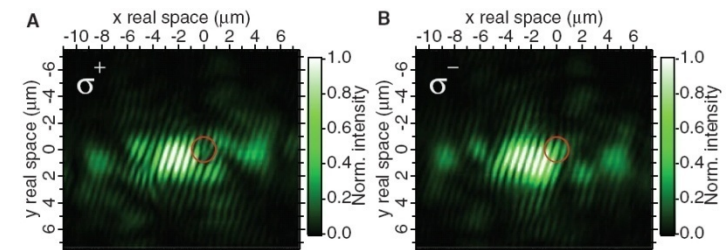
J. Scheuer, M. Orenstein, Science 285, 230 (1999)
and references therein



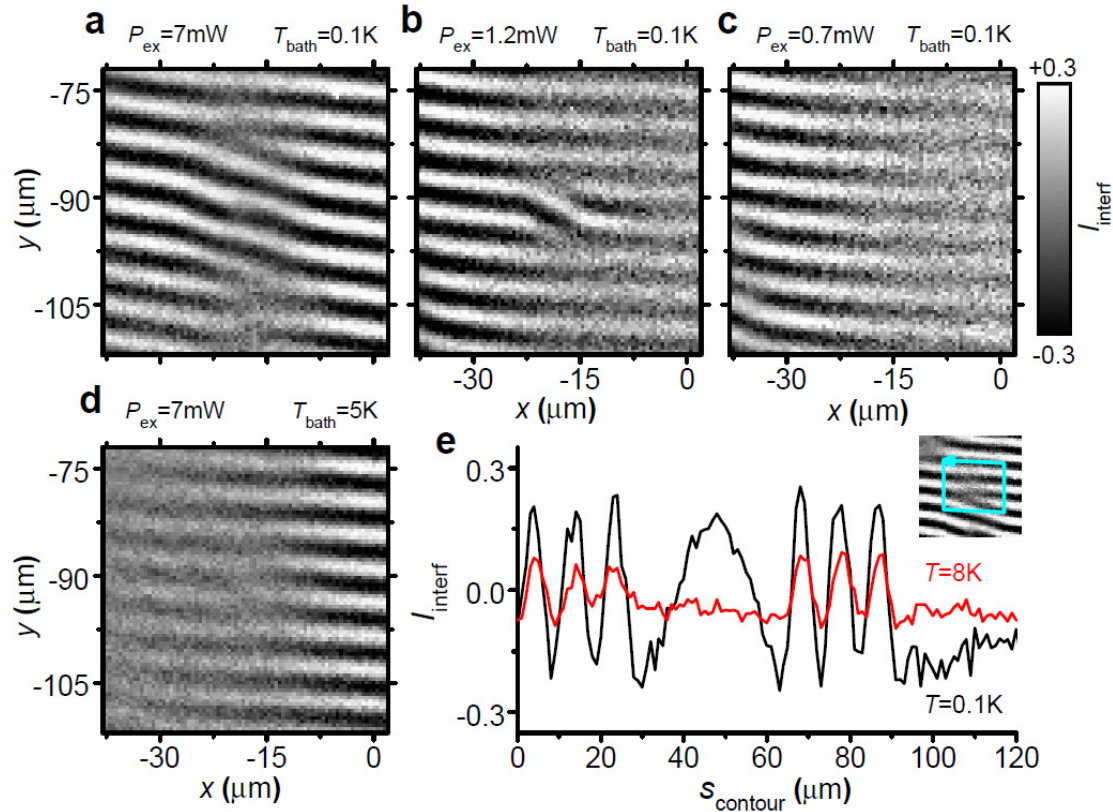
polariton vortices

K.G. Lagoudakis, M. Wouters, M. Richard, A. Baas, I. Carusotto, R. André, Le Si Dang, B. Deveaud-Plédran, Nature Physics 4, 706 (2008)

K.G. Lagoudakis, T. Ostatnický, A.V. Kavokin, Y.G. Rubo, R. André, B. Deveaud-Plédran, Science 326, 974 (2009)



Fork-like defects in exciton interference pattern



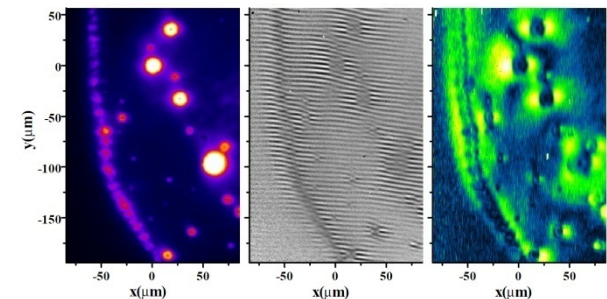
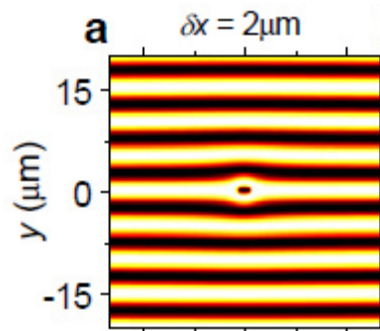
Forks are observed at low T in quantum exciton gas, vanish at high T in classical gas

Phase of interference fringes on closed contour winds by 2π indicating phase singularity

Distance between left- and right-facing forks \neq shift in shift-interferometry

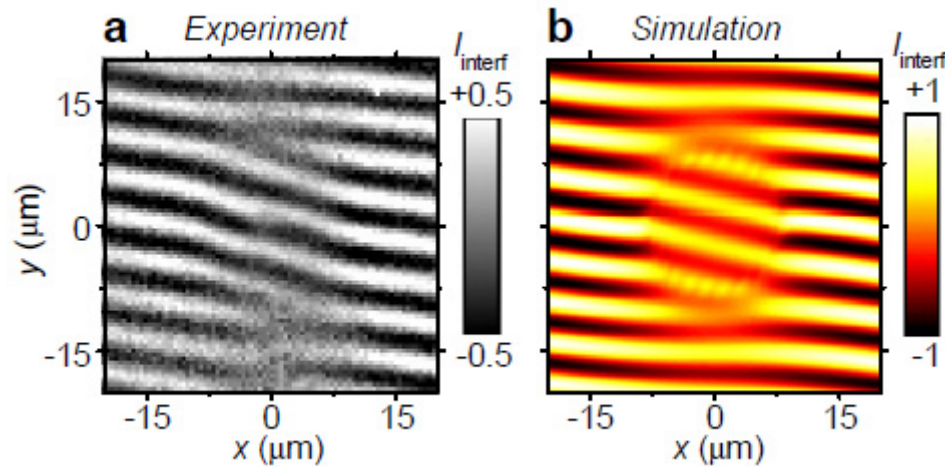


Observed phase singularity is different from a regular quantized vortex



Modeling

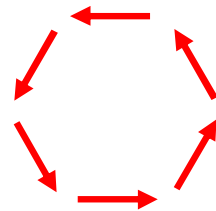
Fork-like defects in interference pattern



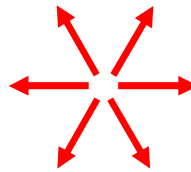
Ring-shaped source \rightarrow interference pattern with left- and right-facing forks with distance between them \gg shift

Ring-shaped source produces more complicated phase pattern than vortex.

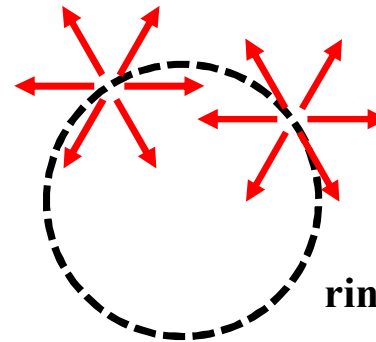
Both objects are characterized by spreading of particle velocities over all directions.



vortex



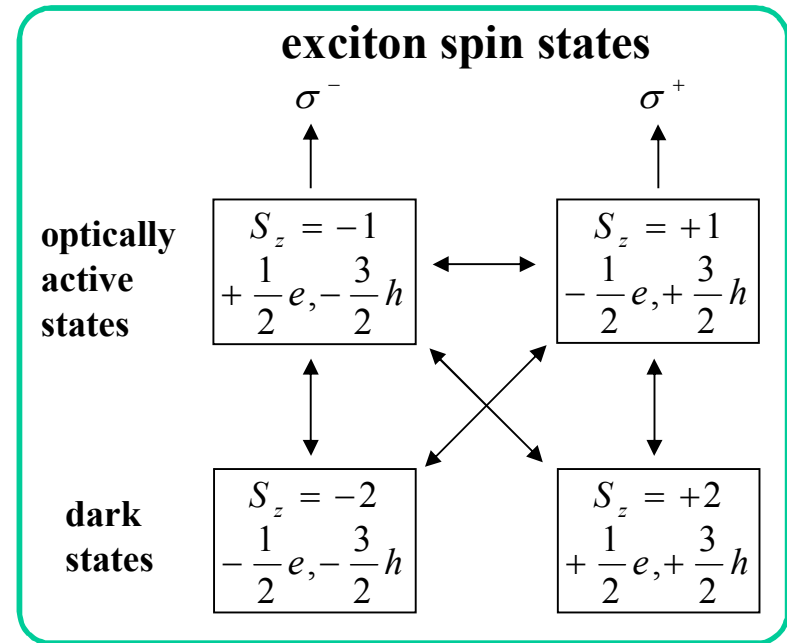
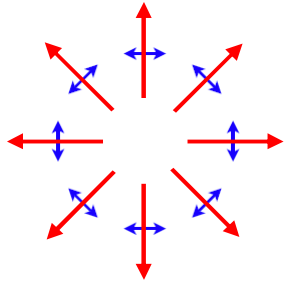
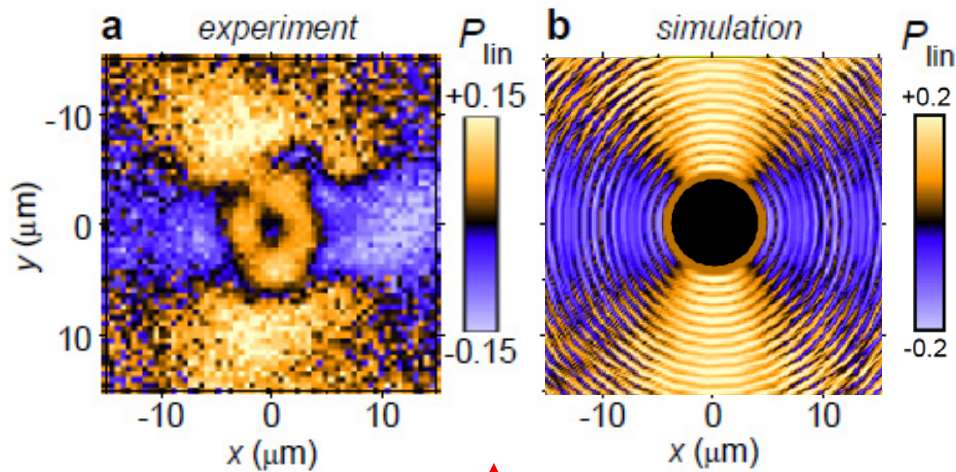
source



ring-shaped source

Spin polarization texture around LBS

– radial source of cold excitons



coherent exciton transport with suppressed scattering
and precession of spins of electrons and holes
 due to splitting of exciton states with different spins



vortex of linear polarization

← due to splitting of linearly polarized exciton states and spin-orbit interaction

measured by
polarization resolved imaging



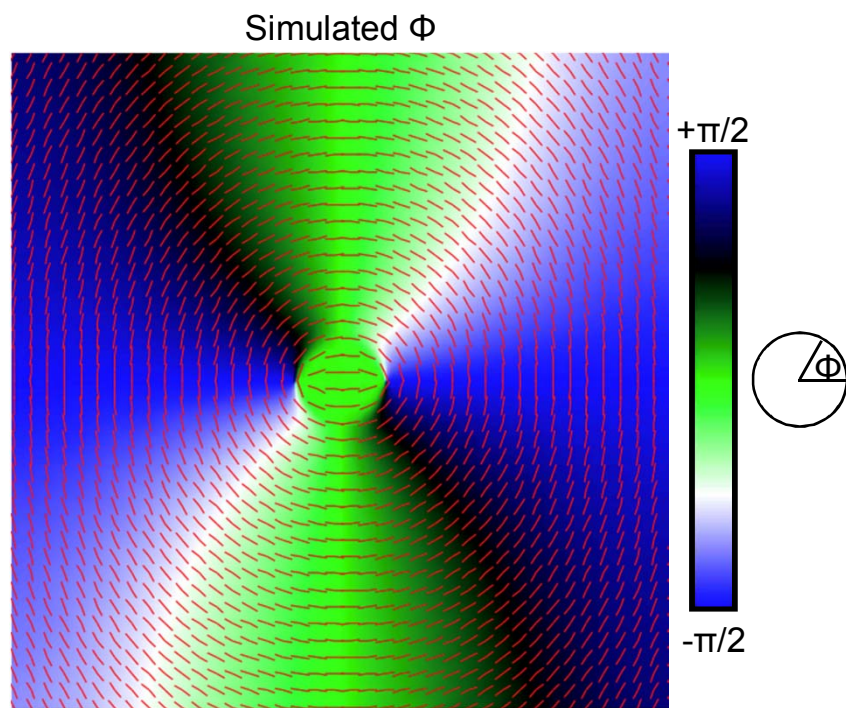
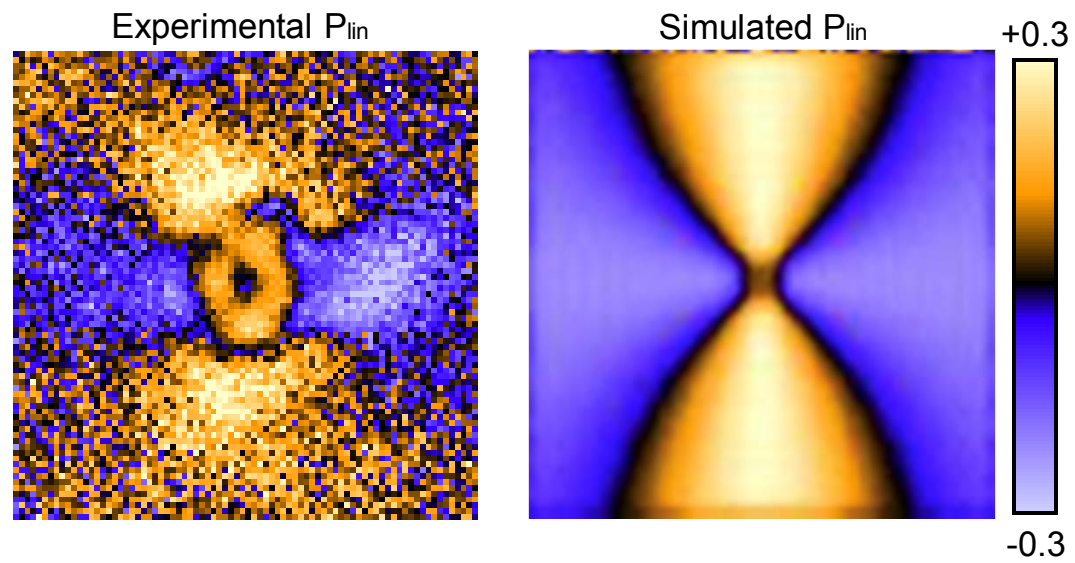
control of spin currents



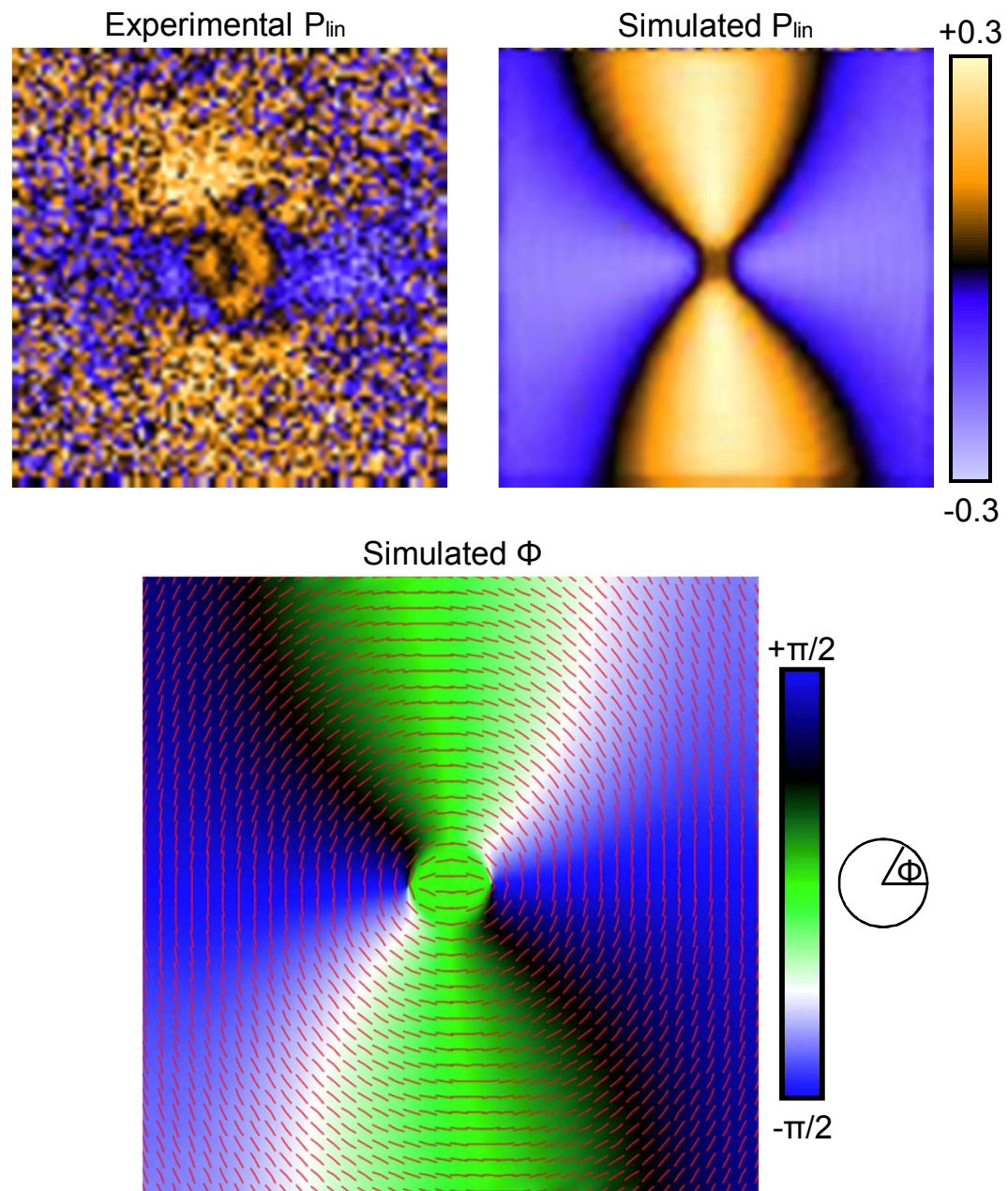
by magnetic field

work in progress

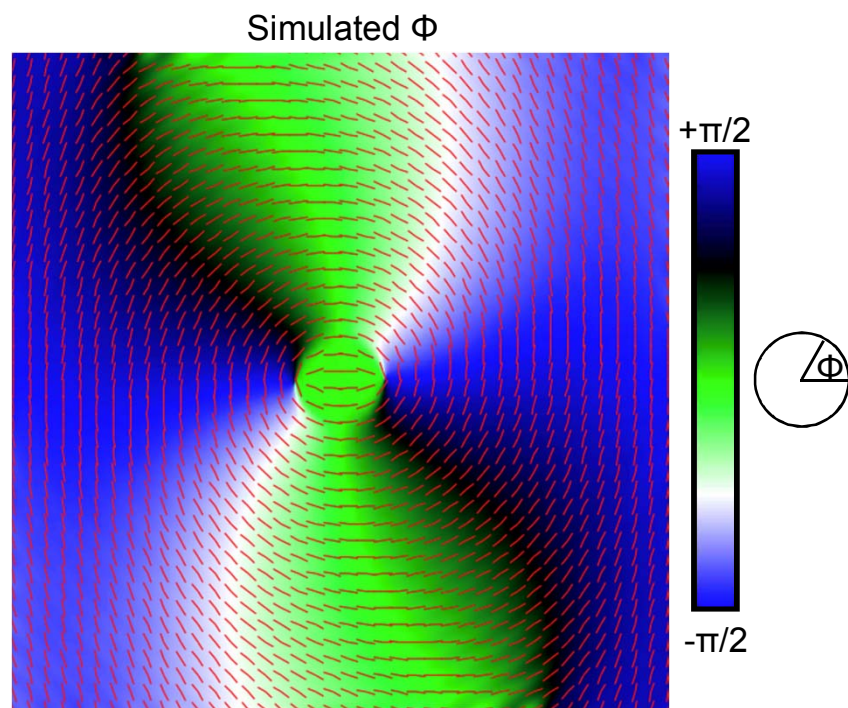
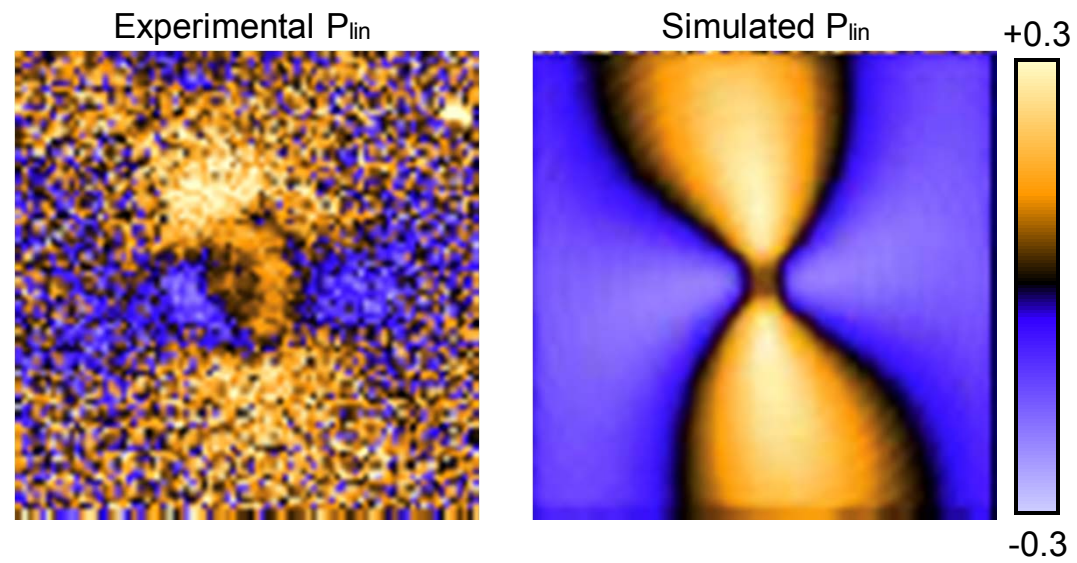
B=0T



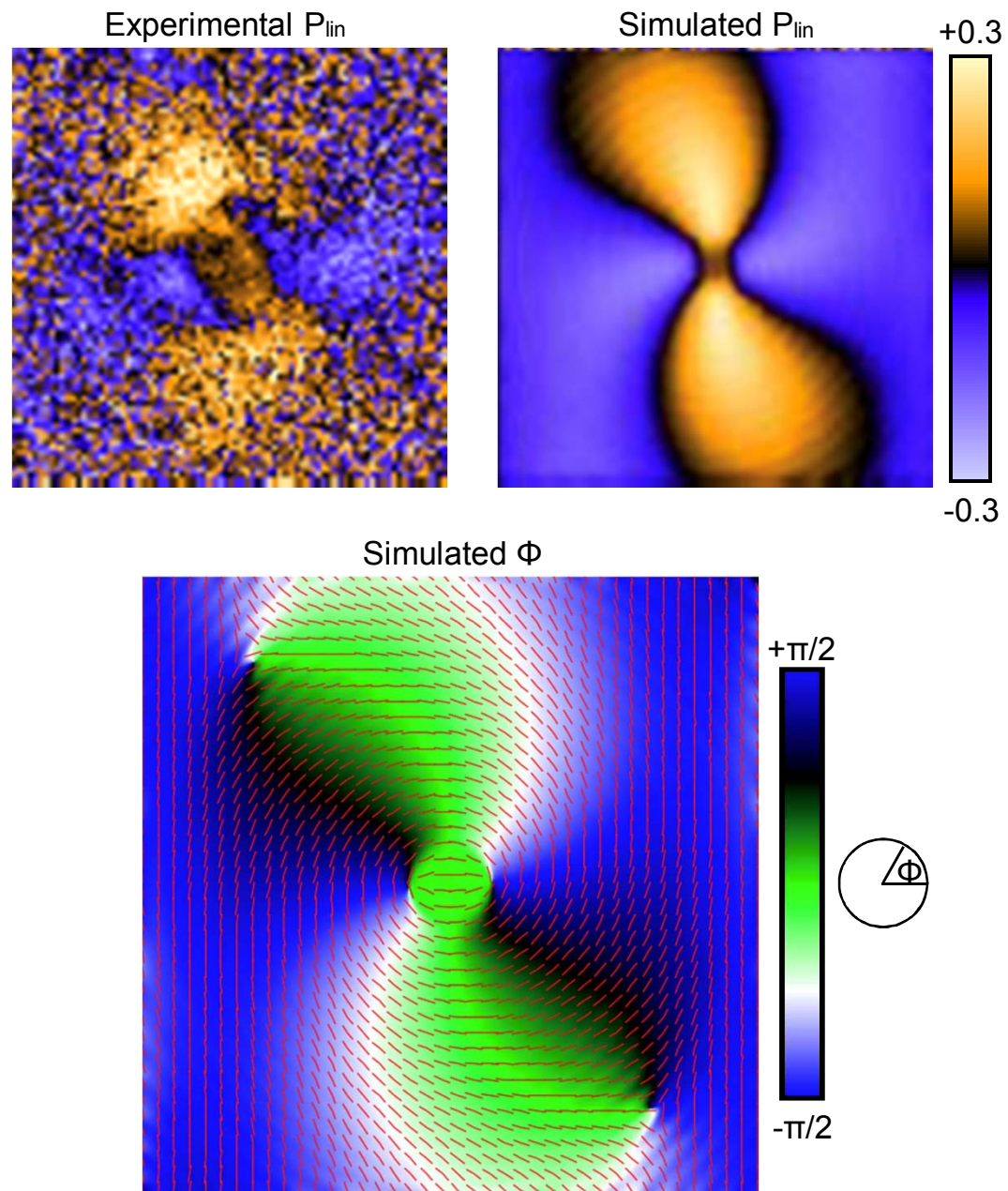
B=1T



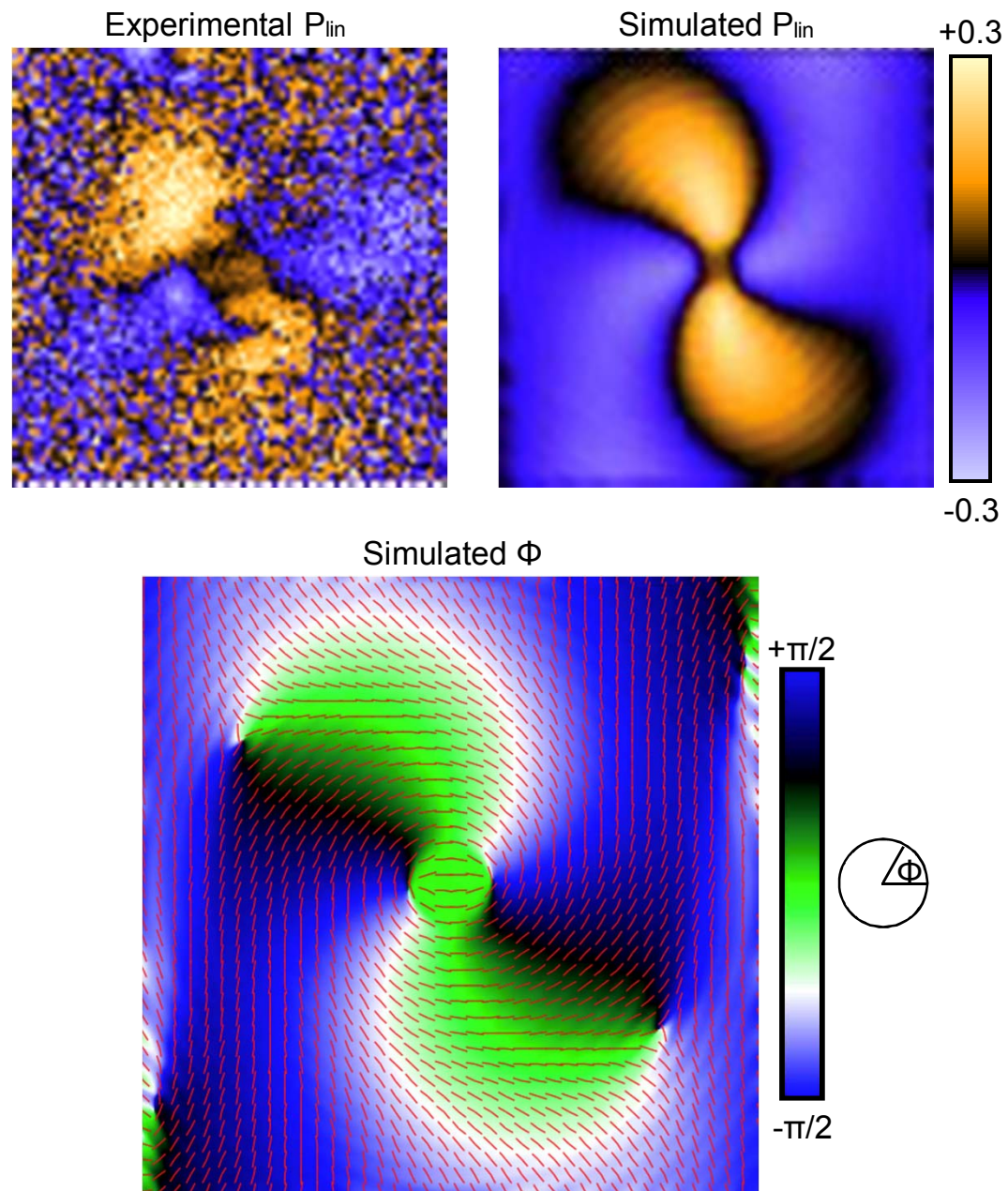
$B=2T$



B=3T

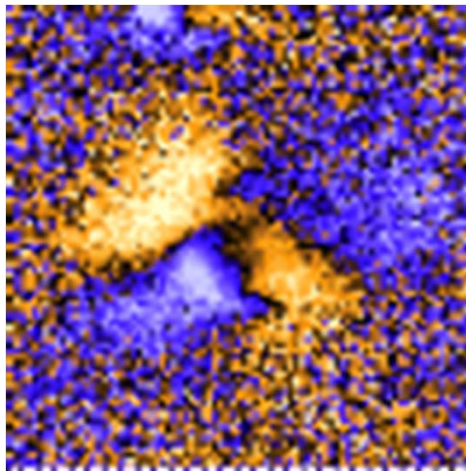


B=4T

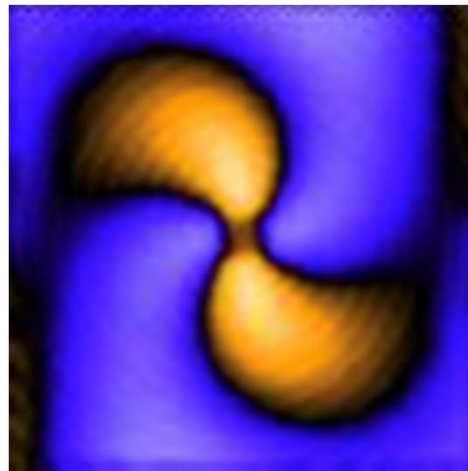


B=5T

Experimental P_{lin}



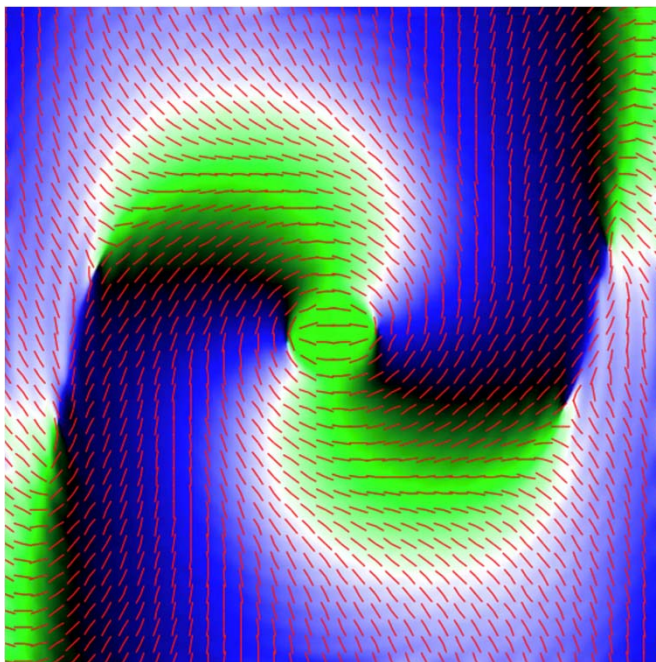
Simulated P_{lin}



+0.3

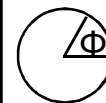
-0.3

Simulated Φ



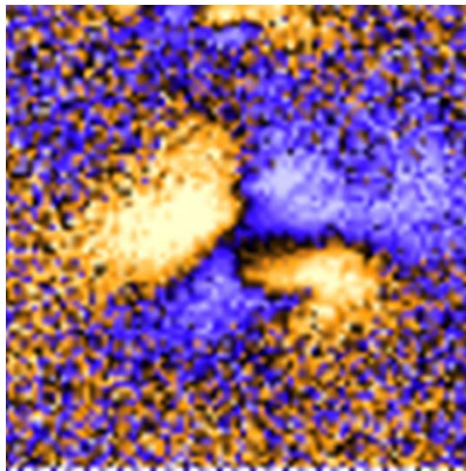
$+\pi/2$

$-\pi/2$

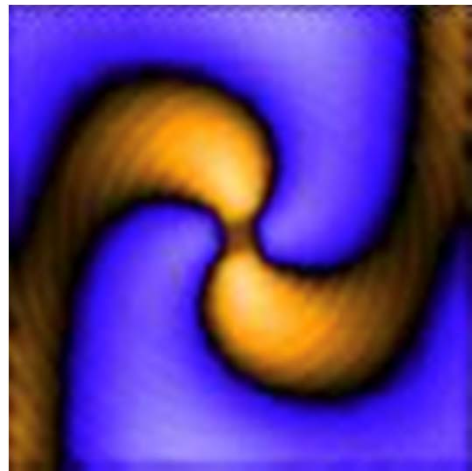


B=6T

Experimental P_{lin}



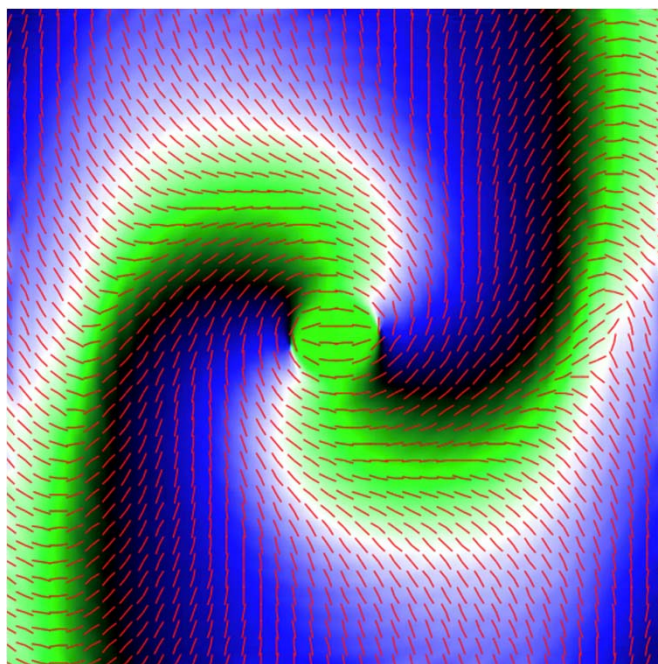
Simulated P_{lin}



+0.3

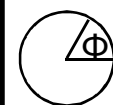
-0.3

Simulated Φ

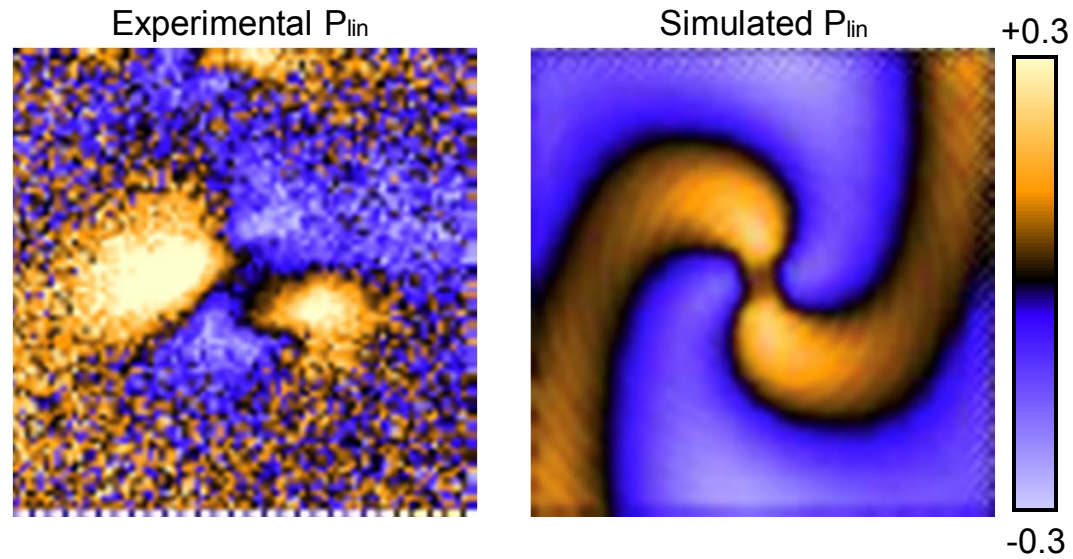


$+\pi/2$

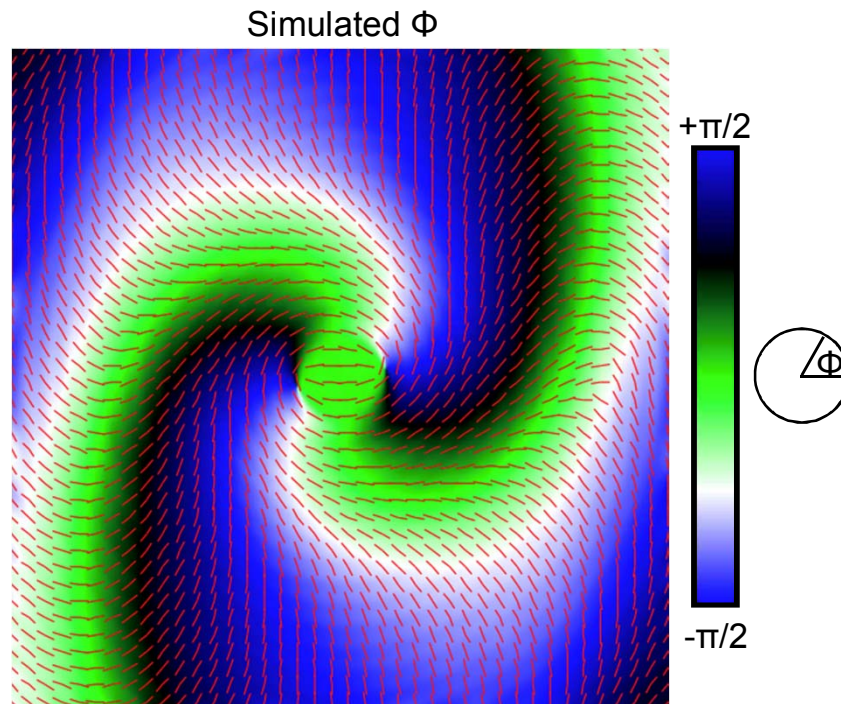
$-\pi/2$



B=7T



**direction of spin current
 \neq
direction of density current**

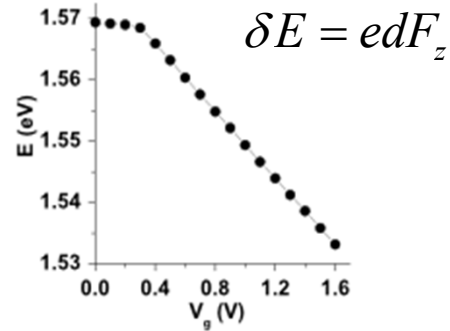
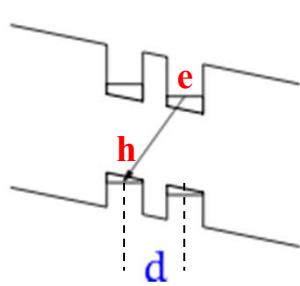


A.A. High, A.T. Hammack,
J.R. Leonard, Sen Yang,
L.V. Butov, T. Ostatnický,
M. Vladimirova, A.V.
Kavokin, K.L. Campman,
A.C. Gossard, unpublished

work in progress

excitonic devices

potential energy of indirect excitons can be controlled by an applied gate voltage



**in-plane potential landscapes
can be created for excitons by voltage pattern
e.g. circuit devices, traps, lattices**

the ability to control exciton fluxes by an applied gate voltage

excitonic devices

delay between signal processing and optical communication is effectively eliminated in excitonic devices

→ advantage in applications where interconnection speed is important

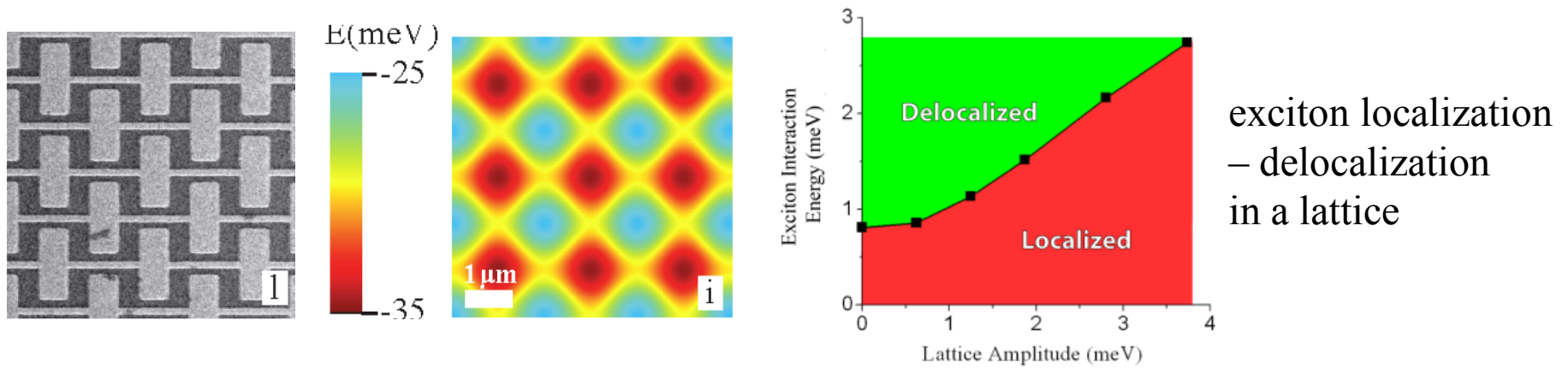
traps for excitons

and other potential landscapes

**control of shape and depth of a trap, lattice, or another potential landscape
→ tool for studying basic properties of excitons**

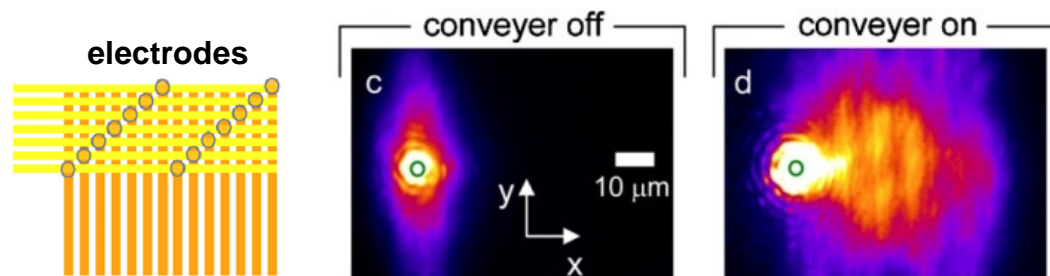
traps and lattices are effectively used in studies of cold atoms

Lattices for excitons



M. Remeika, J.C. Graves, A.T. Hammack, A.D. Meyertholen, M.M. Fogler, L.V. Butov, M. Hanson, A.C. Gossard, *Phys. Rev. Lett.* 102, 186803 (2009)

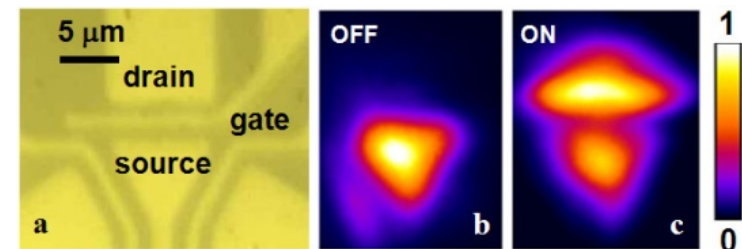
M. Remeika, M.M. Fogler, L.V. Butov, M. Hanson, A.C. Gossard, *Appl. Phys. Lett.* 100, 061103 (2012)



Excitonic conveyers / CCD

realize controlled transport of excitons

A.G. Winbow, J.R. Leonard, M. Remeika, Y.Y. Kuznetsova, A.A. High, A.T. Hammack, L.V. Butov, J. Wilkes, A.A. Guenther, A.L. Ivanov, M. Hanson, A.C. Gossard, *Phys. Rev. Lett.* 106, 196806 (2011)



Excitonic transistors / circuits

realise excitonic signal processing

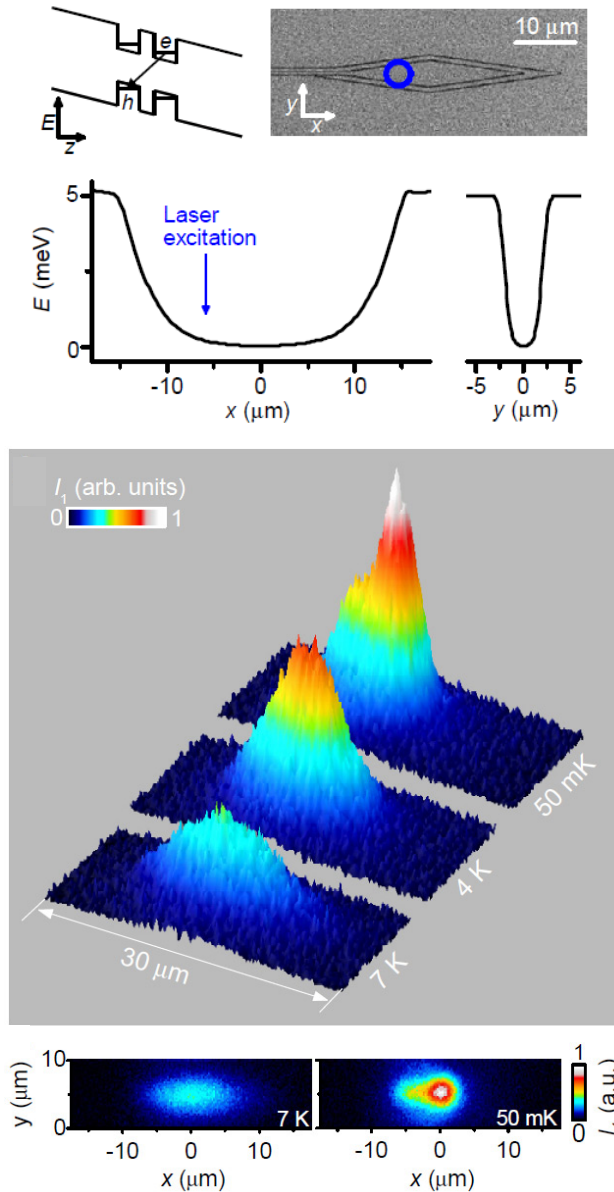
Science 321, 229 (2008)

Nature Photonics 3, 577 (2009)

Appl. Phys. Lett. 100, 231106 (2012)

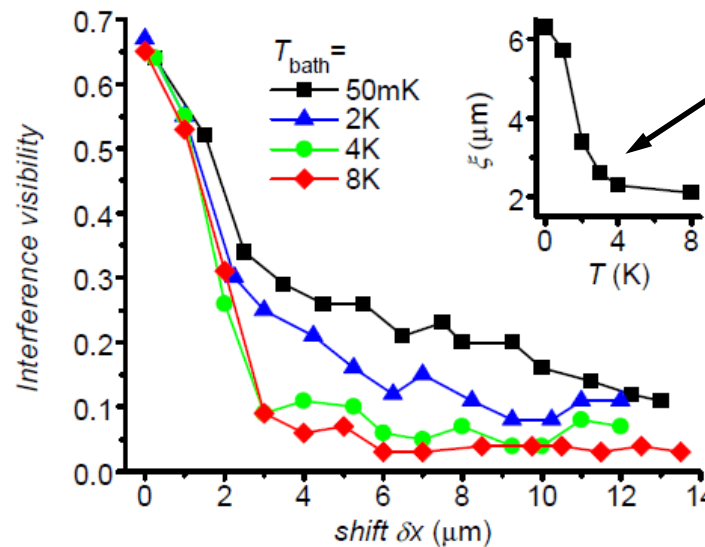
**condensation of excitons
in a trap**

Condensation of excitons in diamond trap



with lowering temperature

- excitons condense at the trap bottom
- exciton spontaneous coherence emerges



measured transition temperature ~2 K

estimates of the temperature of exciton BEC

$$T_c = \frac{\sqrt{6}}{\pi} \hbar \omega_{2D} \sqrt{N/g} \sim 2 \text{ K}$$

High $T > 4 \text{ K}$: $V(r)$ quickly drops with r and vanishes at PSF width ← signature of a **classical gas**

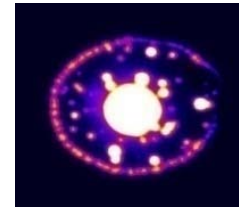
Low T : $\xi \gg \lambda_{dB}$, below $T \sim 1 \text{ K}$, coherence extends over the entire trapped cloud ← signature of a **condensate**

Cold indirect excitons:

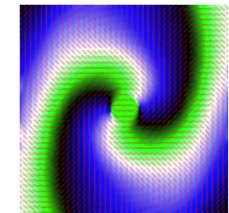
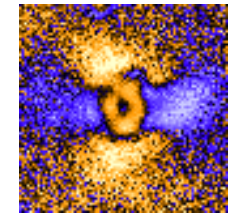
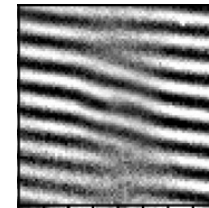
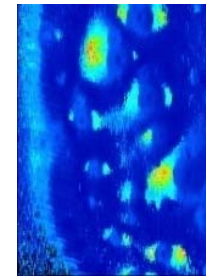
summary

- **Macroscopically ordered exciton state (MOES)**

L.V. Butov, A.C. Gossard, D.S. Chemla, Nature 418, 751 (2002)



- **Spontaneous coherence in MOES and pol. vortex**
- **Phase singularities in interference pattern**
- **Spin textures and spin currents**



A.A. High, J.R. Leonard, A.T. Hammack, M.M. Fogler, L.V. Butov, A.V. Kavokin, K.L. Campman, A.C. Gossard, Nature 483, 584 (2012)

A.A. High, A.T. Hammack, J.R. Leonard, Sen Yang, L.V. Butov, T. Ostatnický, M. Vladimirova, A.V. Kavokin, K.L. Campman, A.C. Gossard, unpublished

- **Condensation in a trap**

A.A. High, J.R. Leonard, M. Remeika, L.V. Butov, M. Hanson, A.C. Gossard, Nano Lett. 12, 2605 (2012)

